

Inelastic X-Ray Scattering & Lattice Dynamics

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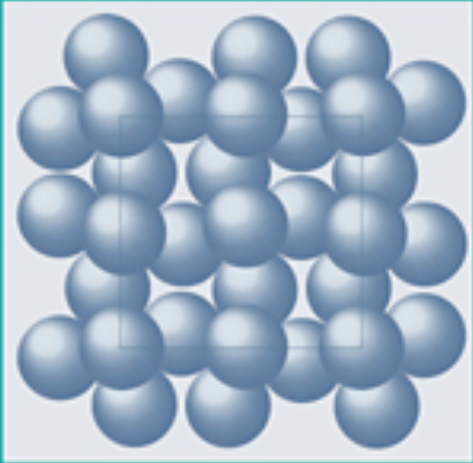
NX School 2019
June 24, 2019, Argonne National Laboratory, Argonne, IL

Thanks : T. S. Toellner, J. Zhao, M. Y. Hu, A. Alatas, W. Bi, A. Said, T. Gog

Lattice dynamics for beginners

4 Cambridge topics in
MINERAL PHYSICS AND CHEMISTRY

Introduction to Lattice Dynamics



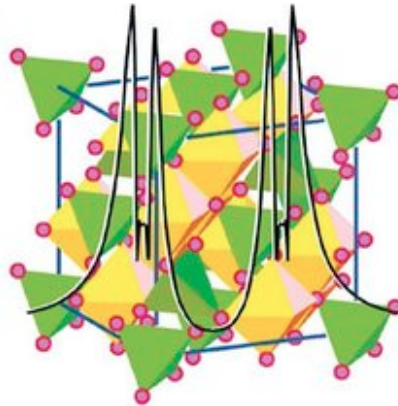
MARTIN T. DOVE

Yi-Long Chen, De-Ping Yang

WILEY-VCH

Mössbauer Effect in Lattice Dynamics

Experimental Techniques and Applications



THE PHYSICS OF PHONONS



G. P. SRIVASTAVA



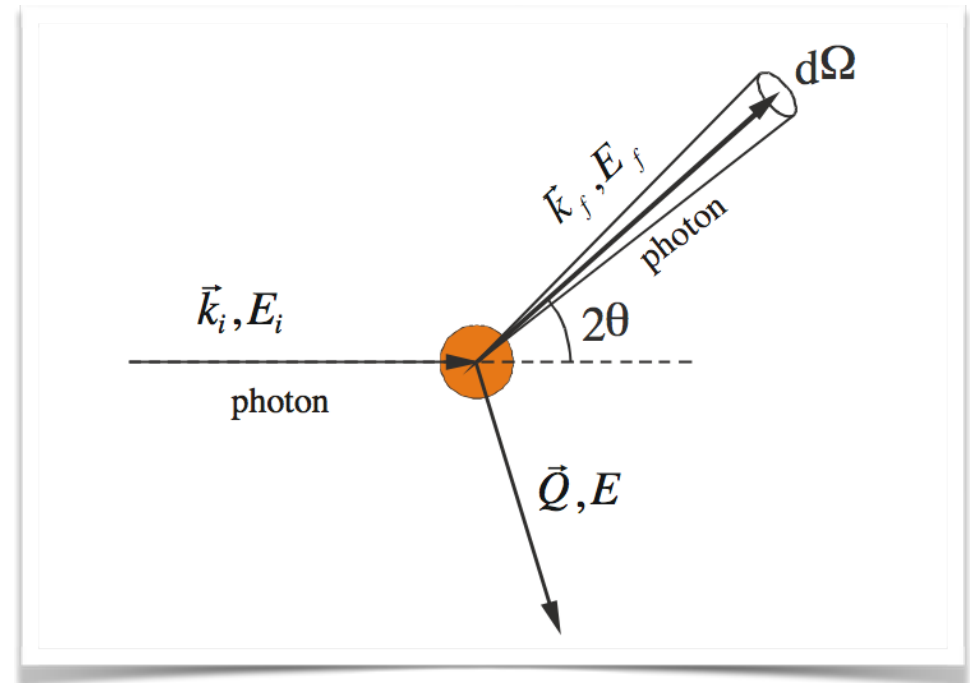
Inelastic X-Ray Scattering & Spectroscopy @ APS

IXS

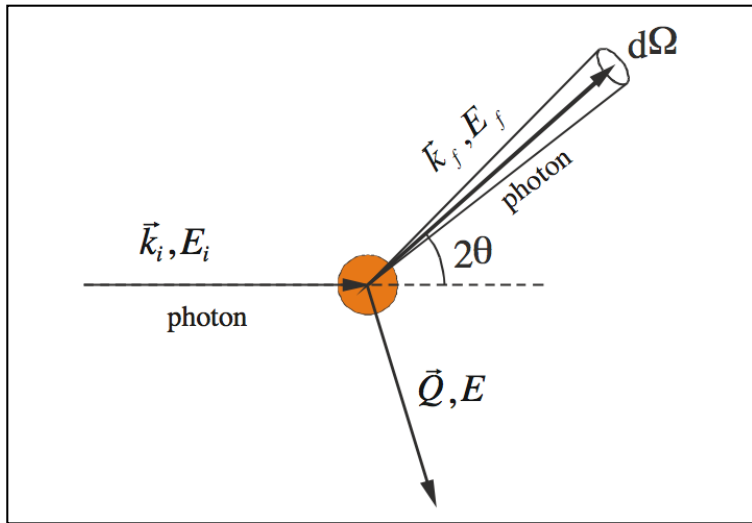
NRIXS **RIXS** **MCS**

NRIS **XES** **XRS**

Compton



- Nuclear Resonant Inelastic X-Ray scattering, NRIXS: **Sectors 3, 16, 30**
- Momentum Resolved High Energy Resolution IXS (**HERIX**) **Sectors 3, 30**
- Resonant Inelastic X-Ray Scattering, RIXS : **Sector 27**
- X-Ray Raman Scattering, XRS : **Sectors 13, 16, 20**
- X-Ray Emission Spectroscopy, XES: **Sectors 6, 13, 16, 17**



$E_i = E_f$: Elastic scattering

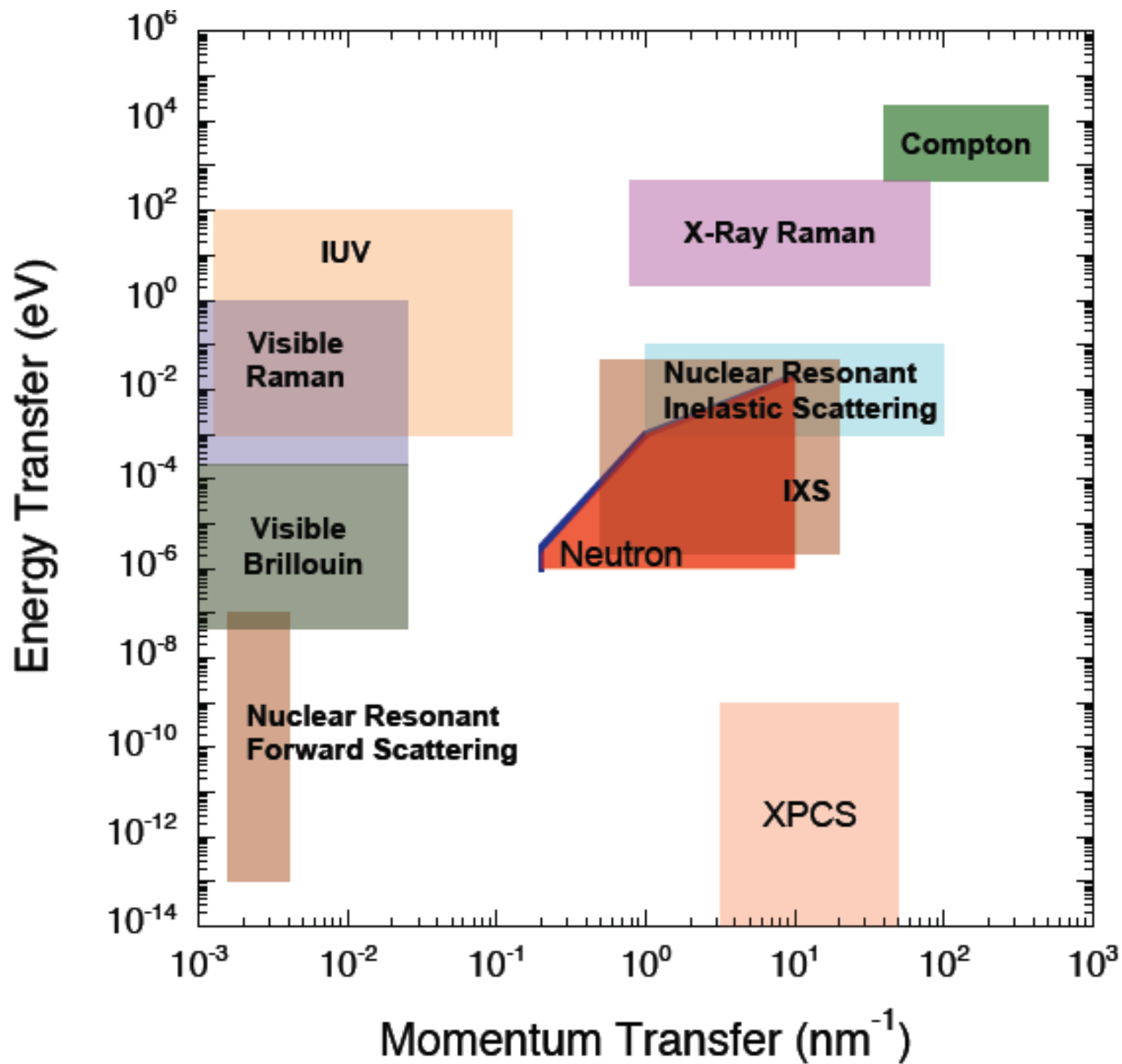
$E_i \neq E_f$: Inelastic scattering

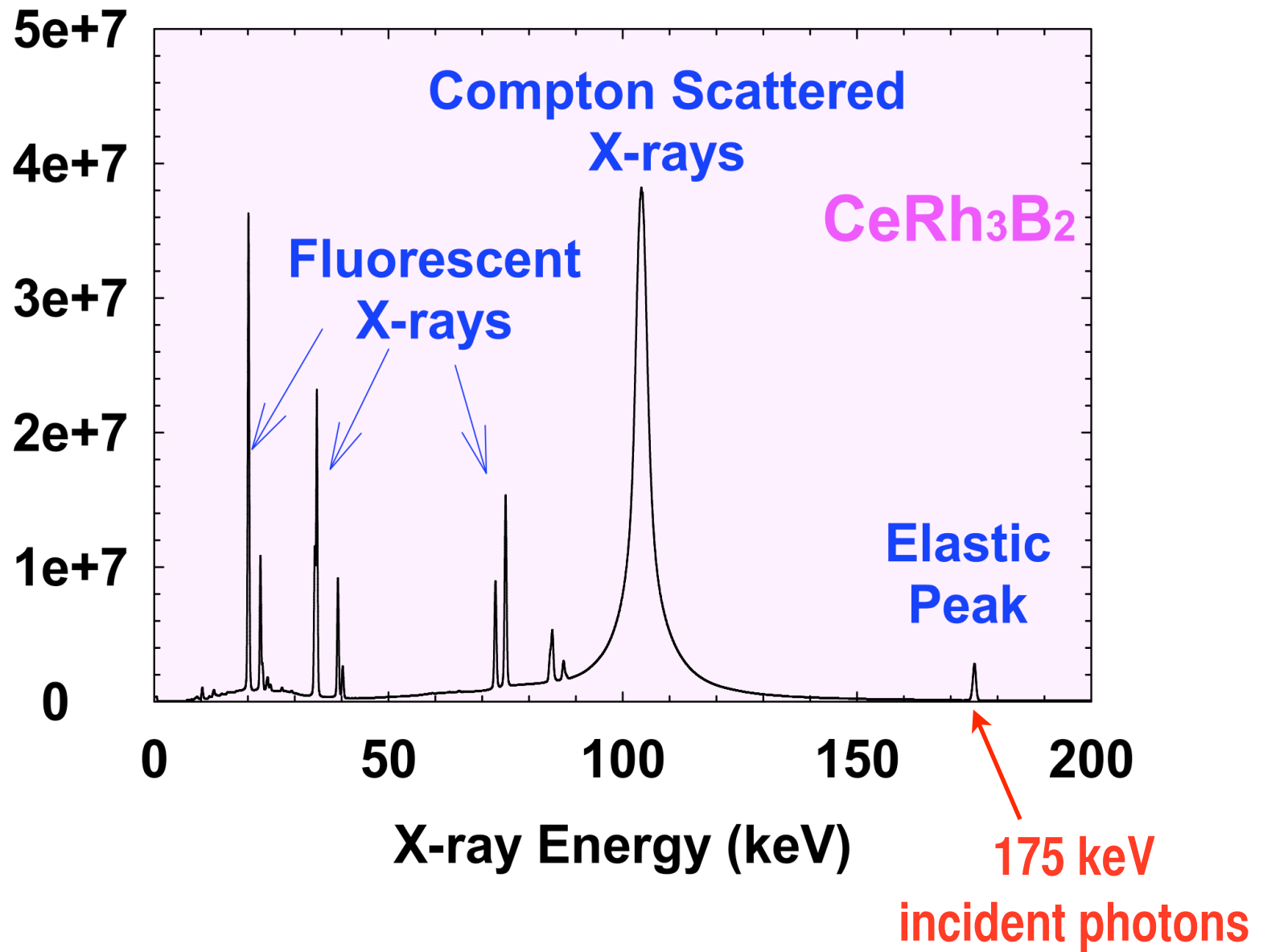
The cause and magnitude of inelastic scattering determines which method to use.

The change in energy could be as little as nano-eV or as high as keV.

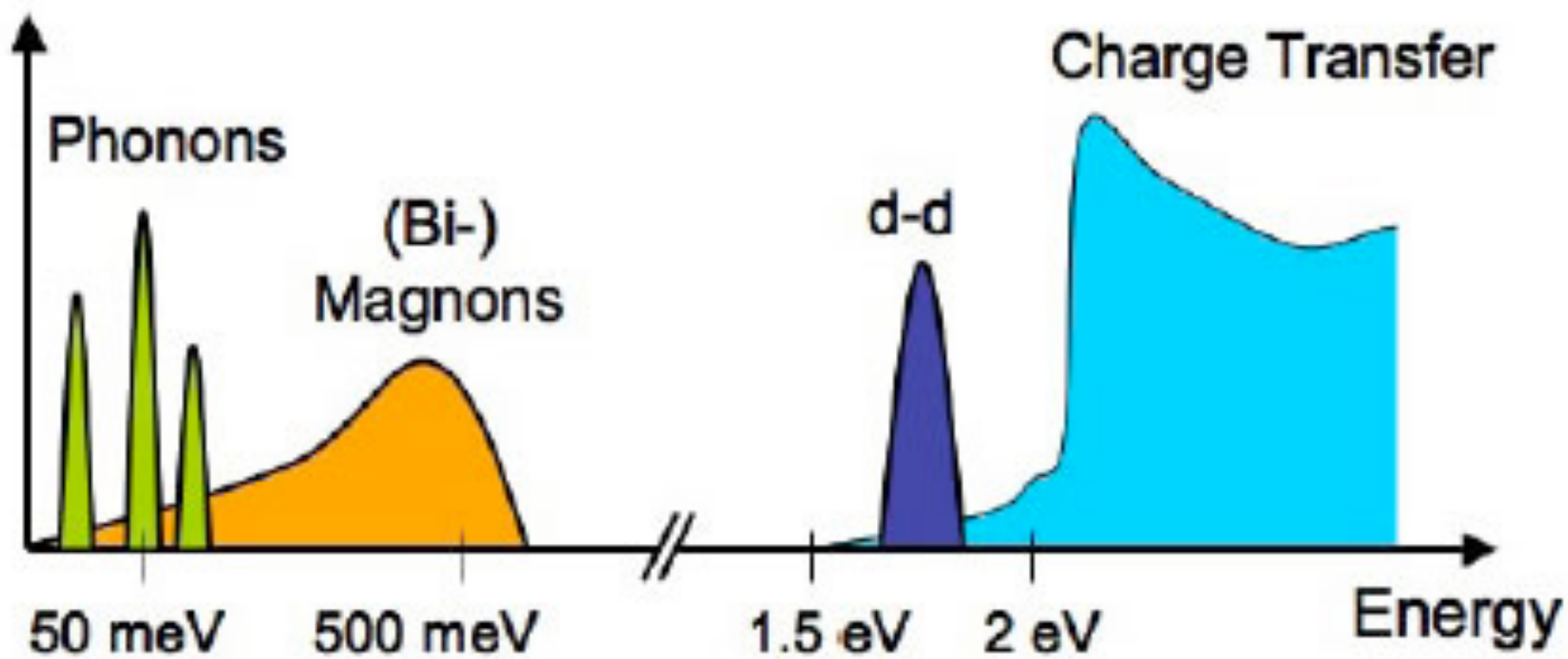
X-rays are quite different than other probes because:

- i) large and small energy transfers are possible
- ii) large momentum transfers at low energy is possible
- iii) avoid multiple scattering by being a gentle probe
- iv) polarization sensitivity
- v) large energy tunability
- vi) small beam size





Incident beam energy



Lattice dynamics for beginners

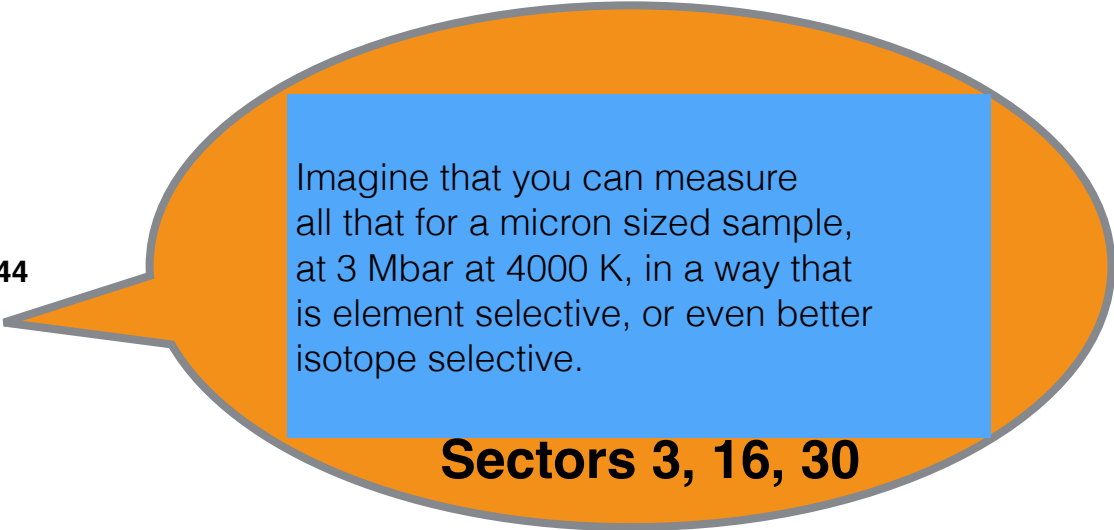
Lattice dynamics describes vibrations of atoms in condensed matter:

- crystalline solids
- glasses, and
- liquids

However, some of the convenience gained by symmetry or periodic lattice is lost for glasses and liquids. Also, effect of surfaces and defects are glowing short-comings of the classical model.

Lattice dynamics is a reflection of forces acting upon atoms and leads to

- sound velocity: V_s, V_p
- vibrational entropy, S_v
- specific heat, C_p
- force constant, $\langle F \rangle$
- compression tensor, C_{11}, C_{12}, C_{44}
- Young's modulus, E
- Shear modulus, G
- stiffness and resilience
- Gruneisen constant, γ
- viscosity, ν



Imagine that you can measure all that for a micron sized sample, at 3 Mbar at 4000 K, in a way that is element selective, or even better isotope selective.

Sectors 3, 16, 30

Many experimental techniques exist to study lattice dynamics

- sound velocity, deformation, thermal expansion, heat capacity....
- spectroscopic methods using light, x-rays and neutrons, and electrons
- point contact spectroscopy

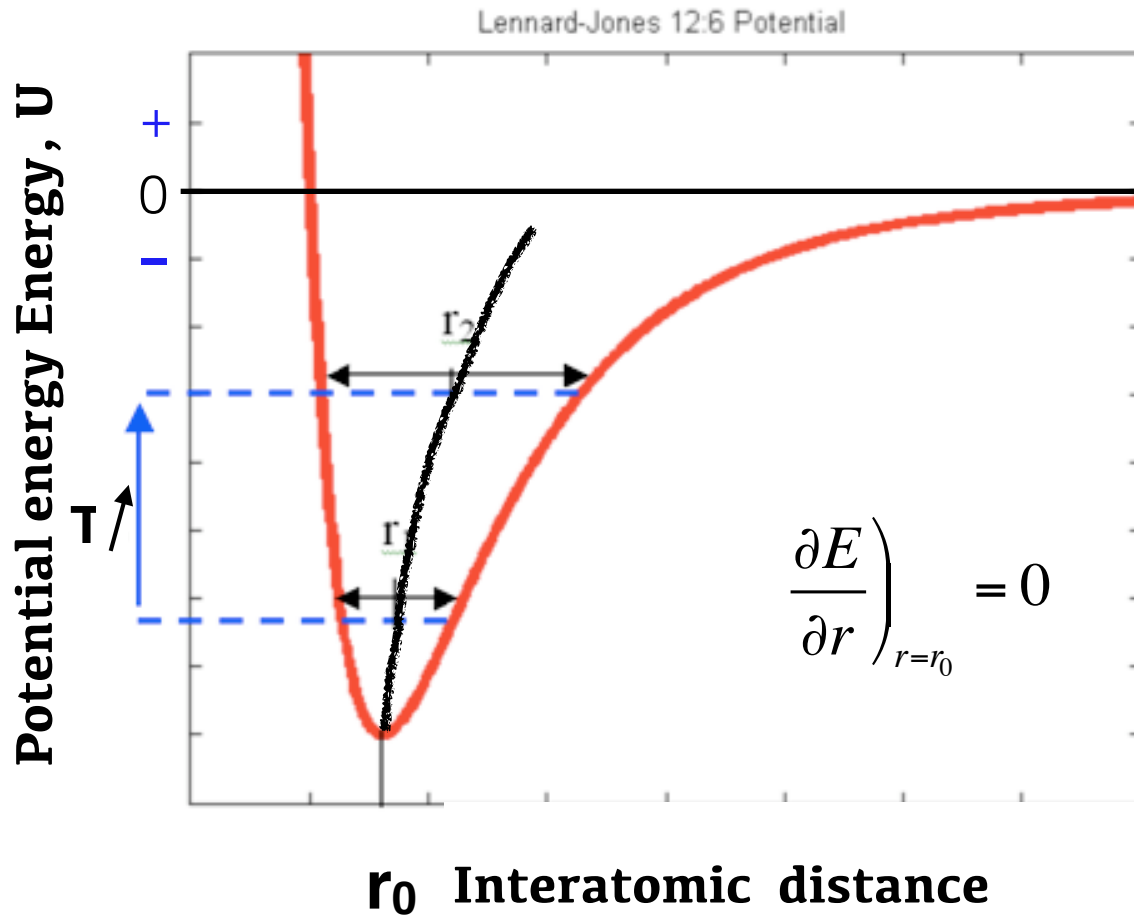
Two main approximations should be noticed:

- **Born-Oppenheimer (adiabatic) approximation**

- Motion of atoms are independent and decoupled from the electrons.
- All electrons follow the nuclei. This can be justified by considering the time scales involved: 10^{-15} s (femto) for electrons, 10^{-12} s (pico) for nuclei

- **Harmonic approximation**

- At equilibrium, attractive and repulsive forces are balanced.
- When atoms move away from the equilibrium positions, they are forced to come back by restoring forces.
- Magnitude of atomic displacements are small compared to interatomic distance.
- All atoms in equivalent positions in every unit cell move together.



There should be no thermal expansion in the harmonic model.

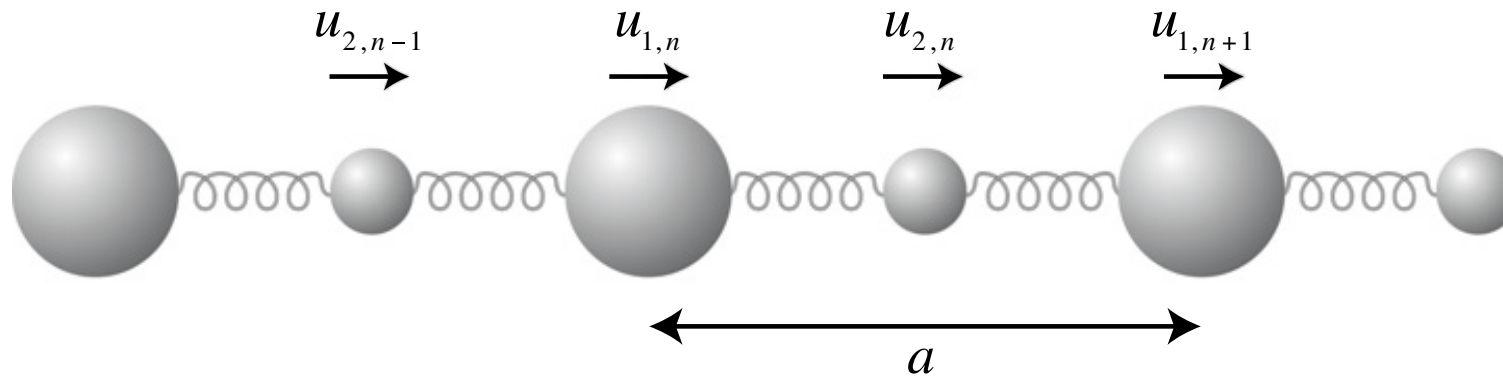
The fact that there is thermal expansion is an indication that the potential under which the atoms move is not harmonic.

However, harmonic model has so many convenient features that we adopt it to explain many features of atomic vibrations.

$$E(r) = E_0 + \frac{1}{2} \left. \frac{\partial^2 E}{\partial r^2} \right|_{r_0} (r - r_0)^2 + \frac{1}{3!} \left. \frac{\partial^3 E}{\partial r^3} \right|_{r_0} (r - r_0)^3 + \frac{1}{4!} \left. \frac{\partial^4 E}{\partial r^4} \right|_{r_0} (r - r_0)^4 + \dots$$

ignoring these terms is the harmonic approximation

Diatomic infinite 1-D chain



$$E = \frac{1}{2} J \sum_n (u_{1,n} - u_{2,n})^2 + \frac{1}{2} J \sum_n (u_{2,n} - u_{1,n+1})^2$$

$$J = \frac{\partial^2 E}{\partial u_{1,n} \partial u_{2,n}}$$

Force constant (spring constant)

$$u_{1,n}(t) = \tilde{u}_1 \exp(i(kna - \omega t))$$

$$u_{2,n}(t) = \tilde{u}_2 \exp(i(kna - \omega t))$$

**Time dependent displacement of two atoms
in terms of relative displacement of each atom**

$$E_{1,n} = \frac{1}{2} J(u_{1,n} - u_{2,n})^2 + \frac{1}{2} J(u_{1,n} - u_{2,n-1})^2$$

$$E_{2,n} = \frac{1}{2} J(u_{2,n} - u_{1,n})^2 + \frac{1}{2} J(u_{2,n} - u_{1,n+1})^2$$

Energy

$$f_{1,n} = -\frac{\partial E_{1,n}}{\partial u_{1,n}} = -J(u_{1,n} - u_{2,n}) - J(u_{1,n} - u_{2,n-1})$$

$$f_{2,n} = -\frac{\partial E_{2,n}}{\partial u_{2,n}} = -J(u_{2,n} - u_{1,n}) - J(u_{2,n} - u_{1,n+1})$$

Force as derivative of energy

$$\ddot{u}_{1,n}(t) = -\omega^2 \tilde{u}_1 \exp i(kna - \omega t) = -\omega^2 u_{1,n}(t)$$

$$\ddot{u}_{2,n}(t) = -\omega^2 \tilde{u}_2 \exp i(kna - \omega t) = -\omega^2 u_{2,n}(t)$$

Acceleration

$$m_1 \ddot{u}_{1,n}(t) = -m_1 \omega^2 u_{1,n}(t) = -J(2u_{1,n}(t) - u_{2,n}(t) - u_{2,n-1}(t))$$

$$m_2 \ddot{u}_{2,n}(t) = -m_2 \omega^2 u_{2,n}(t) = -J(2u_{2,n}(t) - u_{1,n}(t) - u_{1,n+1}(t))$$

Newton's eqⁿ of motion

$$e_1 = m_1^{1/2} \tilde{u}_1; \quad e_2 = m_2^{1/2} \tilde{u}_2$$

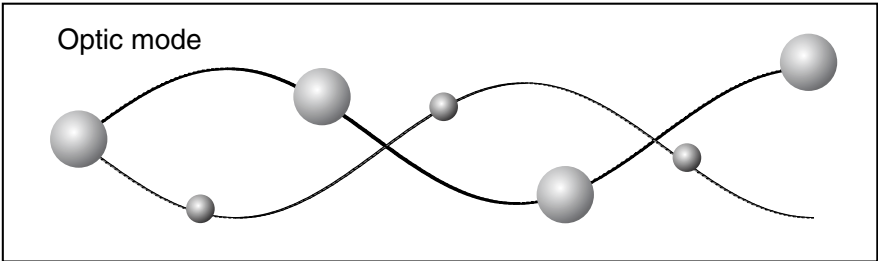
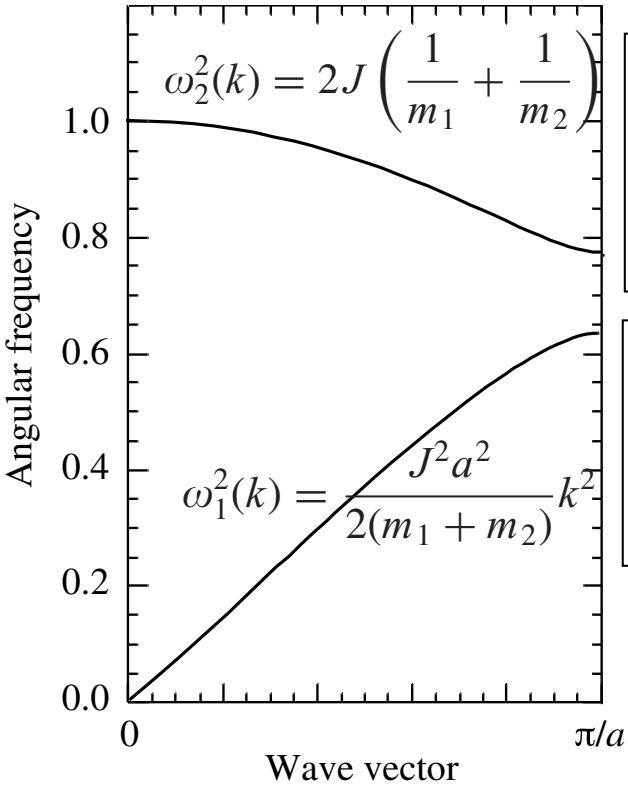
Mass normalized displacements (real)

$$\omega^2 \begin{pmatrix} e_1 \\ e_2 \end{pmatrix} = \mathbf{D}(k) \cdot \begin{pmatrix} e_1 \\ e_2 \end{pmatrix}$$

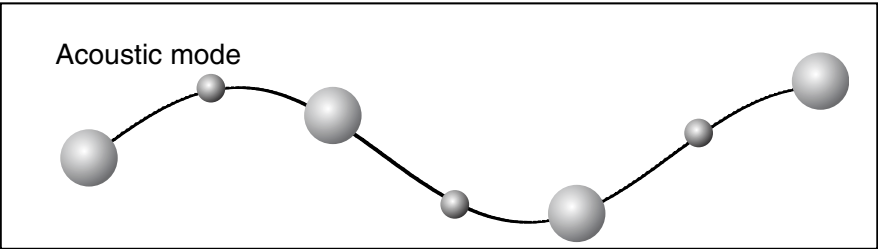
Matrix form of Newton's eqⁿ of motion

$$\mathbf{D}(k) = \begin{pmatrix} 2J/m_1 & -J(1 + \exp(-ika)) / \sqrt{m_1 m_2} \\ -J(1 + \exp(+ika)) / \sqrt{m_1 m_2} & 2J/m_2 \end{pmatrix}$$

Eigen solutions

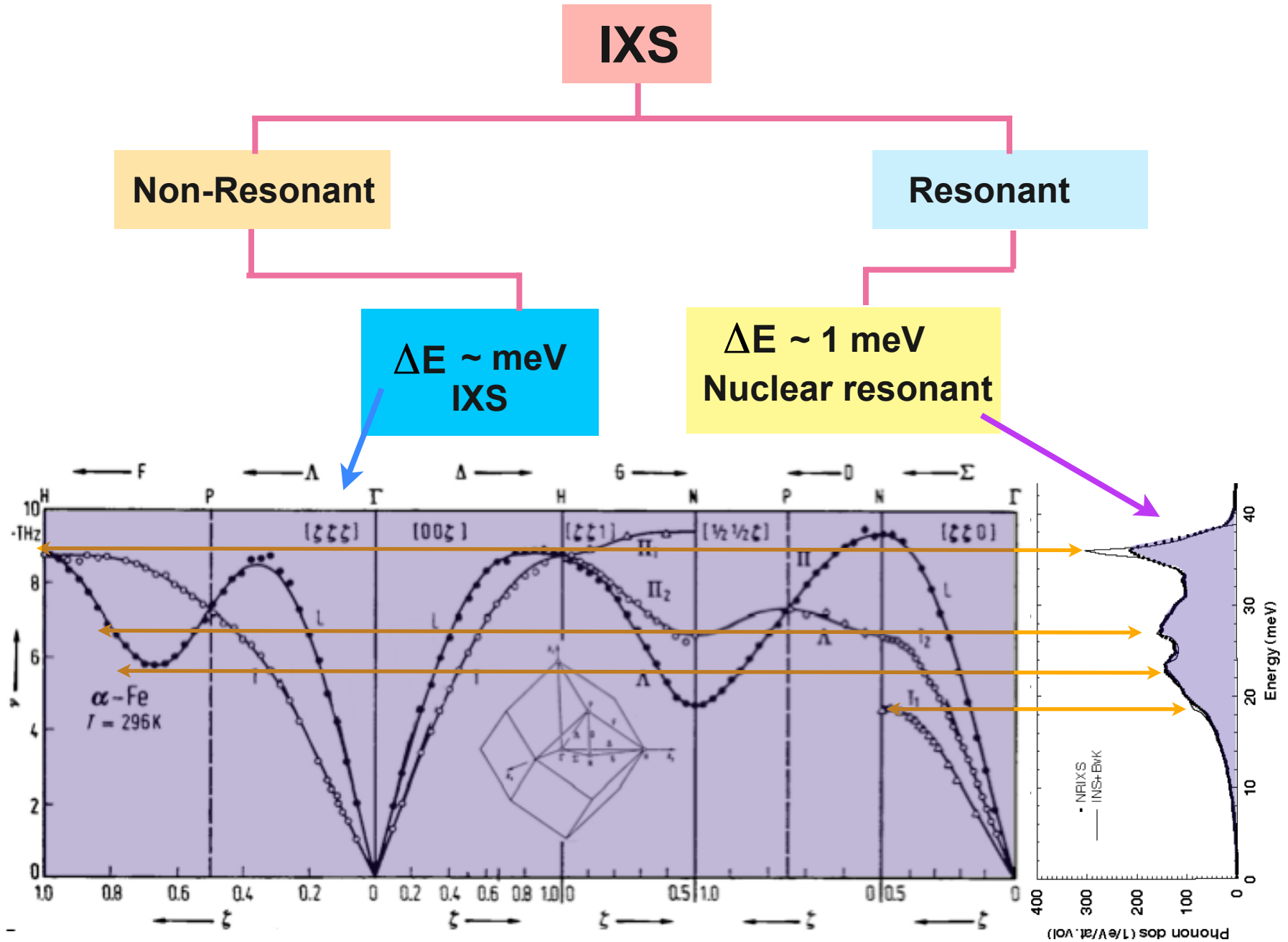


out-of-phase
 $m_1^{1/2} e_1 = -m_2^{1/2} e_2$

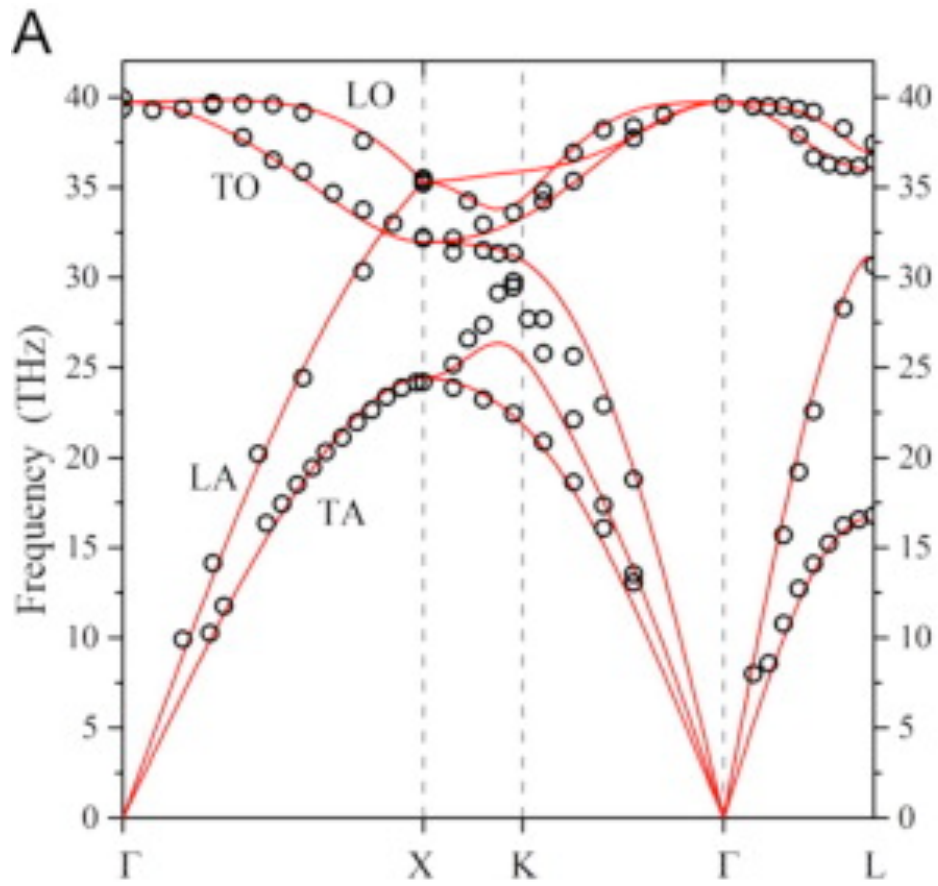


in-phase
 $m_1^{-1/2} e_1 = m_2^{-1/2} e_2$

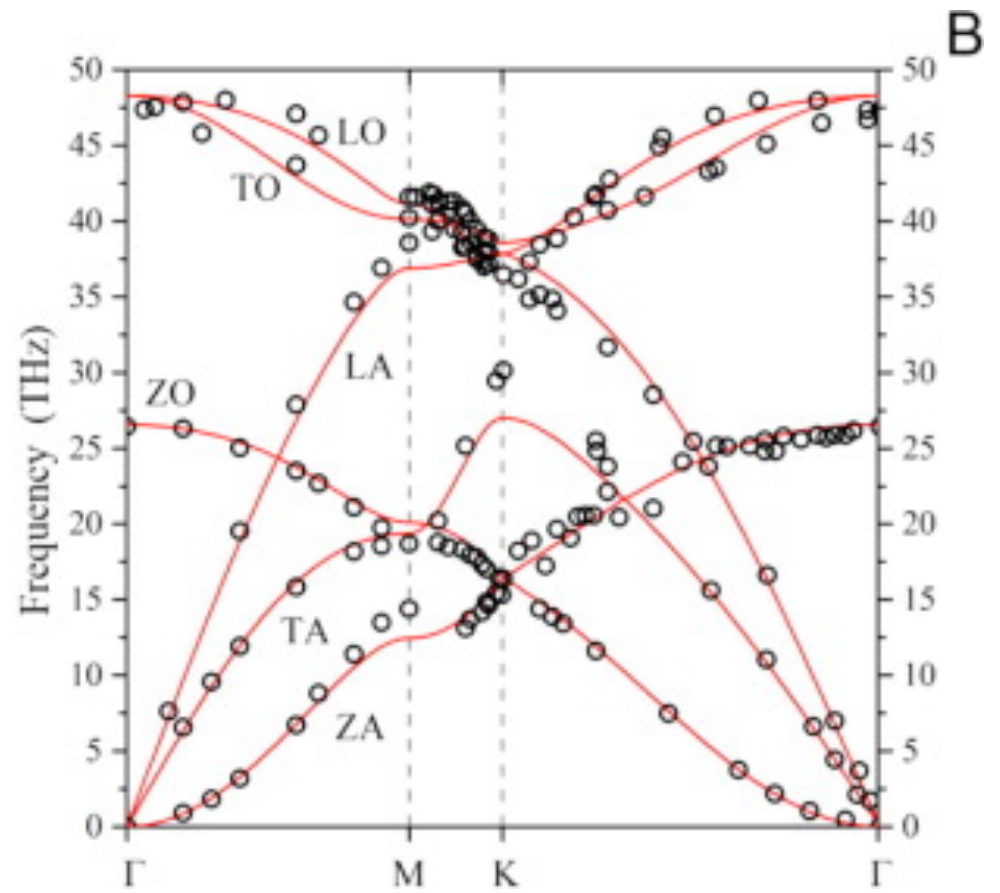
Inelastic X-Ray Scattering: A plethora of different techniques



Diamond

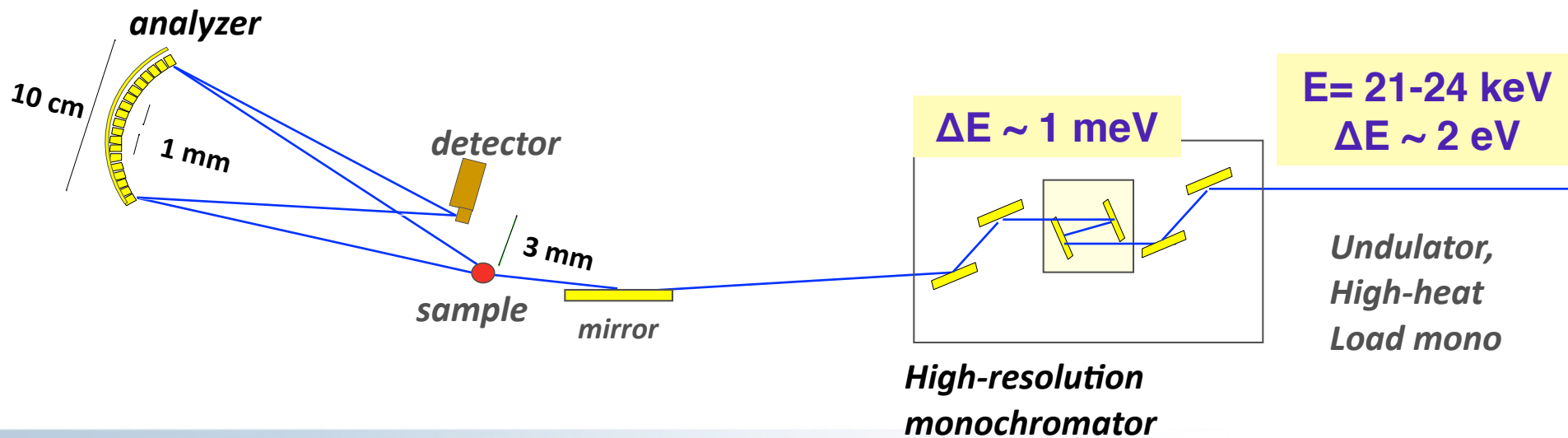
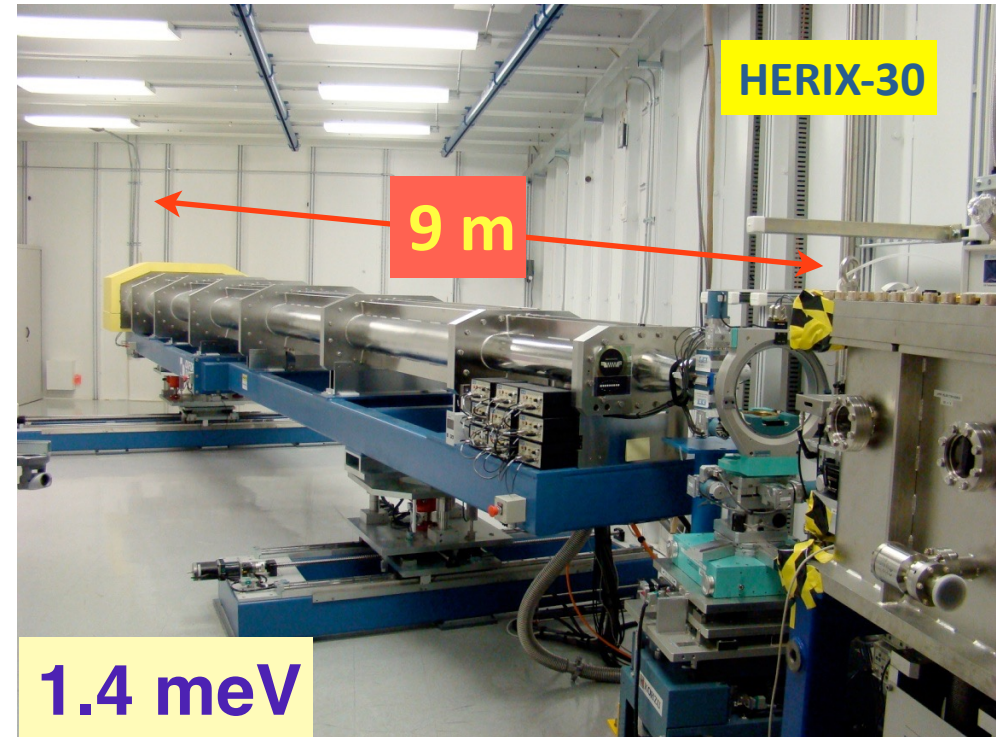
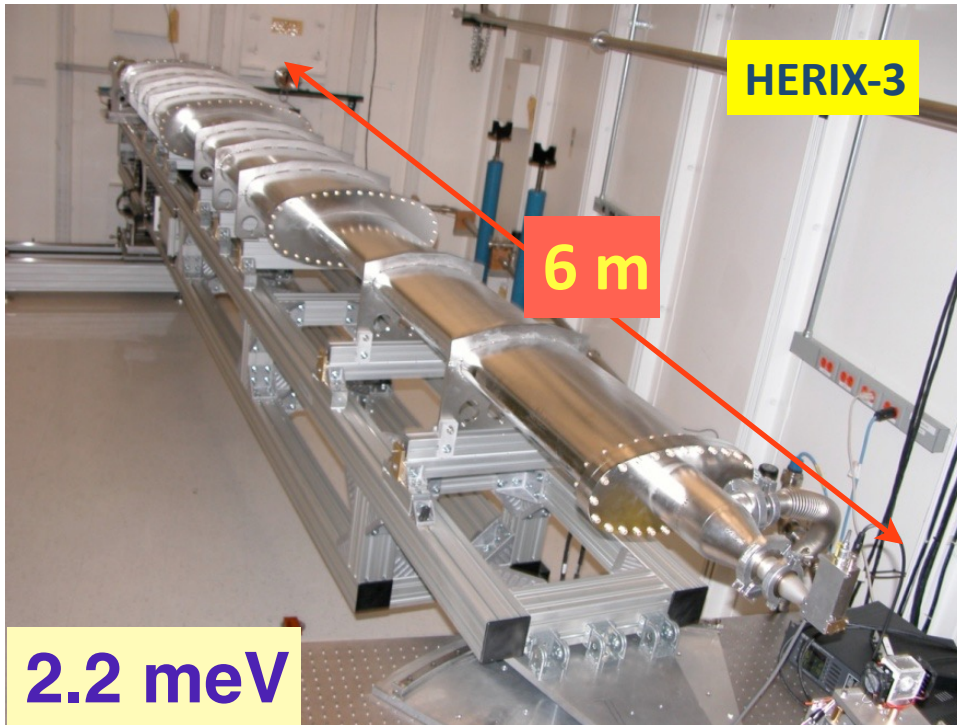


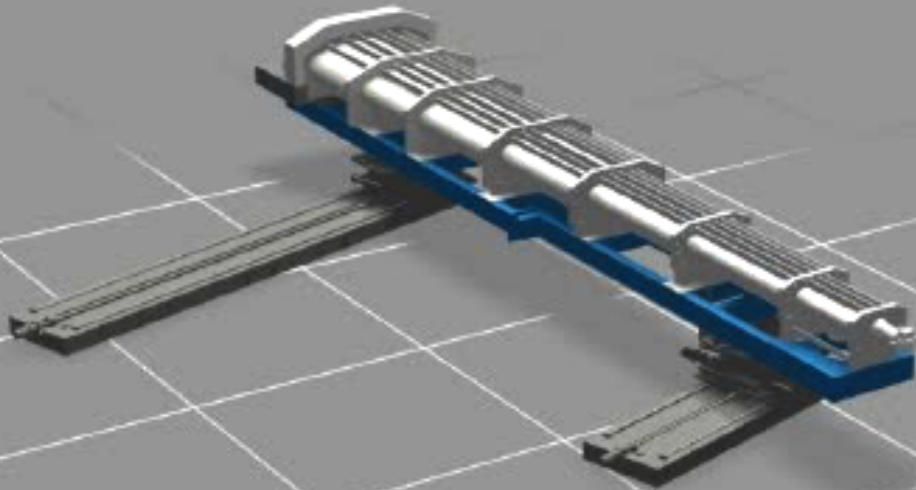
Graphene

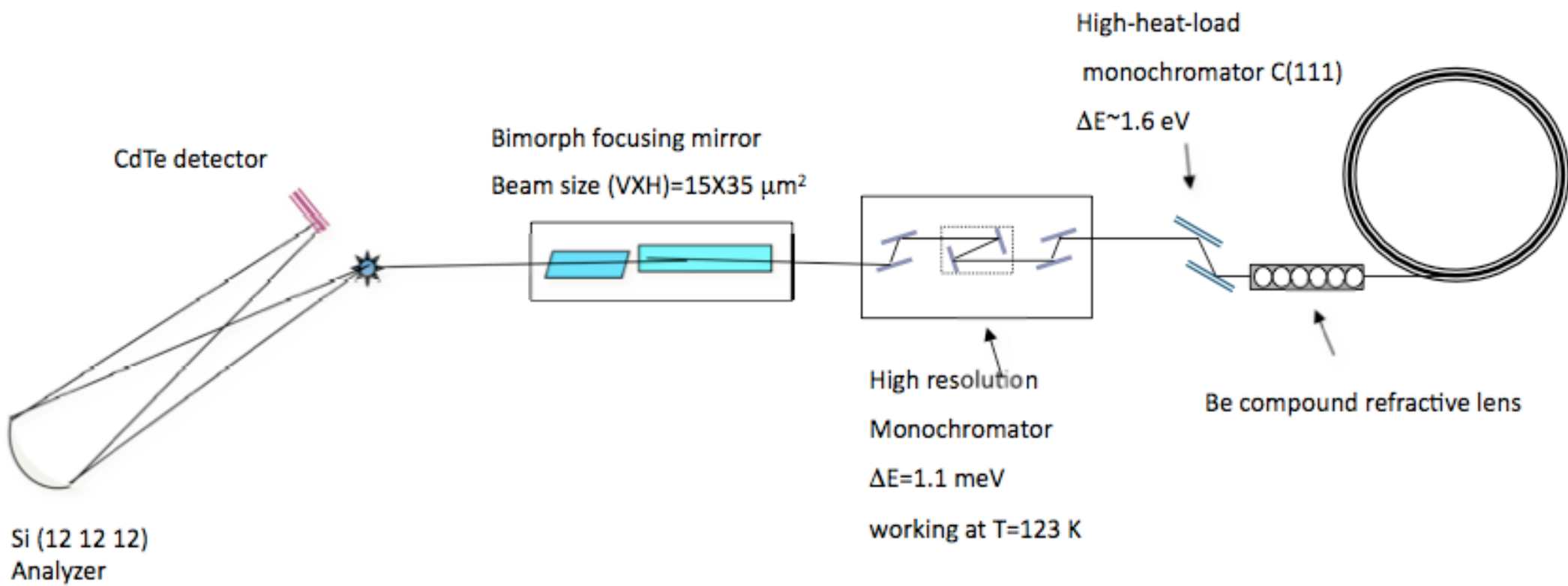


Umberto Monteverde, et al, 2015

HERIX-3 and HERIX-30



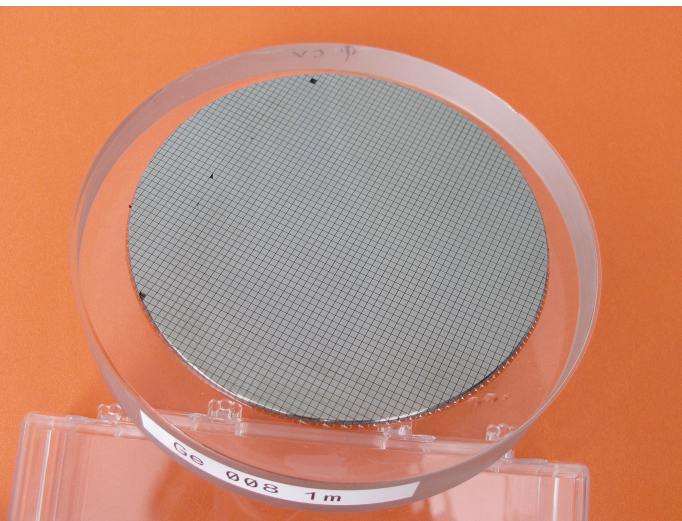




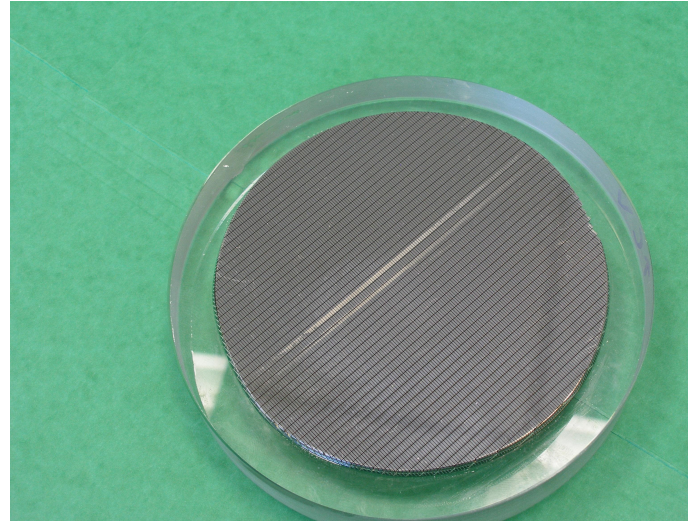
Choice of energy

Si Reflection at 90 °	Energy (keV)	Resolution (meV)	Reflectivity (%)
18 6 0	21.657	1.23	78
11 11 11	21.747	0.83	70
13 11 9	21.985	0.81	69
15 11 7	22.685	0.70	68
20 4 0	23.280	0.87	76
12 12 12	23.724	0.80	75
14 14 8	24.374	0.69	74
22 2 0	25.215	0.576	71
13 13 13	25.701	0.37	60

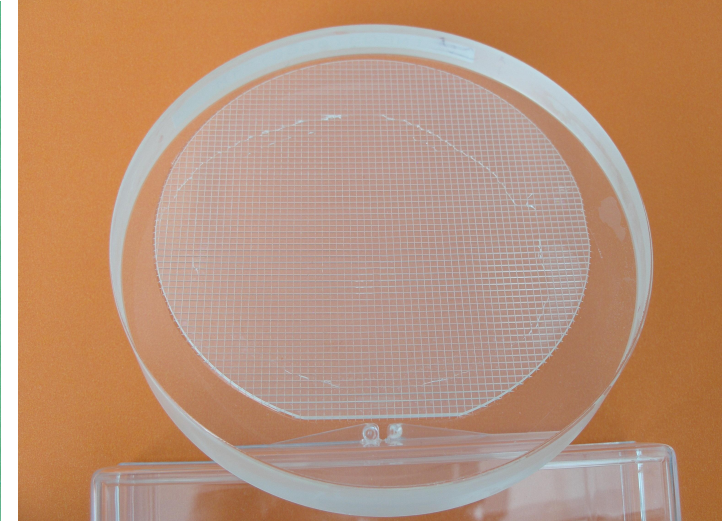
Bent-diced IXS analyzers



Si



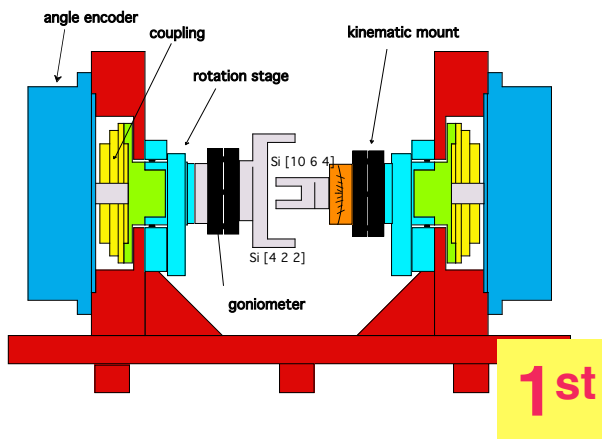
Ge



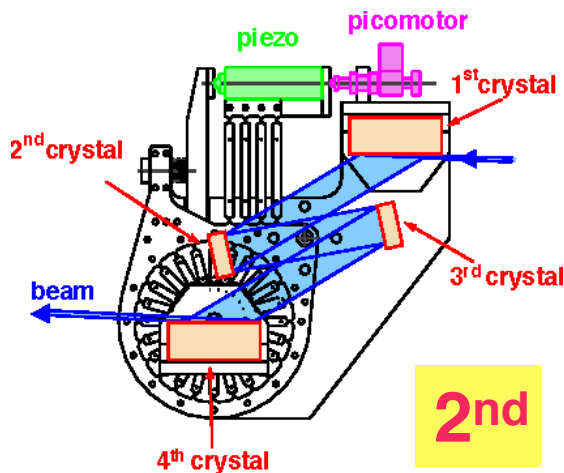
LiNbO₃

Generations of high-resolution monochromators

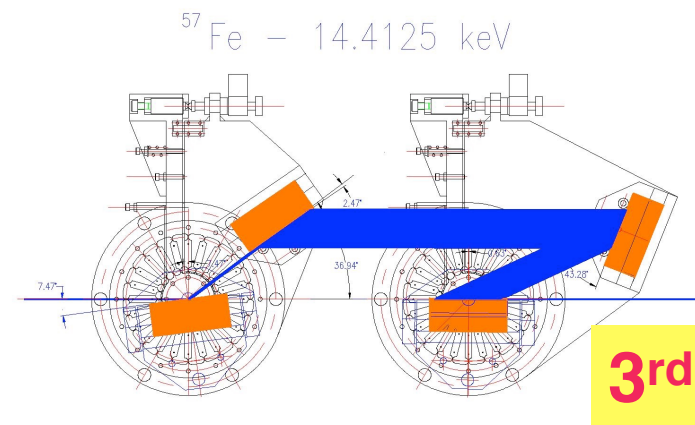
1992



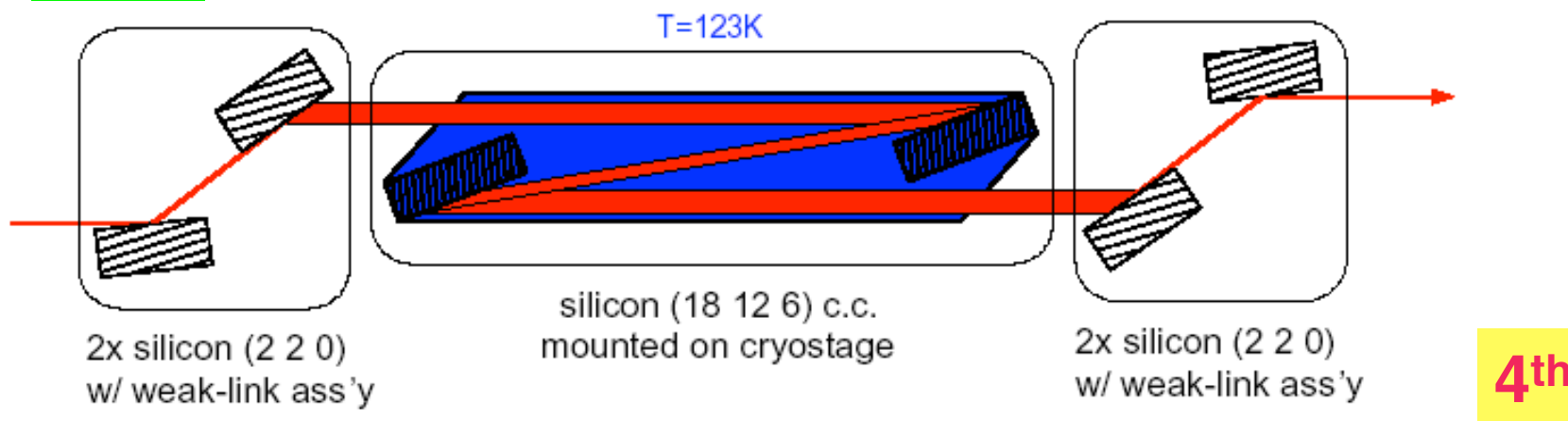
1999



2002



2004



What is being measured ?

$$\frac{d^2\sigma}{d\Omega d\omega} = r_0^2 \frac{\omega_f}{\omega_i} |\mathbf{e}_i \cdot \mathbf{e}_f| N \sum_{i,f} \left| \langle i | \sum e^{i\mathbf{Q}\cdot\mathbf{r}_j} | f \rangle \right|^2 \delta(E_f - E_i - \hbar\omega)$$

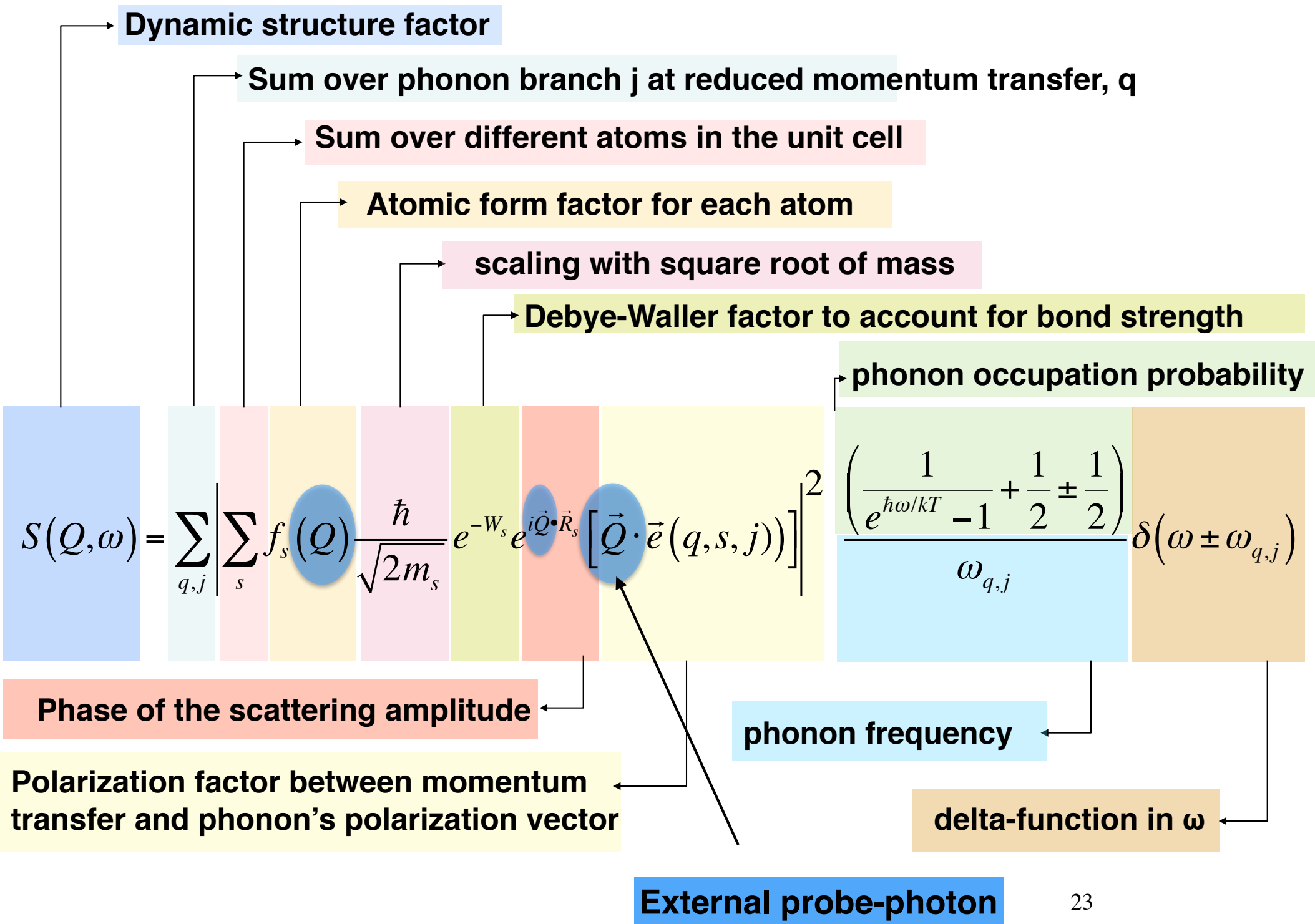
Thomson cross section

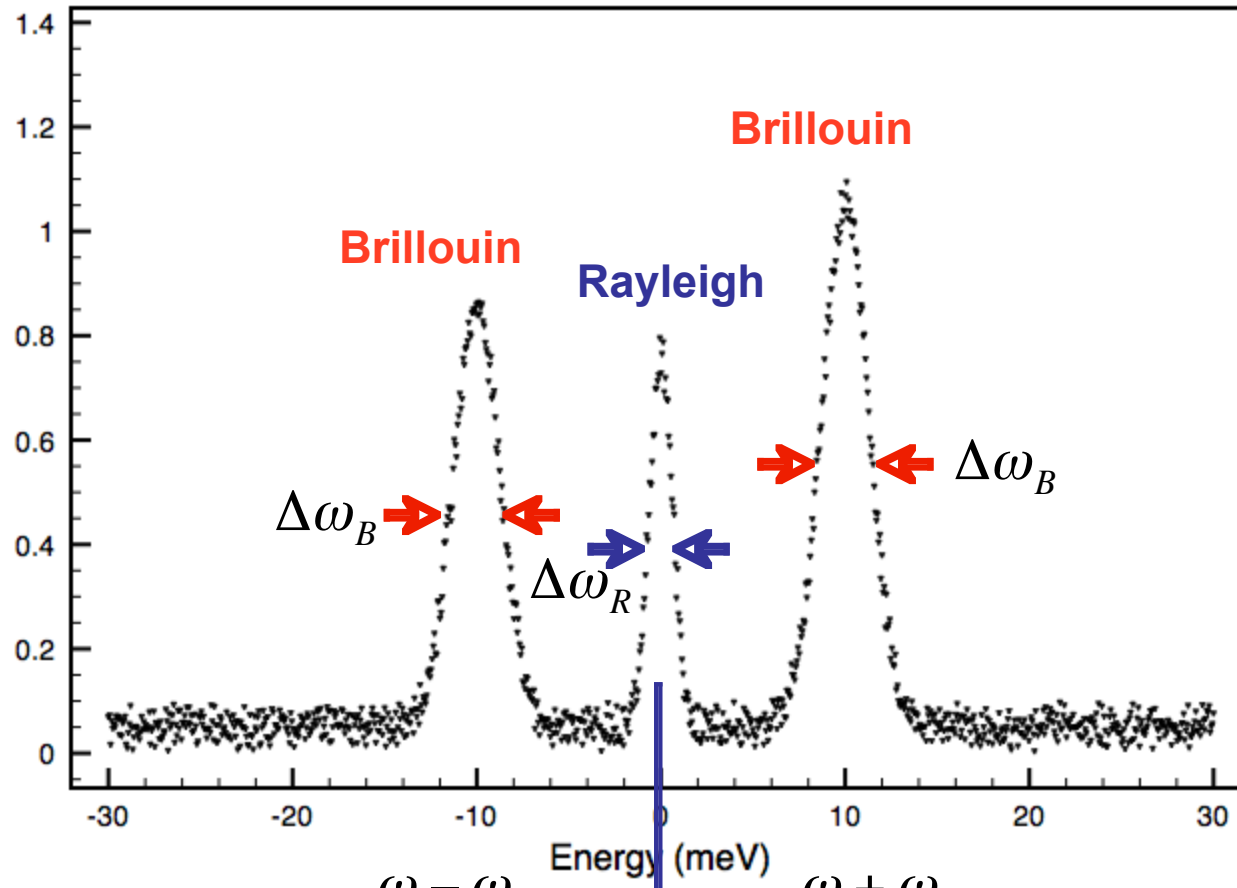
Dynamical structure factor $S(\mathbf{Q},\omega)$

$$S(\mathbf{Q},\omega) = \frac{1}{2\pi} \int dt e^{-i\omega t} \langle \phi_i | \sum_{ll'} f_l(\mathbf{Q}) e^{-i\mathbf{Q}\cdot\mathbf{r}_l(t)} f_{l'}(\mathbf{Q}) e^{i\mathbf{Q}\cdot\mathbf{r}_{l'}(0)} | \phi_i \rangle$$

Density-density correlations

$$f(\mathbf{Q}) = f_{ion}(\mathbf{Q}) + f_{valence}(\mathbf{Q}) \quad \text{Atomic form factor}$$





Entropy fluctuations,

Concentration fluctuations

$$\Delta\omega_R \sim \alpha q^2$$

$$\Delta\omega_R \sim Dq^2$$

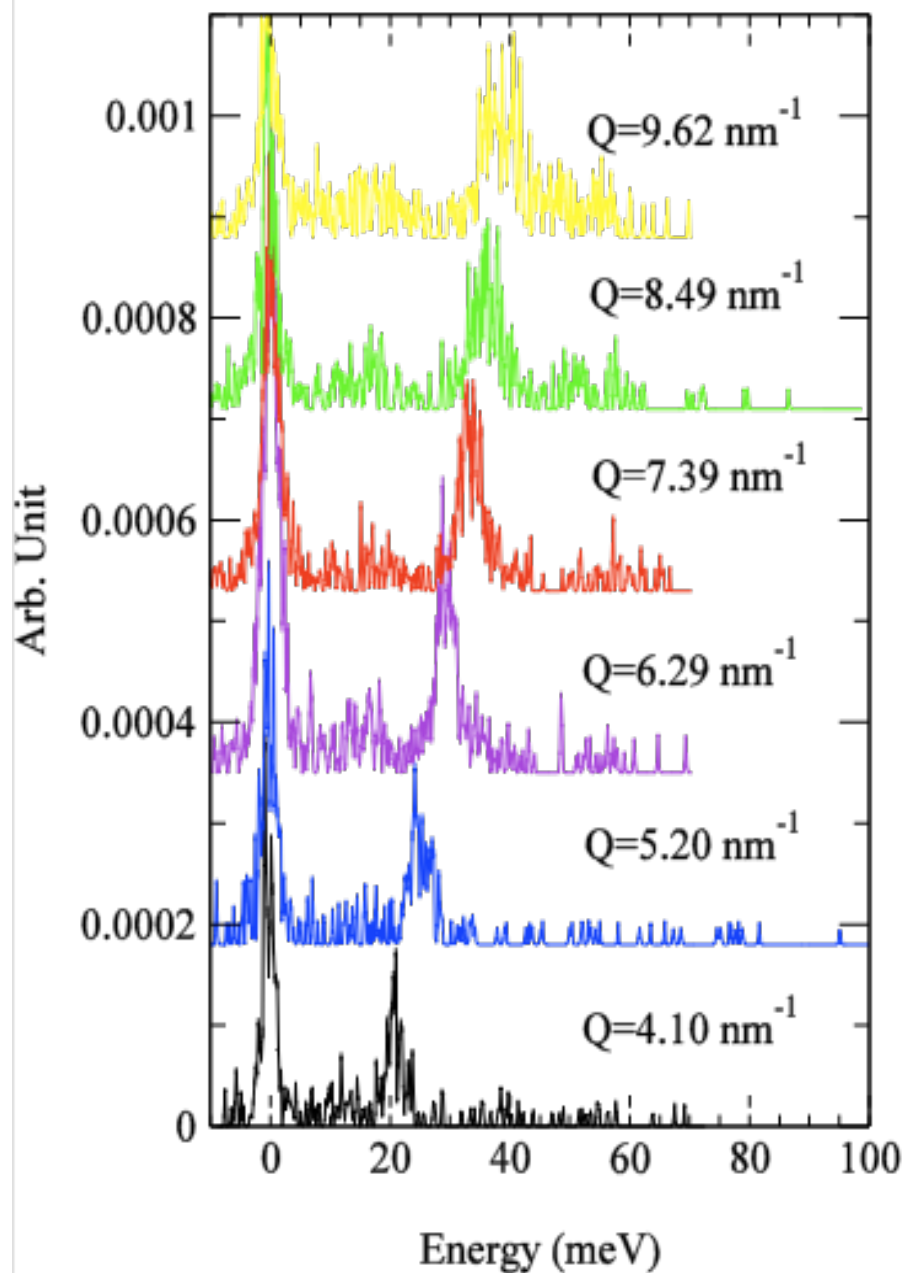
Pressure fluctuations

$$\omega_B(q) = V \cdot q$$

$$\Delta\omega_B \sim Vq^2$$

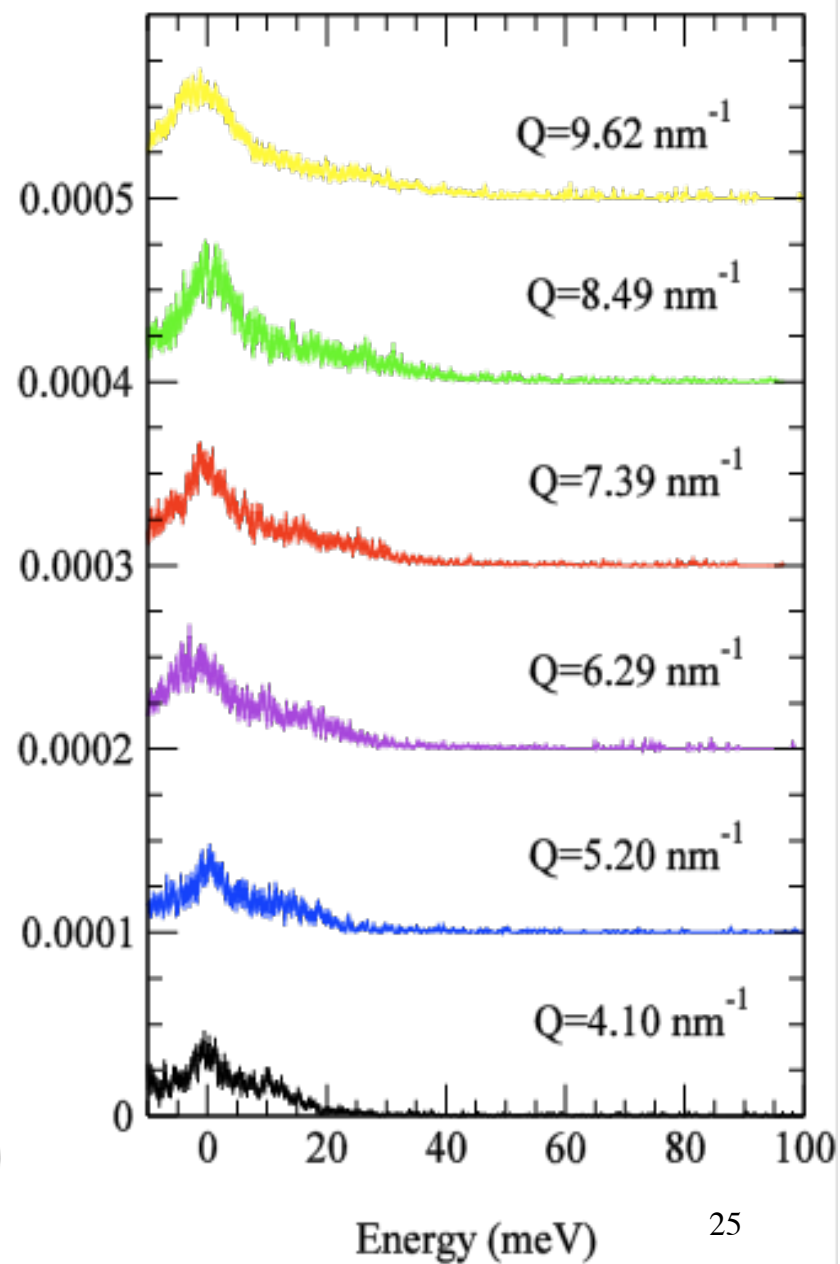
Hot Solid Silicon

T=1300 C°



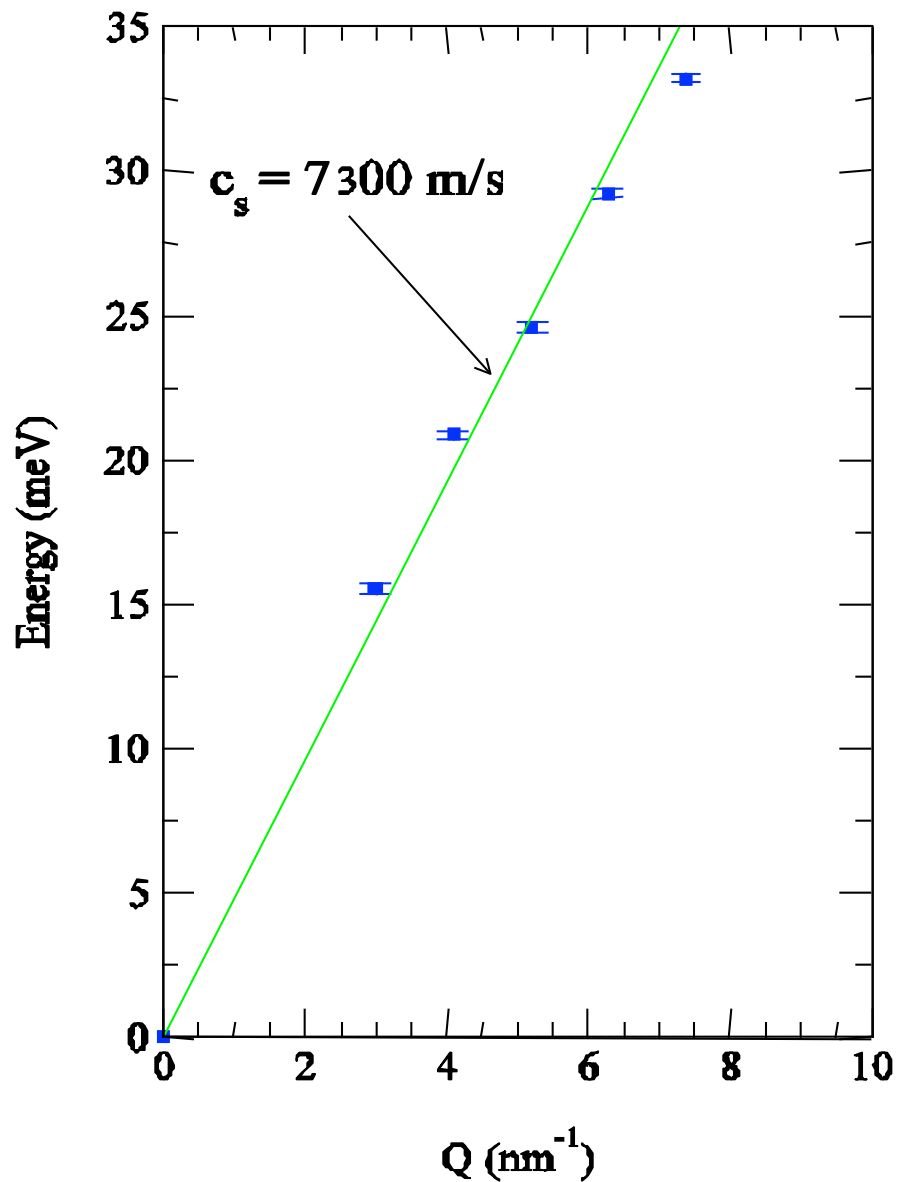
Supercooled Silicon

T=1300 C°



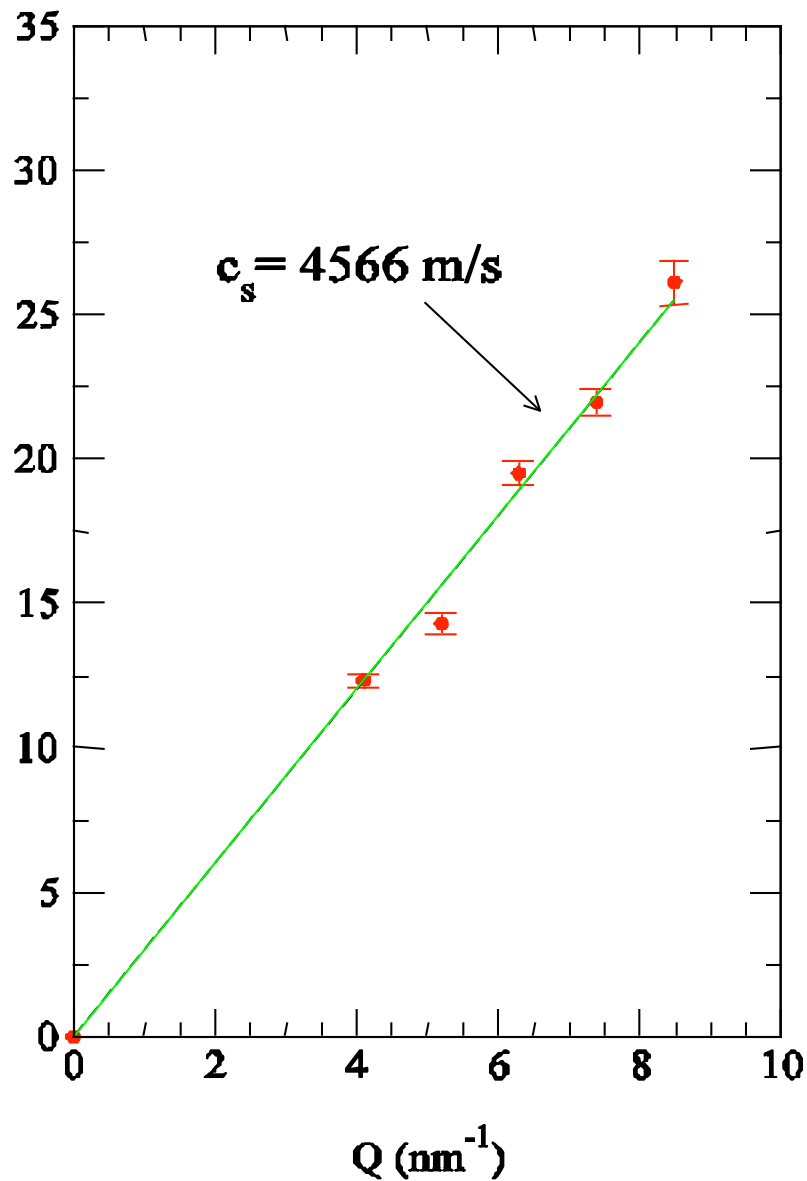
Hot Solid Si

$T=1300\text{ C}^\circ$



Supercooled Si

$T=1300\text{ C}^\circ$



PHONON's: $\phi\omega\nu\acute{\eta}$ (phonē), *sound*

- Phonons are periodic oscillations in condensed systems.
- They are inherently involved in thermal and electrical conductivity.
- They can show anomalous (non-linear) behavior near a phase transition.
- They can carry sound (acoustic modes) or couple to electromagnetic radiation or neutrons (acoustical and optical).
- Have energy of $\hbar\omega$ as quanta of excitation of the lattice vibration mode of angular frequency ω . Since momentum, $\hbar k$, is exact, they are delocalized, collective excitations.
- Phonons are bosons, and they are not conserved. They can be created or annihilated during interactions with neutrons or photons.
- They can be detected by Brillouin scattering (acoustic), Raman scattering, FTIR (optical).
- Their dispersion throughout the BZ can ONLY be monitored with x-rays (IXS), or neutrons (INS).
- Accurate prediction of phonon dispersion require correct knowledge about the force constants:
COMPUTATIONAL TECHNIQUES ARE ESSENTIAL.

$$\omega^2 \mathbf{e} = \mathbf{D}(\mathbf{k}) \cdot \mathbf{e} \quad \Rightarrow \quad \omega^2 = \mathbf{e}^T \cdot \mathbf{D}(\mathbf{k}) \cdot \mathbf{e}$$

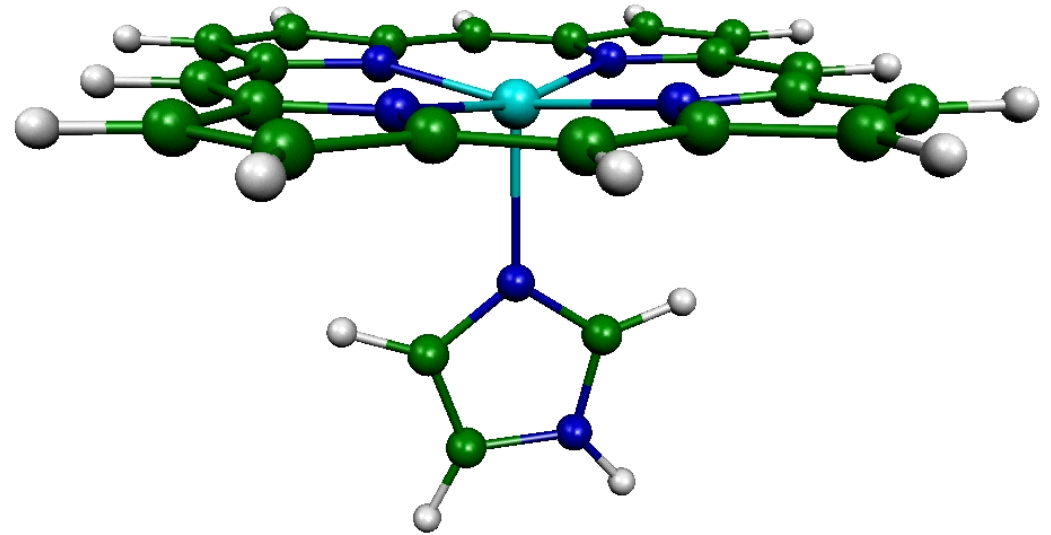
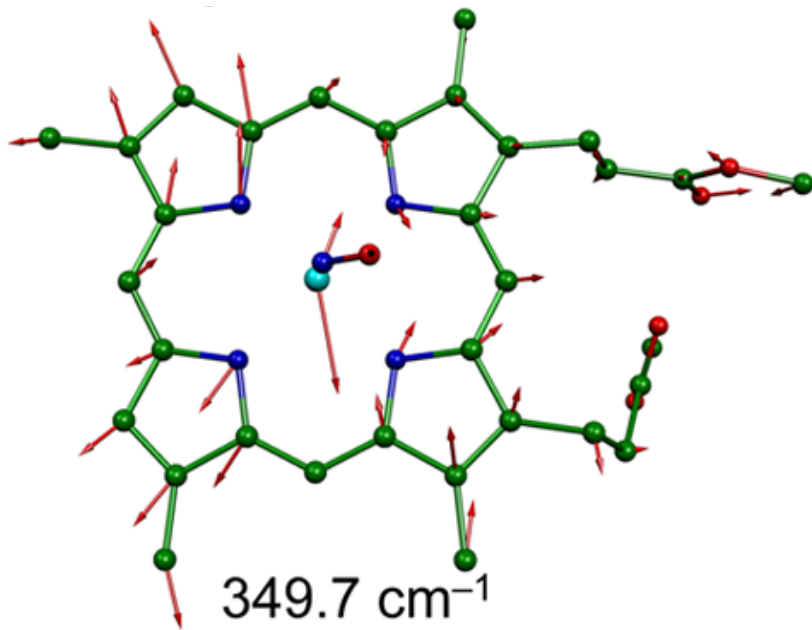
Eigenvalue eqⁿ.

$$D_{j,j'}(\mathbf{k}) = \frac{1}{\sqrt{m_j m_{j'}}} \sum_{n'} \Phi_{0,n'}^{j,j'} \exp(i\mathbf{k} \cdot (\mathbf{r}_{j,0} - \mathbf{r}_{j',n'}))$$

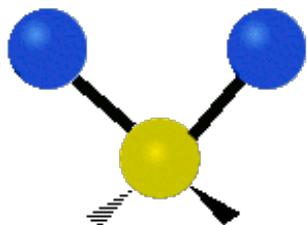
Dynamical matrix

$$\mathbf{e}_\lambda^T \cdot \mathbf{e}_\lambda = 1; \quad \mathbf{e}_{\lambda'}^T \cdot \mathbf{e}_\lambda = \delta_{\lambda',\lambda}$$

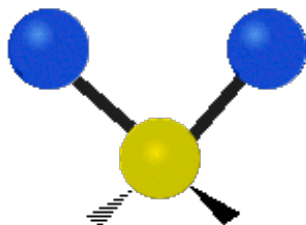
Eigenvalues are orthonormal..



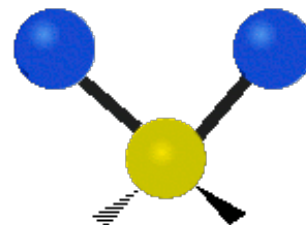
symmetrical
stretching



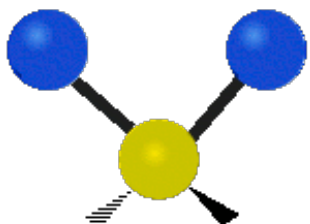
asymmetrical
stretching



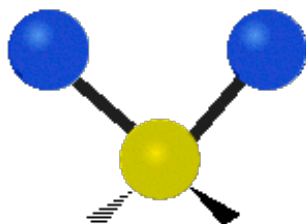
scissoring



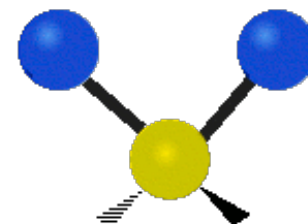
rocking

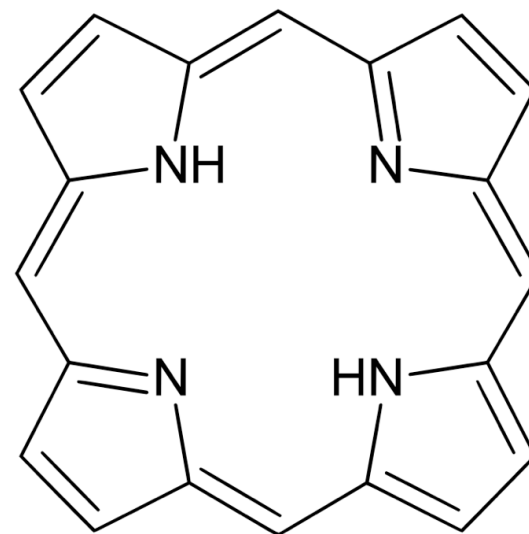
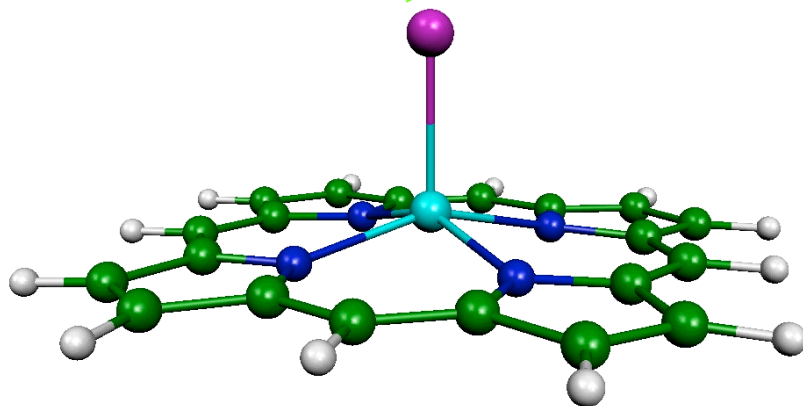
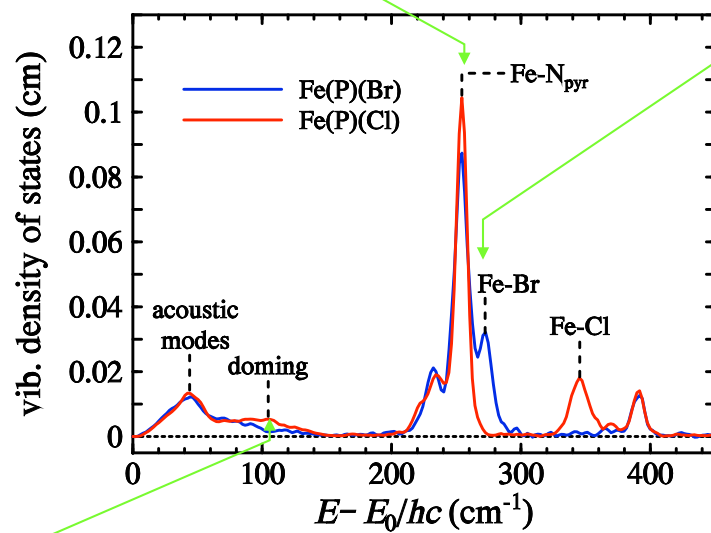
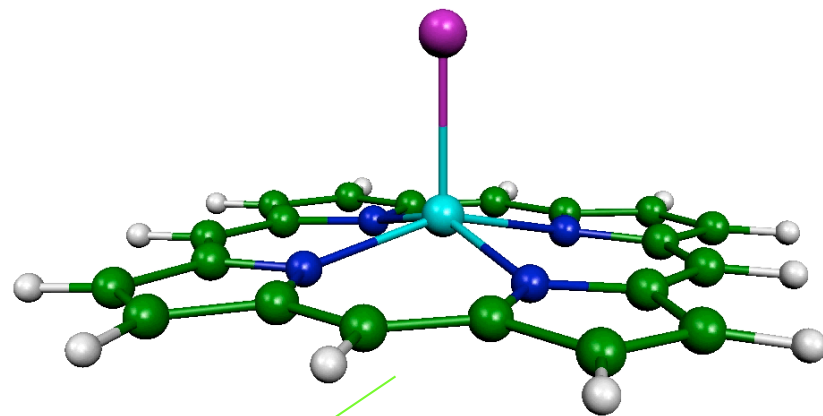
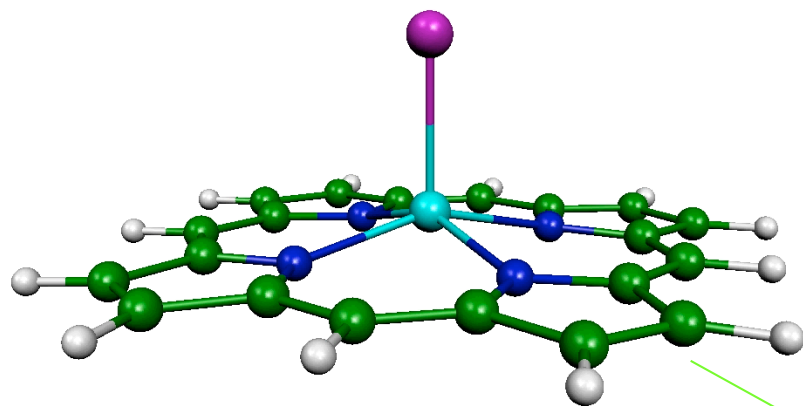


wagging



twisting





PHONONS (cont'd)

$$E_n = \left(n + \frac{1}{2} \right) \hbar \omega$$

Energy of a single oscillation as a function of number of phonons. The second term +1/2 is the “zero-point” energy.

$$E = \sum_{\mathbf{k}, \lambda} \omega_{\mathbf{k}, \lambda}^2 |Q(\mathbf{k}, \lambda)|^2 = \sum_{\mathbf{k}, \lambda} \left(n_{\mathbf{k}, \lambda} + \frac{1}{2} \right) \hbar \omega_{\mathbf{k}, \lambda}$$

Total energy, in terms of normal mode coordinates

$$\langle n(\omega_{\mathbf{k}, \lambda}) \rangle = \frac{1}{\exp(\hbar \omega_{\mathbf{k}, \lambda} / k_B T) - 1}$$

Bose-Einstein statistics for average number of modes at a given temperature

$$\mathcal{H} = \frac{1}{2} \sum_{j, \ell} m_j |\dot{\mathbf{u}}_{j\ell}|^2 + \frac{1}{2} \sum_{\substack{j, j' \\ \ell, \ell'}} \mathbf{u}_{j\ell}^T \cdot \Phi_{\ell, \ell'}^{j, j'} \cdot \mathbf{u}_{j'\ell'}$$

Hamiltonian of the system:

$\mathcal{H} = \text{Kin. En.} + \text{Pot. En}$

Phonon density of states

Many thermodynamic functions like free energy, specific heat, and entropy are additive functions of phonon density of states.

This stems from the notion that the normal modes do not interact in the harmonic approximation.

Phonon density of states is the number of modes in a unit energy interval.

$$c_v(T) = 3Nk \int \frac{\hbar^2 \omega^2 e^{\hbar\omega/kT}}{(kT)^2 (1 - e^{\hbar\omega/kT})^2} \cdot g(\omega) \cdot d\omega$$

Vibrational specific heat

Phonon density of states is a key ingredient for many thermodynamic properties

If we choose to write in terms of energy, $E = \hbar\omega$, $\beta = 1/k_B T$

$$c_v(T) = 3k_B \int (\beta E / 2)^2 \operatorname{csc} h(\beta E) \cdot g(E) \cdot dE$$

Vibrational specific heat

$$S_v(T) = 3k_B \int_0^{\infty} \left\{ \beta E / 2 \cdot \cot h(\beta E) - \ln [2 \sin h(\beta E)] \right\} \cdot g(E) \cdot dE$$

Vibrational entropy

$$f_{LM} = e^{-E_R} \int \left\{ g(E) / 2 \right\} \cdot \operatorname{coth}(\beta E / 2) dE$$

Lamb-Mössbauer factor

$$g(E) = \frac{3m}{2\pi^2 \hbar^3 \rho v_D^3} E^2$$

Debye Sound velocity

$$\langle F \rangle = \frac{M}{\hbar^2} \int_0^{\infty} E^2 g(E) dE$$

Average restoring force constant

And, some thermodynamics

$$\mathcal{Z} = \frac{1}{1 - \exp(-\beta\hbar\omega)}$$

Partition function

$$F = -k_B T \ln \mathcal{Z}$$

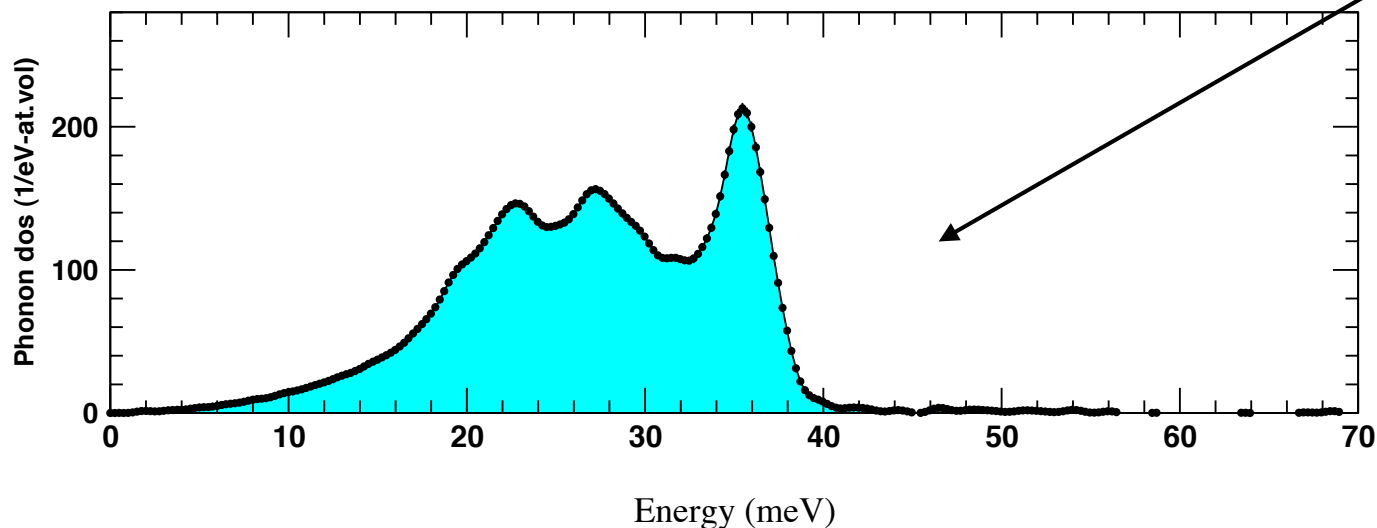
Free energy

$$C = -T \frac{\partial^2 F}{\partial T^2}$$

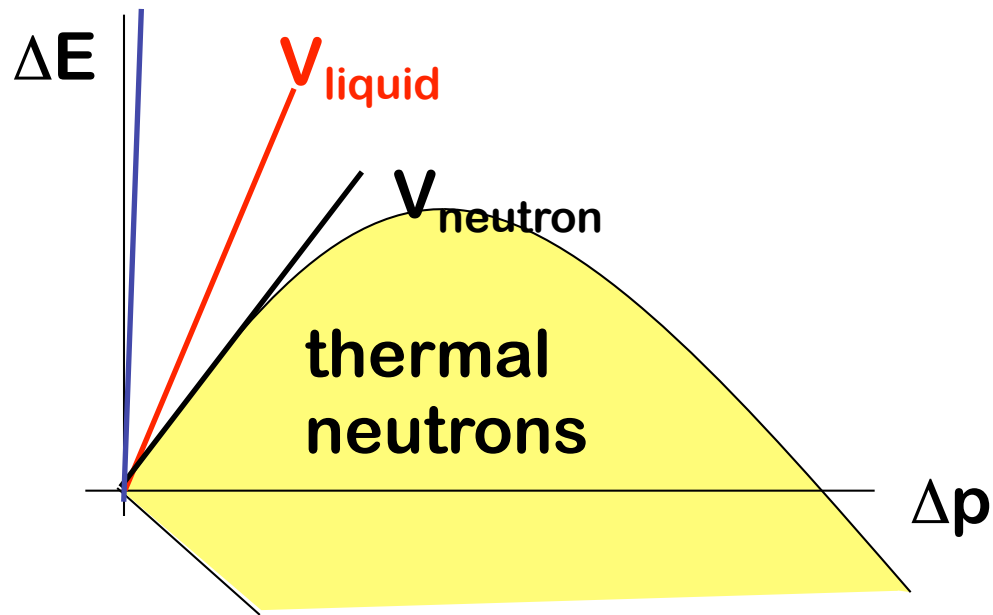
Heat capacity

$$E = \sum_{\mathbf{k}, \lambda} \left(\langle n(\omega_{\mathbf{k}, \lambda}) \rangle + \frac{1}{2} \right) \hbar \omega_{\mathbf{k}, \lambda} \equiv \int \left(\langle n(\omega) \rangle + \frac{1}{2} \right) \hbar \omega g(\omega) d\omega.$$

Energy in terms of
phonon density of states

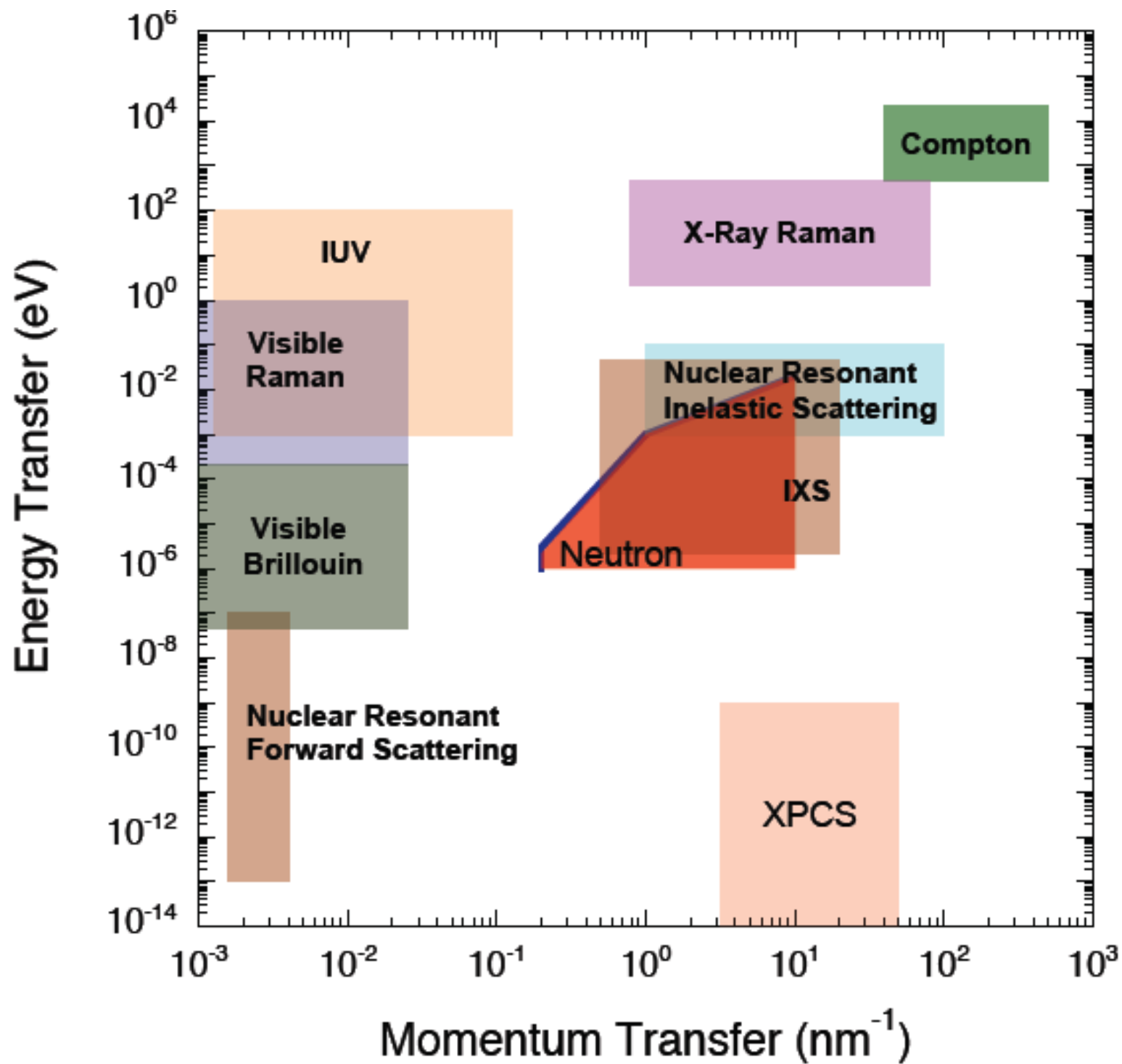


Why x-rays instead of neutrons or visible light ?



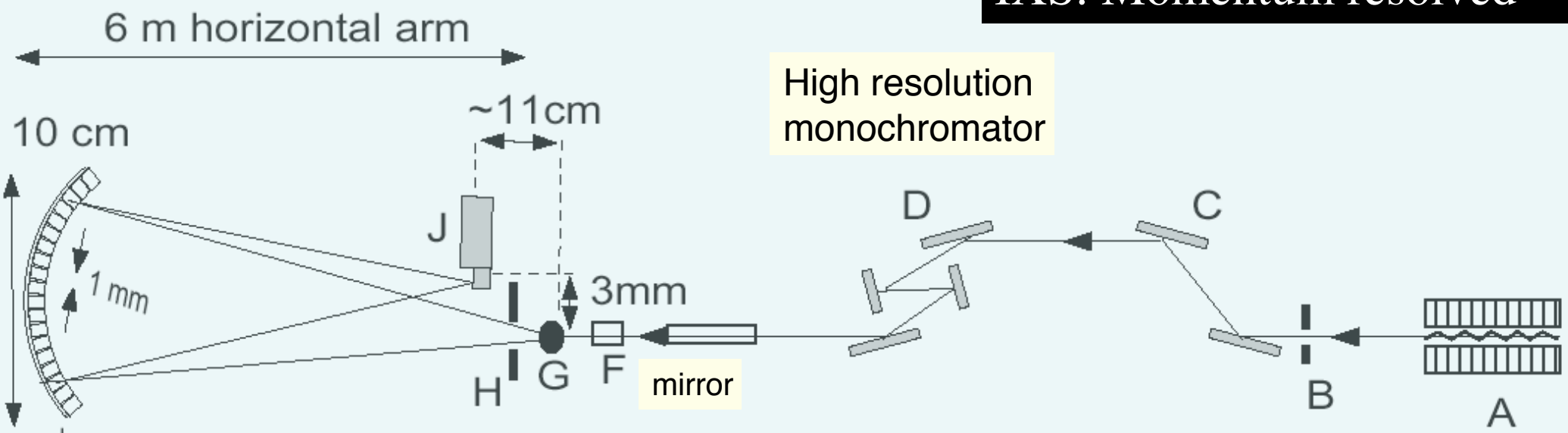
Limited momentum transfer capability of neutrons at low energies favor x-rays to study collective excitations with large dispersion, like sound modes.

When the sound velocity exceeds that of neutrons in the liquid, x-rays become unique. The low-momentum/high-energy transfer region is only accessible by x-rays.

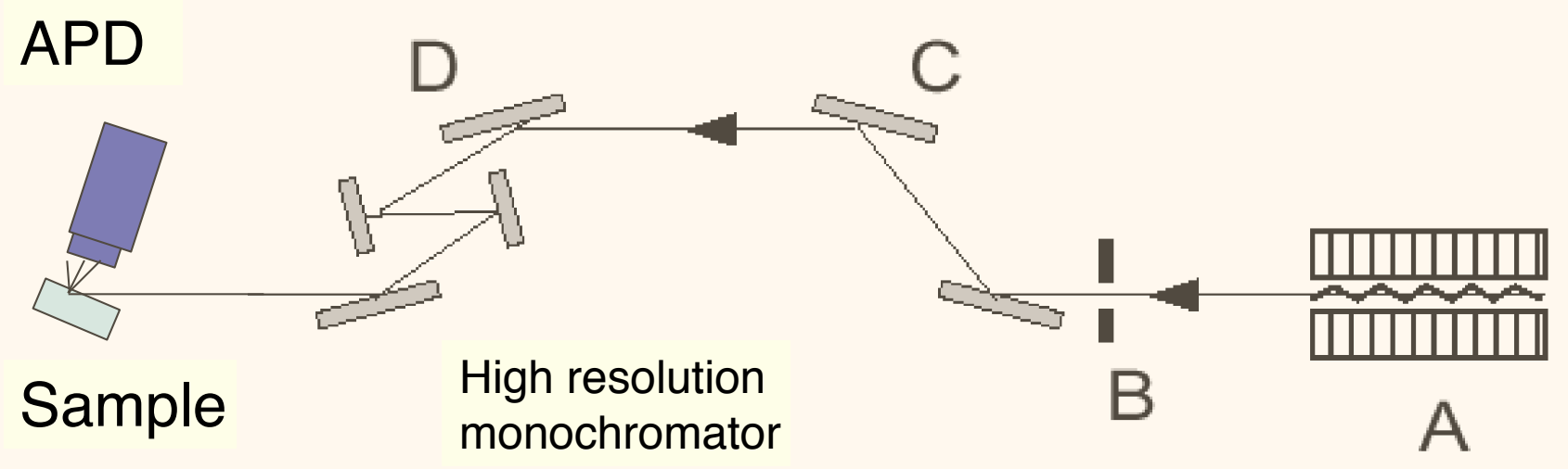


Inelastic X-Ray Scattering: two approaches

IXS: Momentum resolved

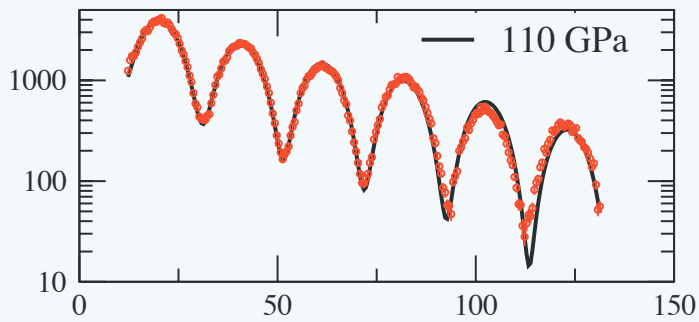


NRIXS: Momentum integrated



Nuclear Resonant Scattering

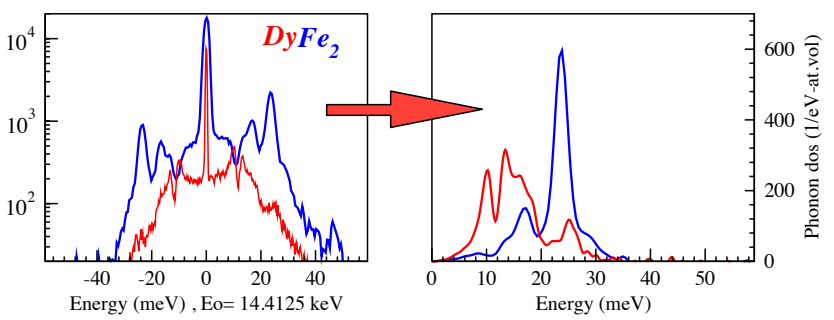
SMS: Synchrotron Mössbauer Spectroscopy NFS : Nuclear Forward Scattering



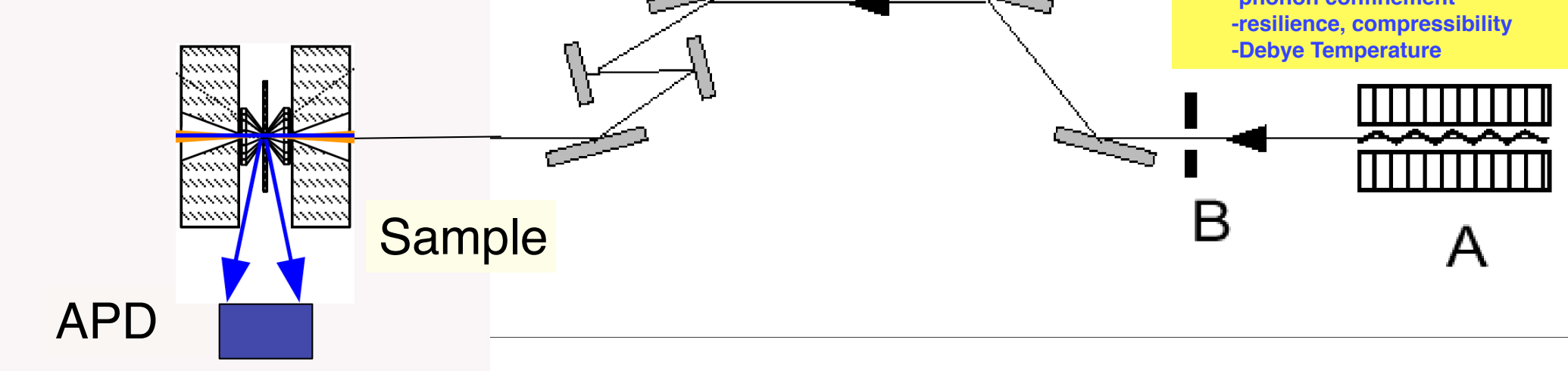
- Isomer shift
- Quadrupole splitting
- Magnetic hyperfine field
 - valence state
 - local crystallographic symmetry
 - magnetic ordering
 - relaxation



NRIXS: Nuclear Resonant Inelastic X-ray Scattering NRVS: Nuclear Resonant Vibrational Spectroscopy



- Partial phonon density of states
- Recoil-free fraction
 - speed of sound
 - vibrational modes
 - entropy and specific heat
 - phonon confinement
 - resilience, compressibility
 - Debye Temperature



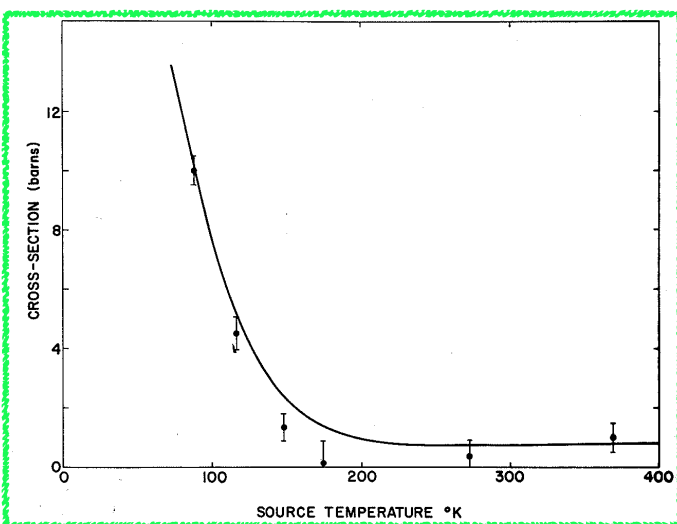
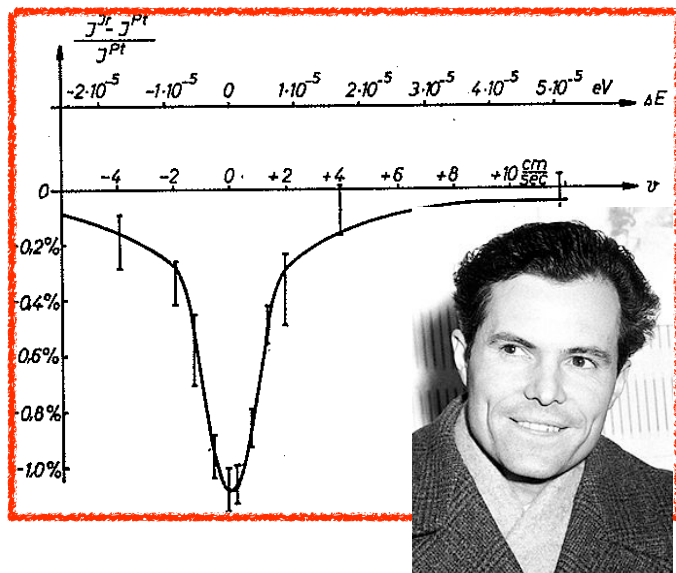
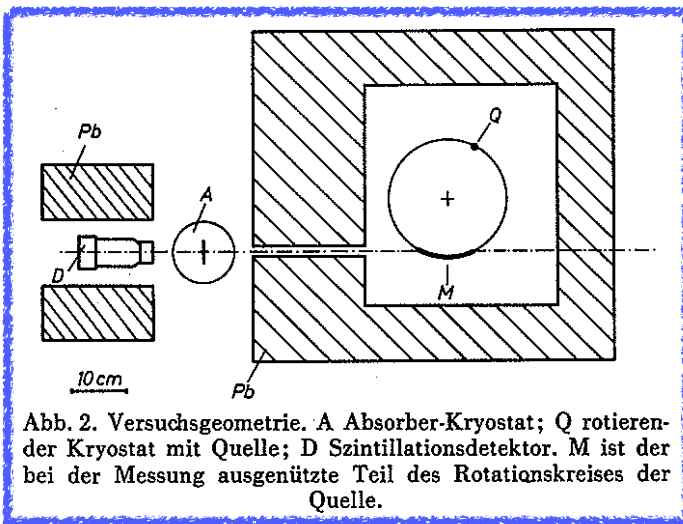
Kernresonanzabsorption von γ -Strahlung in Ir^{191}

VON RUDOLF L. MÖSSBAUER

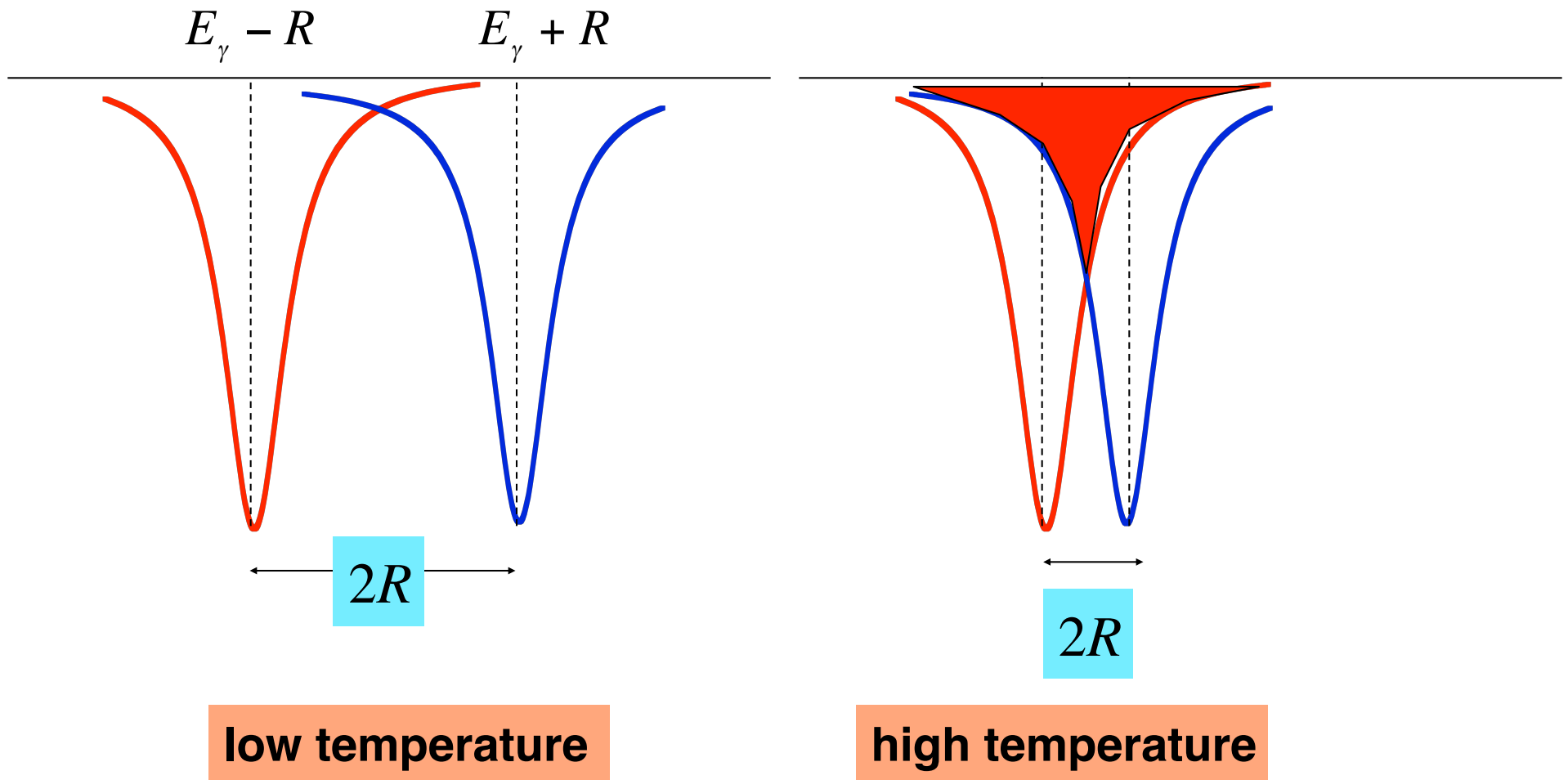
Aus dem Laboratorium für technische Physik der Technischen Hochschule in München
und dem Institut für Physik im Max-Planck-Institut für medizinische Forschung in Heidelberg

(Z. Naturforschg. 14 a, 211—216 [1959]; eingegangen am 5. November 1958)

Bei der Emission und Selbstabsorption von weicher γ -Strahlung in Kernen treten bei tiefen Temperaturen in Festkörpern sehr starke Linien mit der natürlichen Linienbreite auf. Diese Linien erscheinen als Folge davon, daß bei tiefen Temperaturen bei einem Teil der Quantenübergänge der γ -Rückstoßimpuls nicht mehr vom einzelnen Kern aufgenommen wird, sondern von dem Kristall als Ganzes. Da die scharfen Emissions- und Absorptionslinien energetisch an der gleichen Stelle liegen, tritt ein sehr starker **Resonanzfluoreszenzeffekt** auf. Durch eine „Zentrifugen“-Methode, bei der die Emissions- und Absorptionslinien gegeneinander verschoben werden, läßt sich der Fluoreszenzeffekt unterdrücken und so eine unmittelbare Bestimmung der natürlichen Linienbreite von Resonanzlinien vornehmen. Erste Messungen nach dieser Methode ergeben für die Lebenszeit τ des 129 keV-Niveaus in Ir^{191} : $\tau = \left(1,4 \begin{smallmatrix} +0,2 \\ -0,1 \end{smallmatrix}\right) \cdot 10^{-10}$ sec.

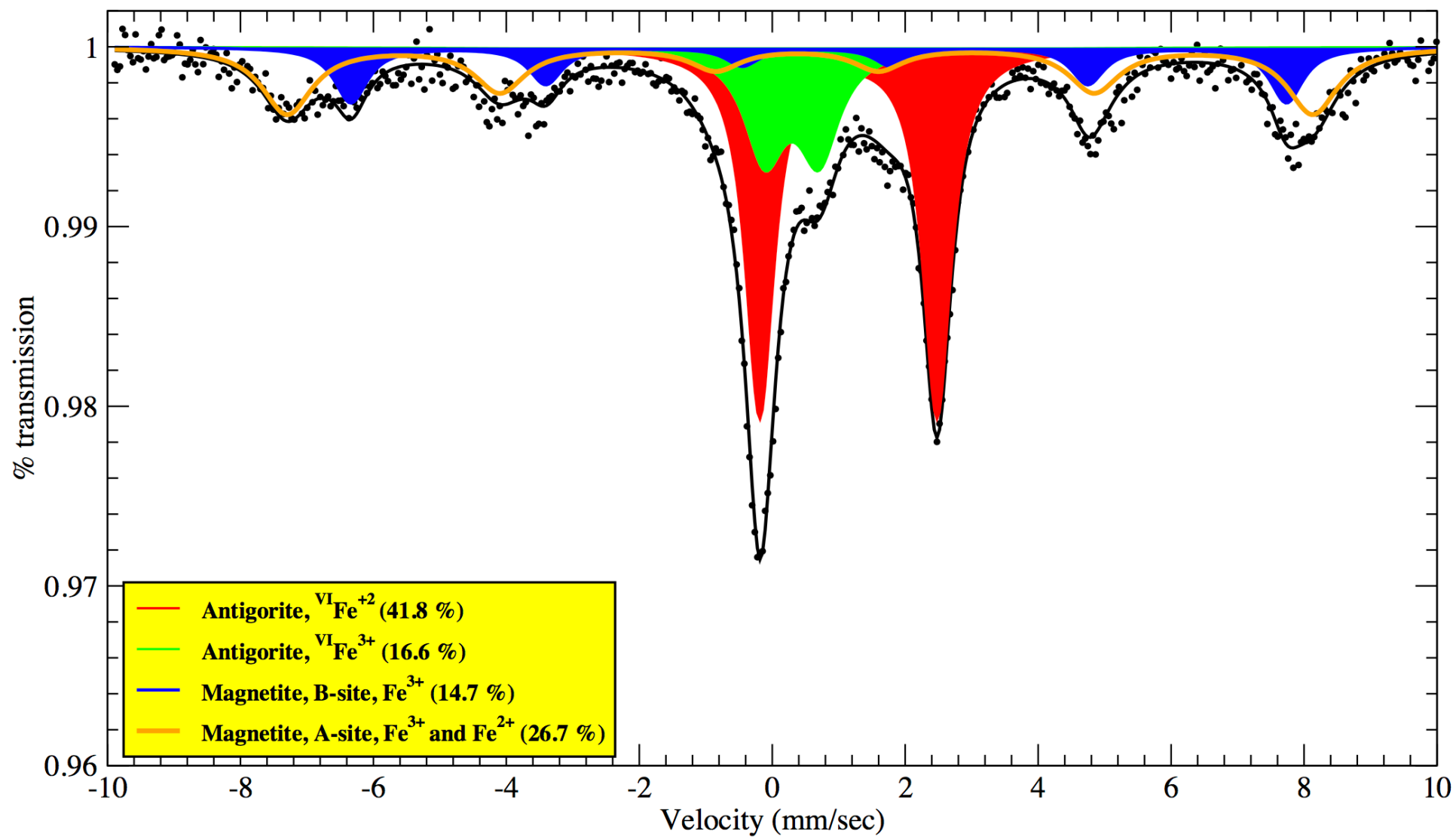
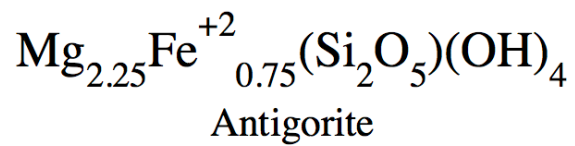


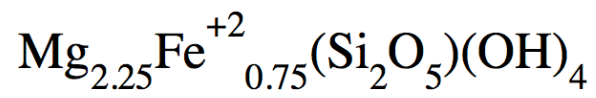
absorption-emission & recoil



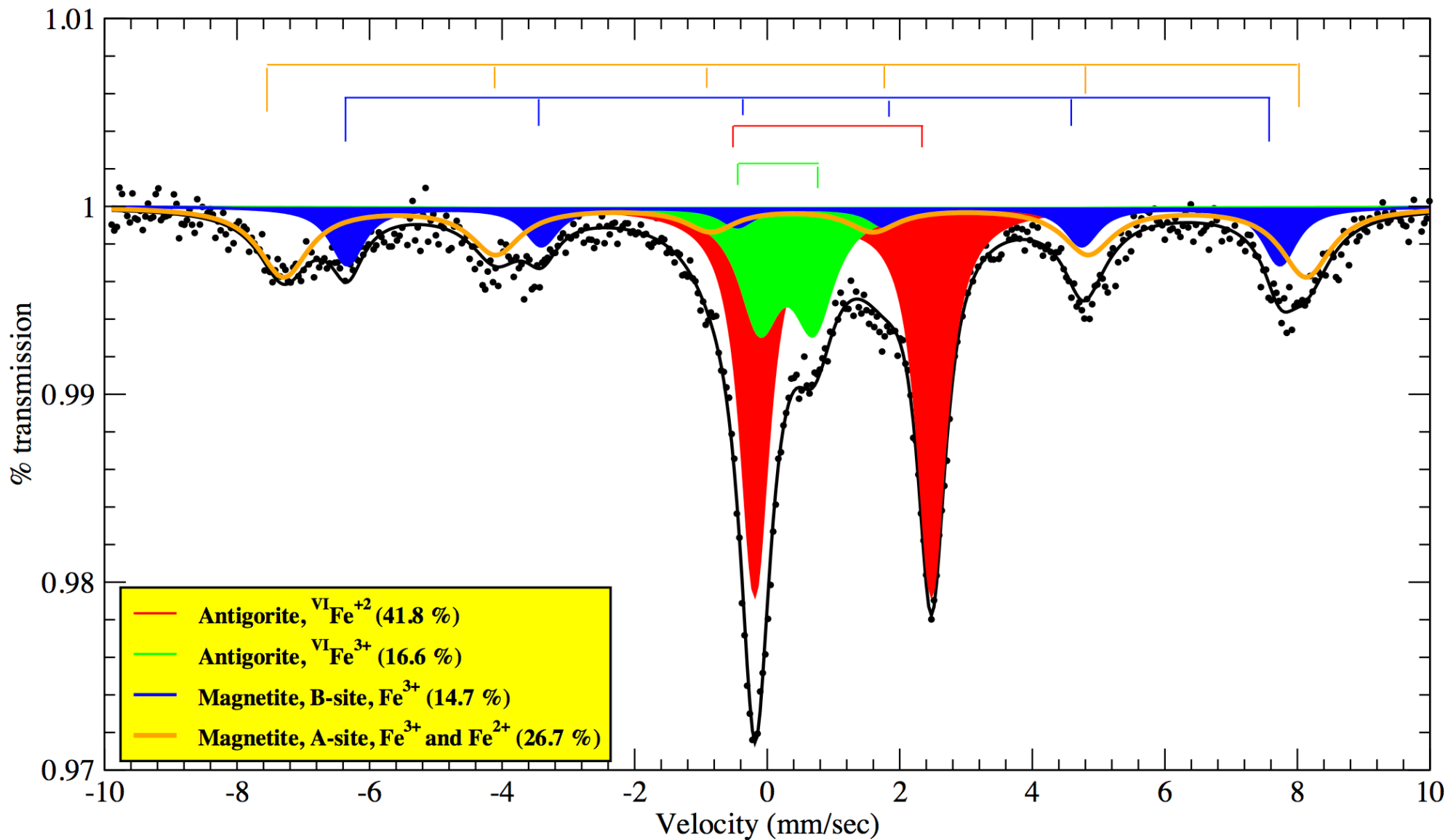
intuitive expectation: large resonance absorption at high temperature

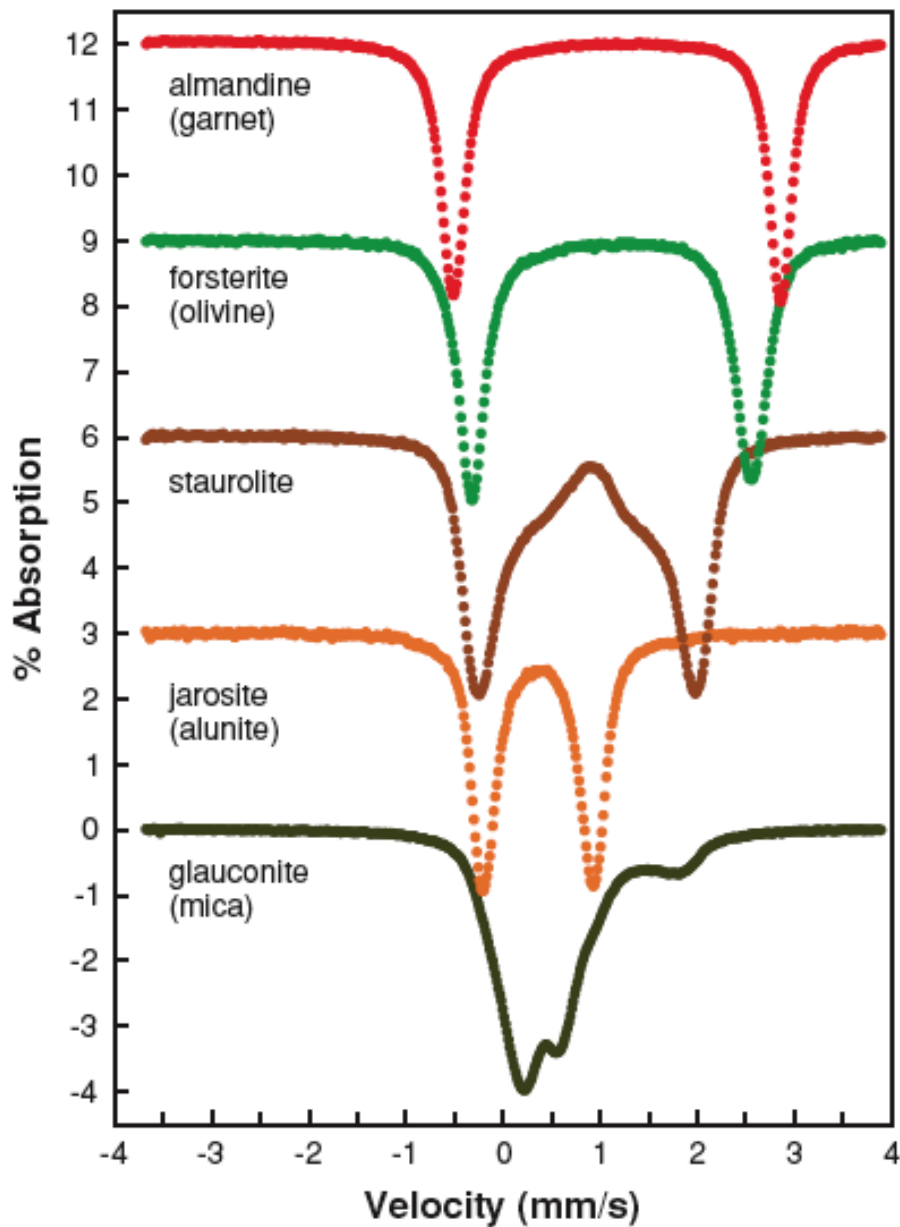
Mossbauer's observation: less absorption at high temperature





Antigorite





Fe²⁺, cubic

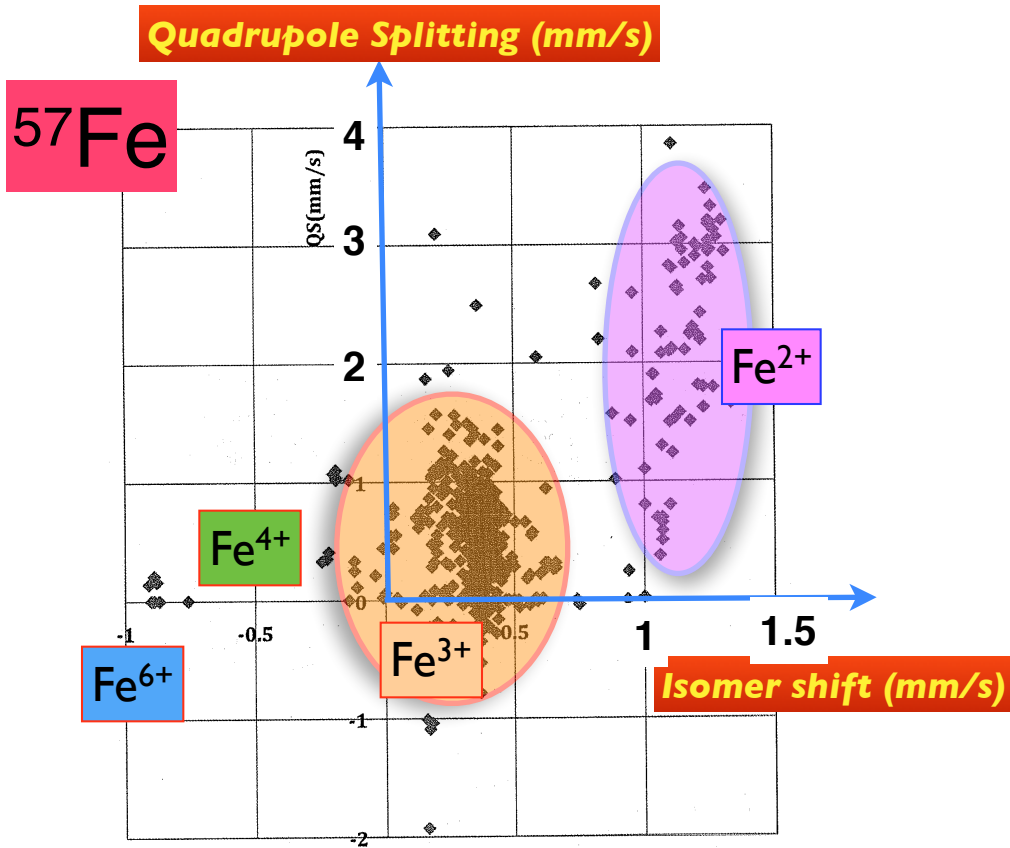
Fe²⁺, octahedral

Fe²⁺, tetrahedral

Fe³⁺, octahedral

Fe³⁺, tetrahedral

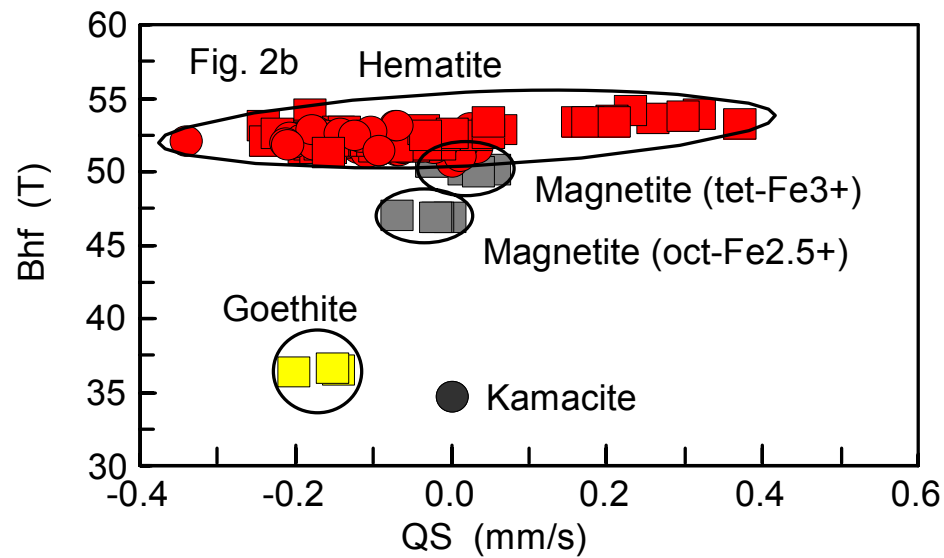
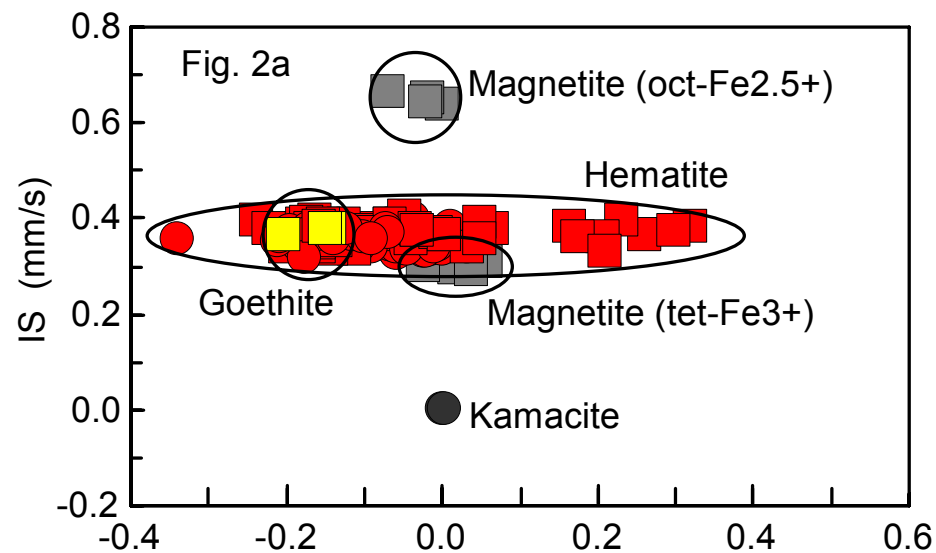
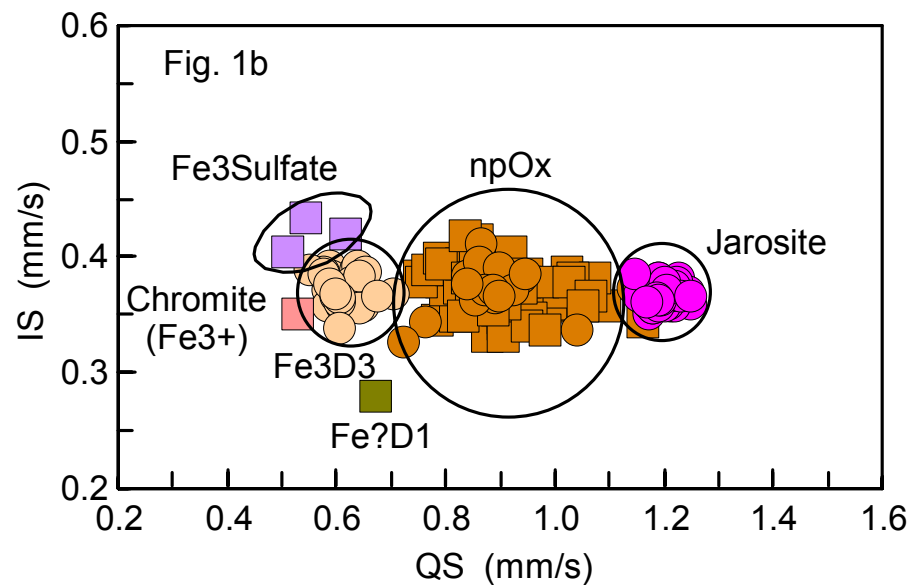
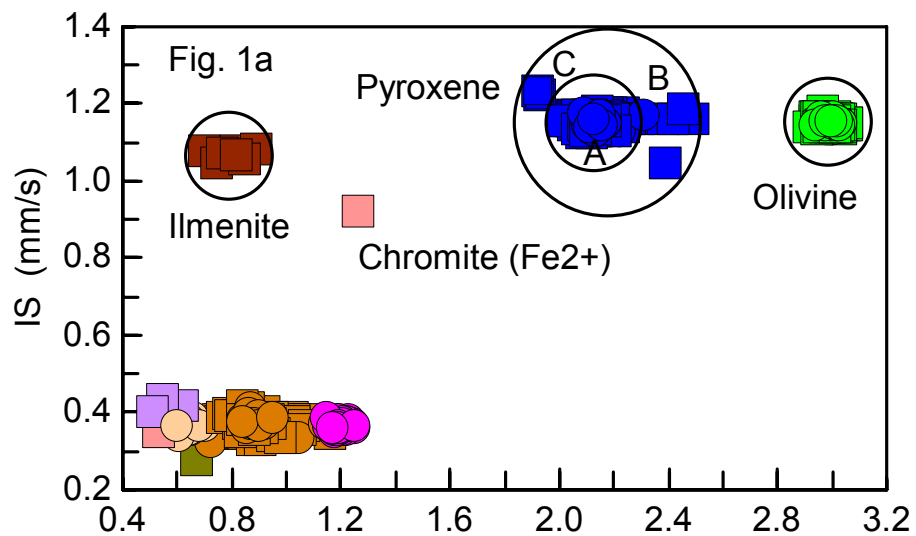
How isomer shift & quadrupole splitting are used for valence identification in Mössbauer Spectroscopy ?



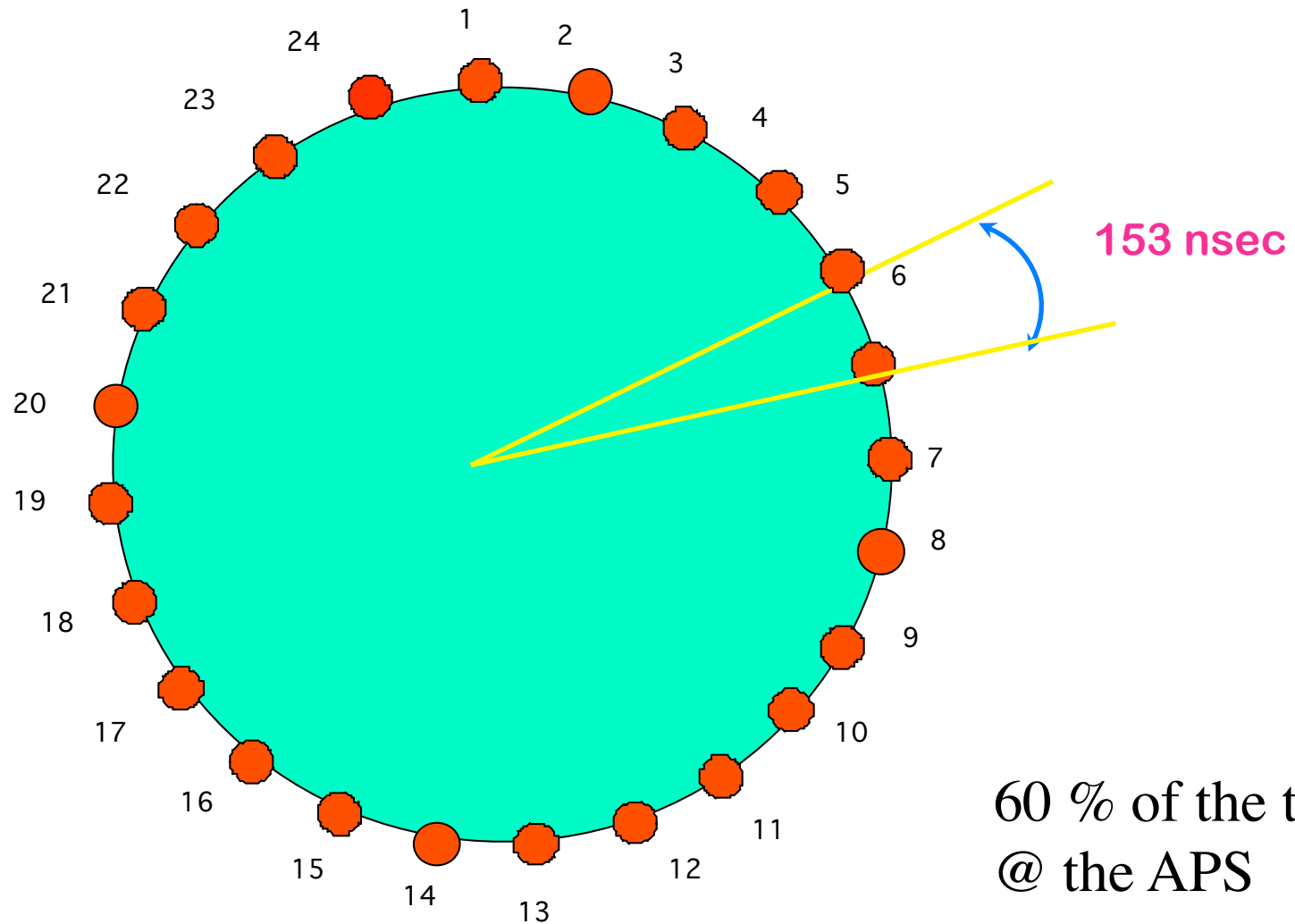
After 50 years of research and more than 10,000 papers, approximately 800 iron compounds have been classified, and the results are disseminated by the Mössbauer Effect Data Center (MEDC).

Given the fact that measured Mössbauer line-widths are typically 0.3 mm/sec, it is common to determine IS and QS with an accuracy of 0.1 mm/sec.

Hence, in many circumstances, this combination of IS-QS values provide valuable guidance into valence issues in minerals, lunar rocks, and meteorite studies.

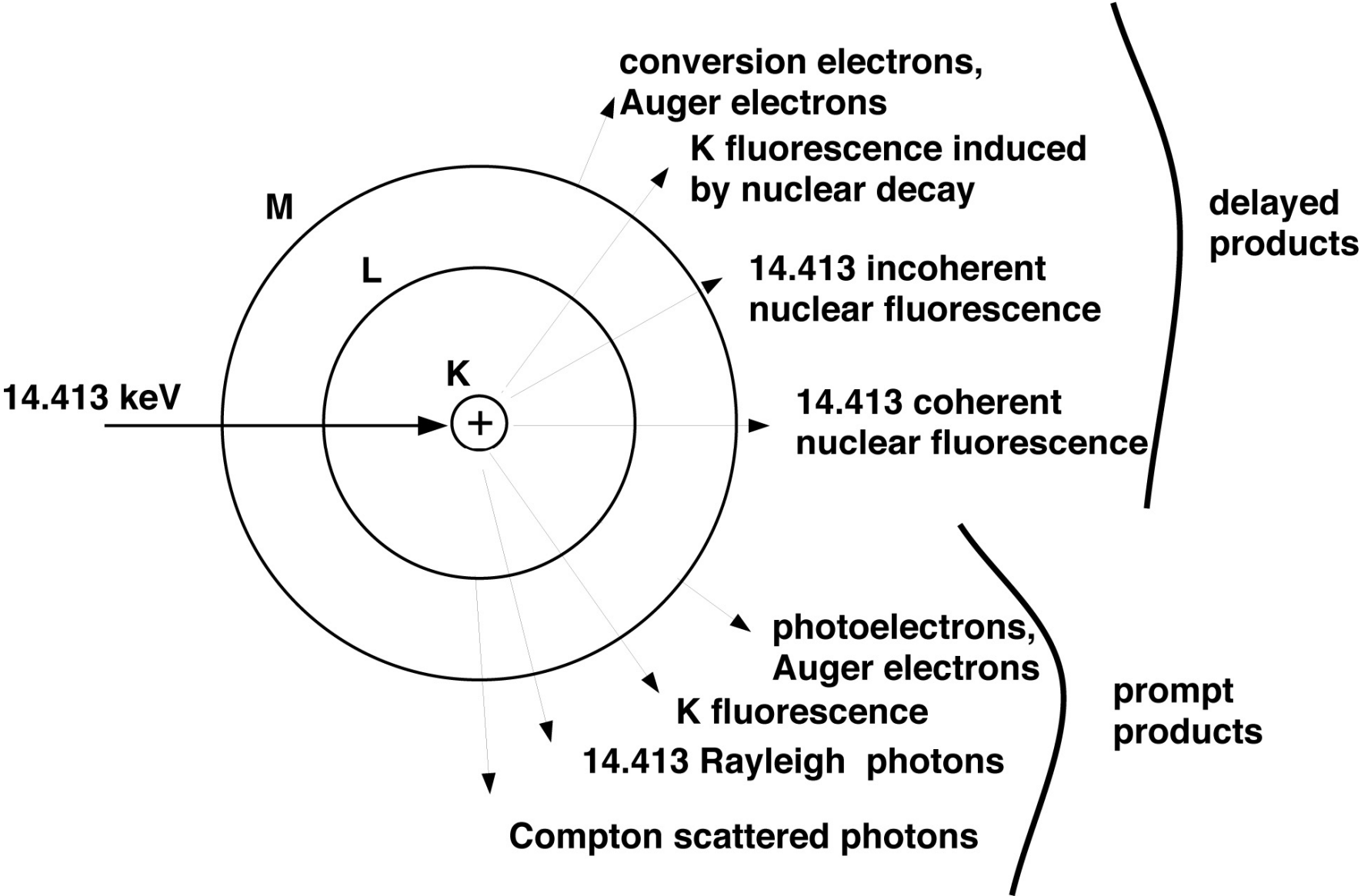


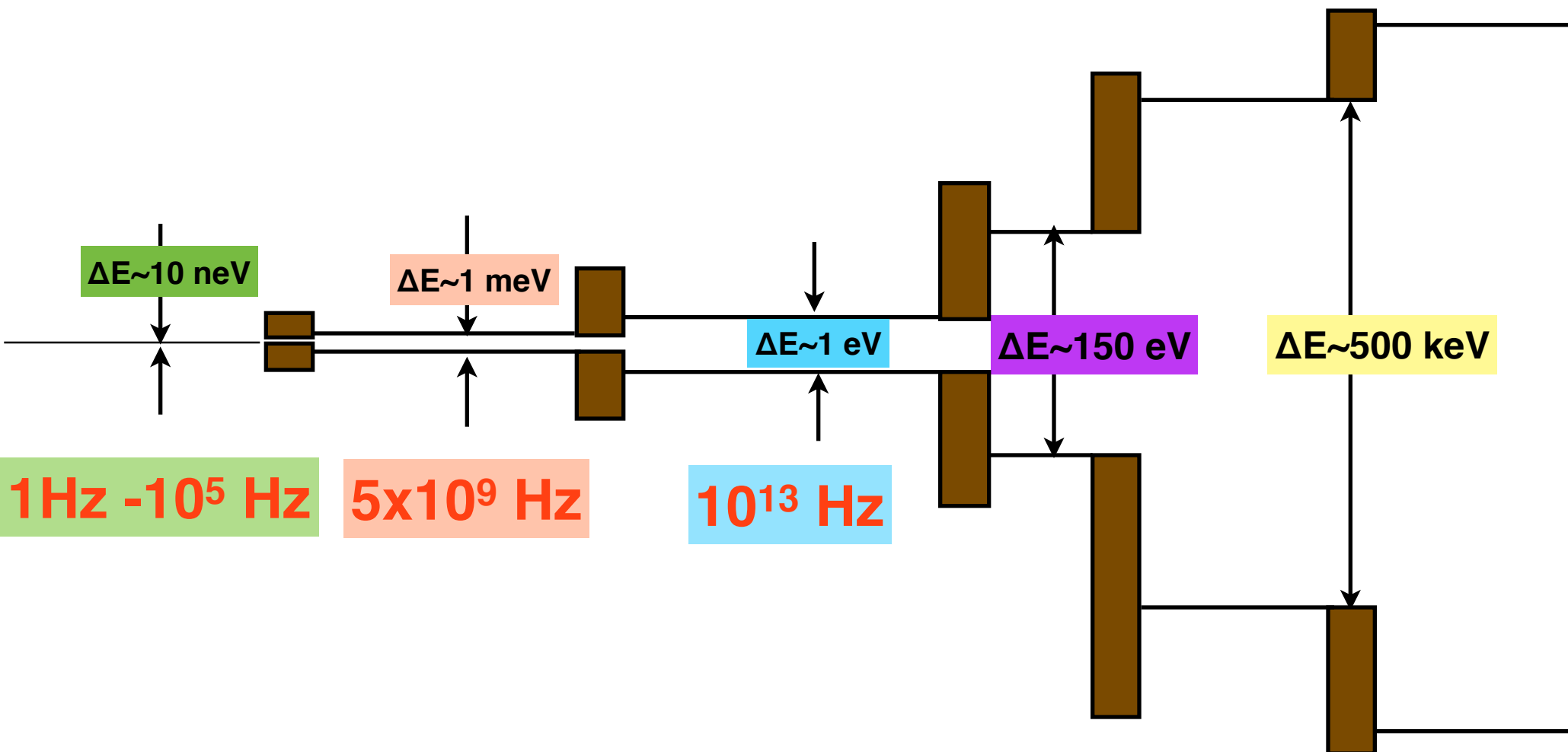
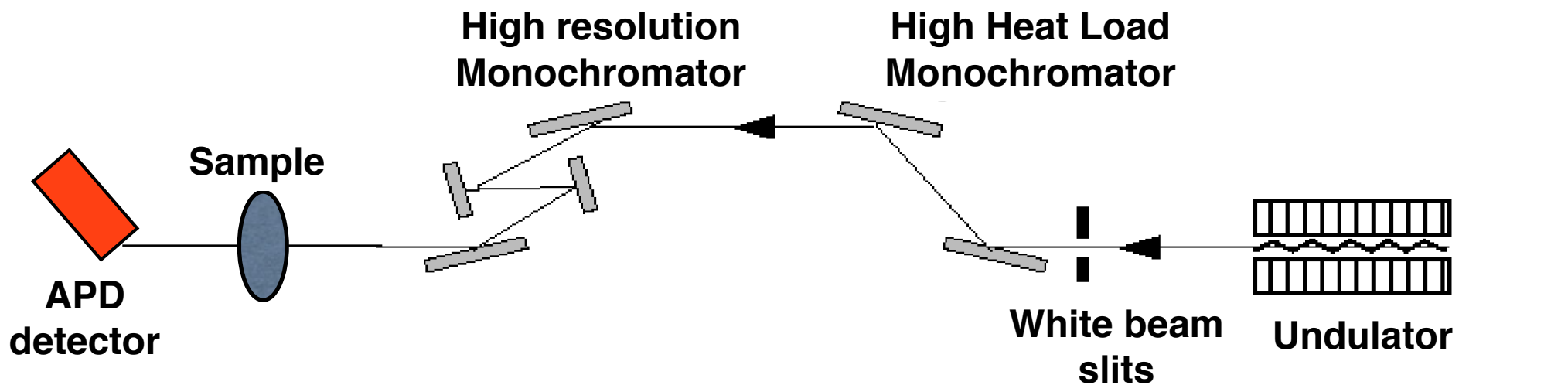
Standard Time structure @ APS



1 revolution = 3.68 μ sec \Rightarrow 1296 buckets

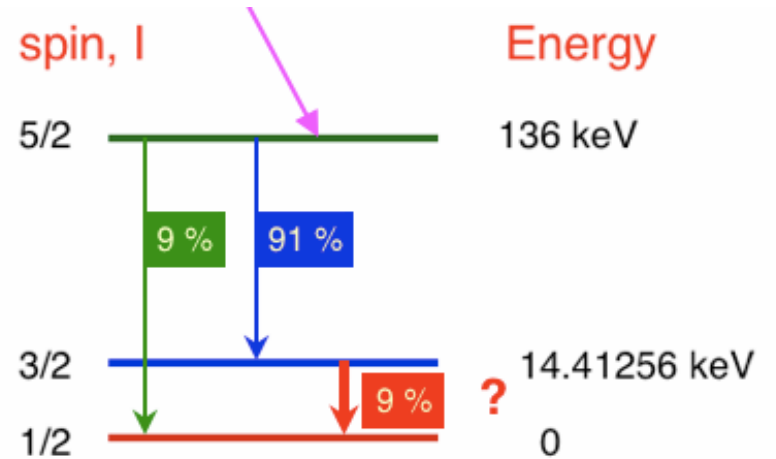
Nuclear Resonance and Fallout in ^{57}Fe -decay





Detection of nuclear decay

^{57}Fe



prompt photons

log I

exponential decay

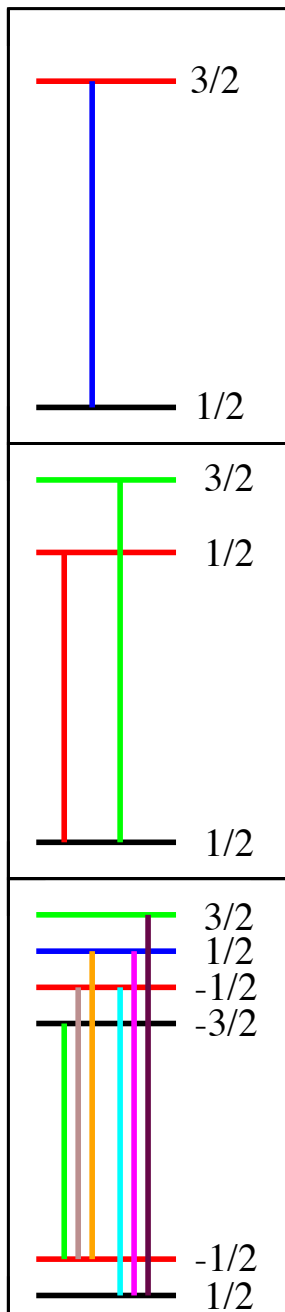
delayed photons

0

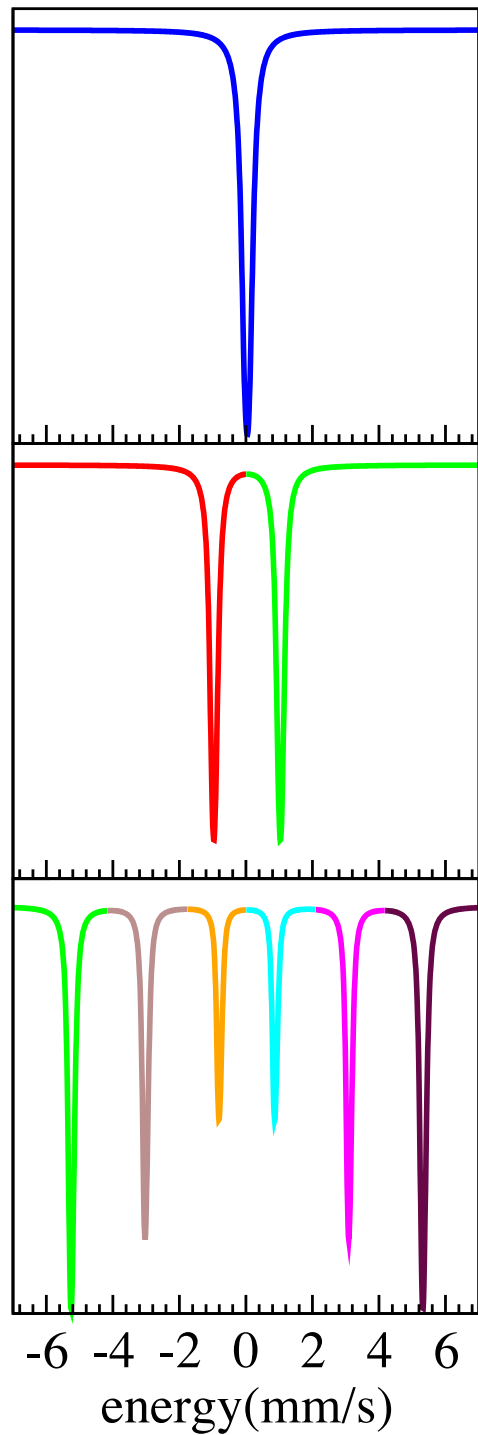
time (nsec)

153 nsec

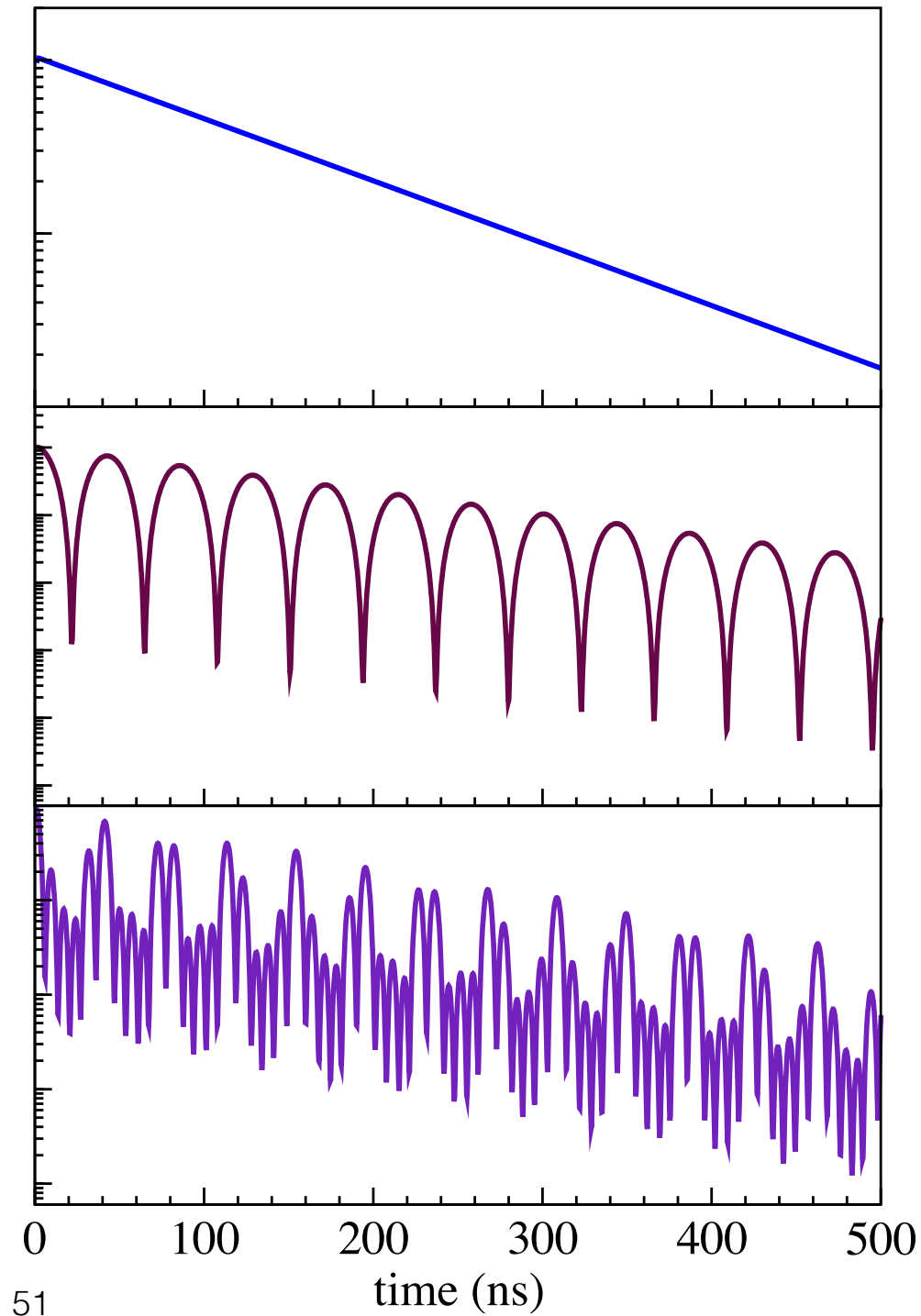
Level Diagram



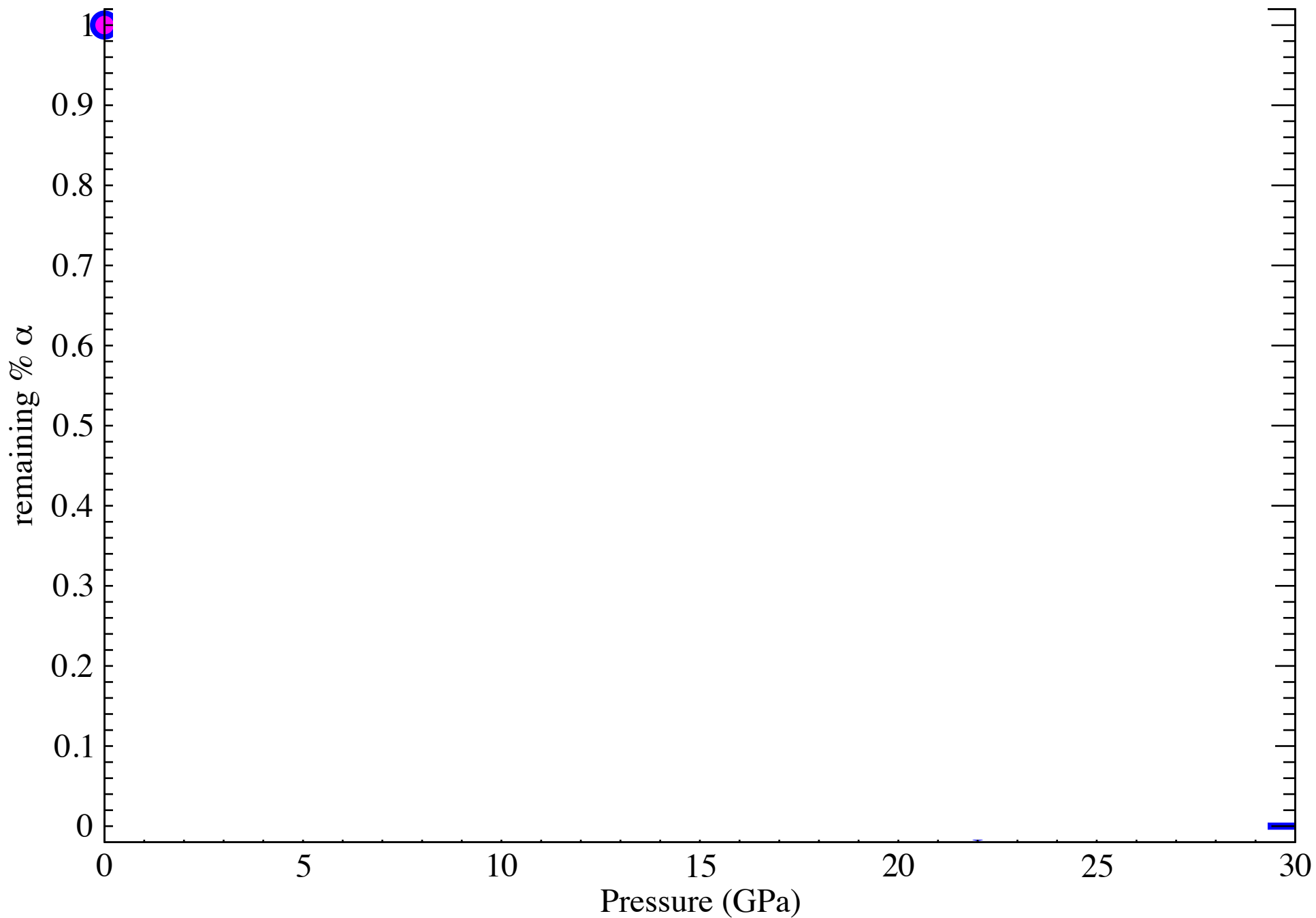
Energy domain



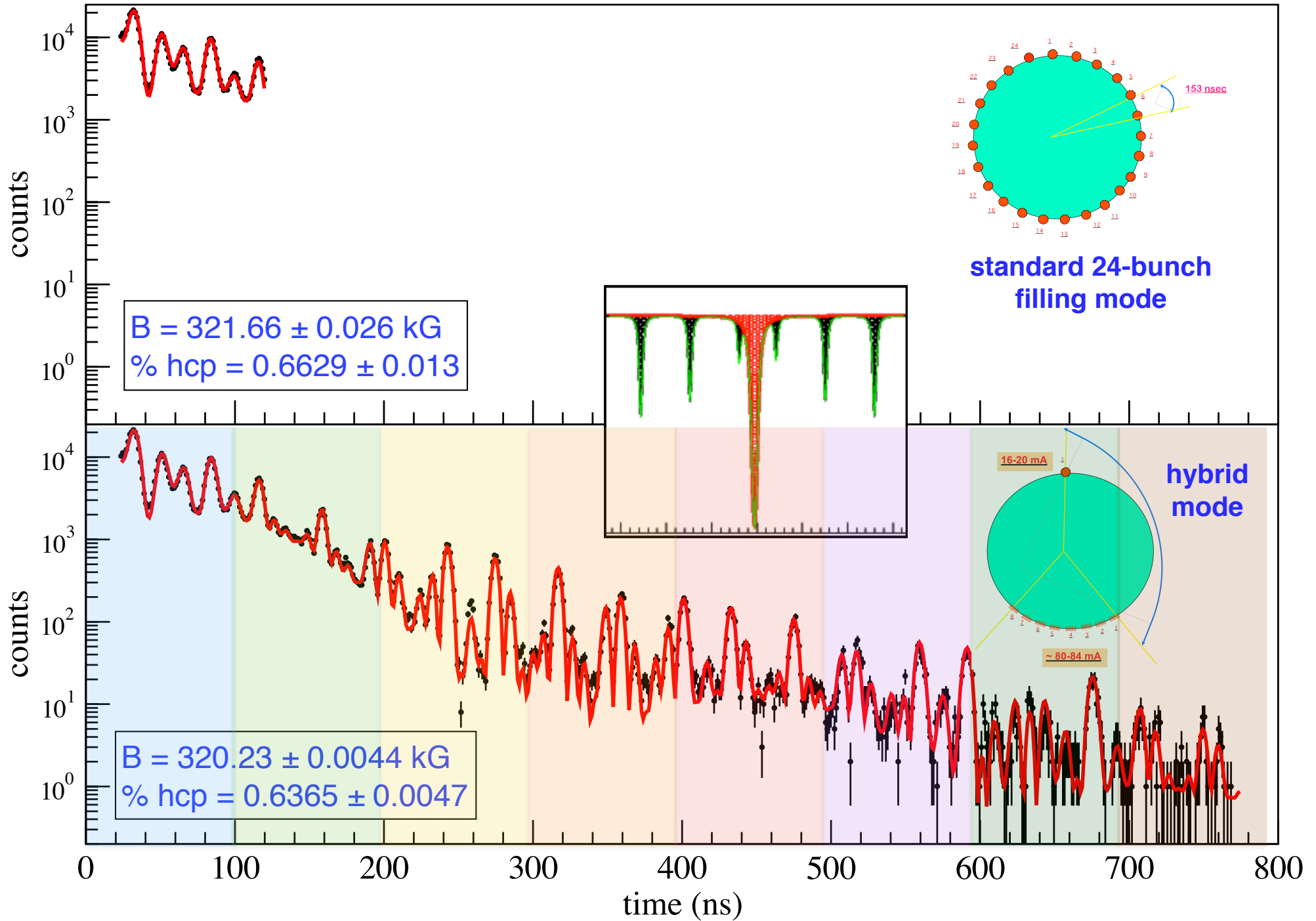
Time domain (SMS or NFS)



α (bcc-Fe) to ϵ (fcc-Fe) transition under pressure by synchrotron Mössbauer spectroscopy



mixed alpha & epsilon phase of pure iron at 15.3 GPa pressure

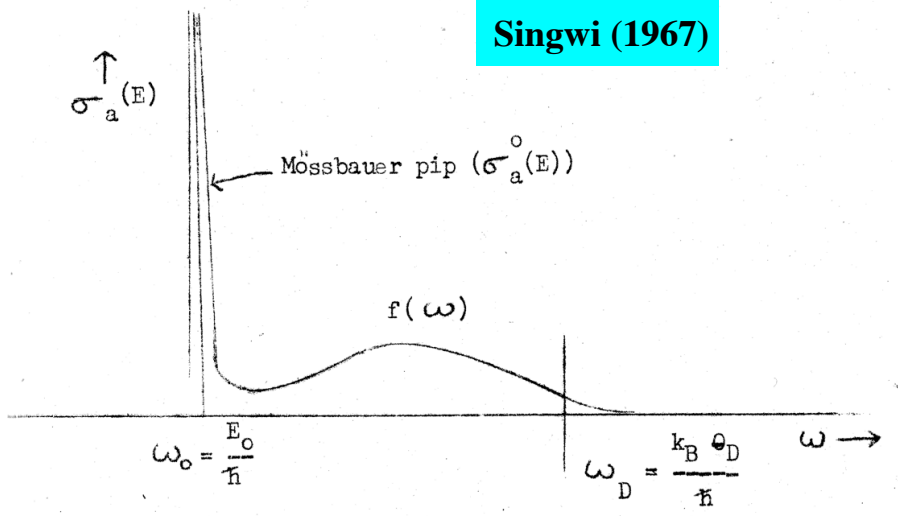


Early dreamers..

Visualized by W. Vischer at Los Alamos & K. S. Singwi at Argonne (1960), but only properly observed after synchrotron radiation based tunable monochromators are realized.

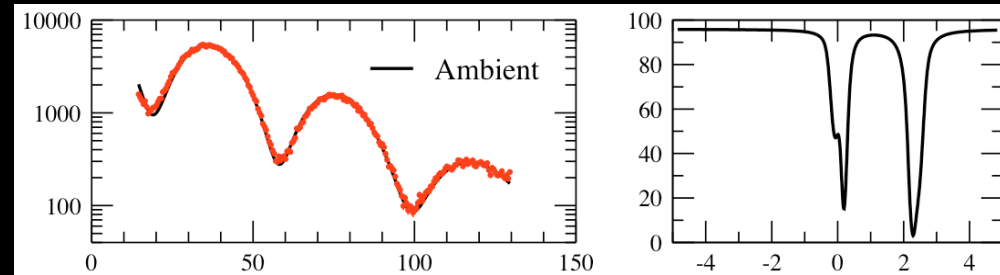
(W. Sturhahn et al, PRL, 74 (1995) p. 3832)

Singwi (1967)



Zero phonon “Mössbauer pip”

Visualized by Stan Ruby (1974) at Argonne and properly observed by E. Gerdau (Hamburg).
(S. L Ruby. J. de Physique 35 (1974) C6-209)



5 neV + mono. resolution

Phonon annihilation

Phonon creation

- 0 +
Energy (~ meV)

Phonon Density of States Measured by Inelastic Nuclear Resonant Scattering

W. Sturhahn, T. S. Toellner, and E. E. Alp

Advanced Photon Source, Argonne National Laboratory, Argonne, Illinois 60439

X. Zhang and M. Ando

Photon Factory, National Laboratory for High Energy Physics, Oho 1-1, Tsukuba, Ibaraki 305, Japan

Y. Yoda and S. Kikuta

Department of Applied Physics, Faculty of Engineering, The University of Tokyo, Hongo 7-3-1, Bunkyo-ku, Tokyo 113, Japan

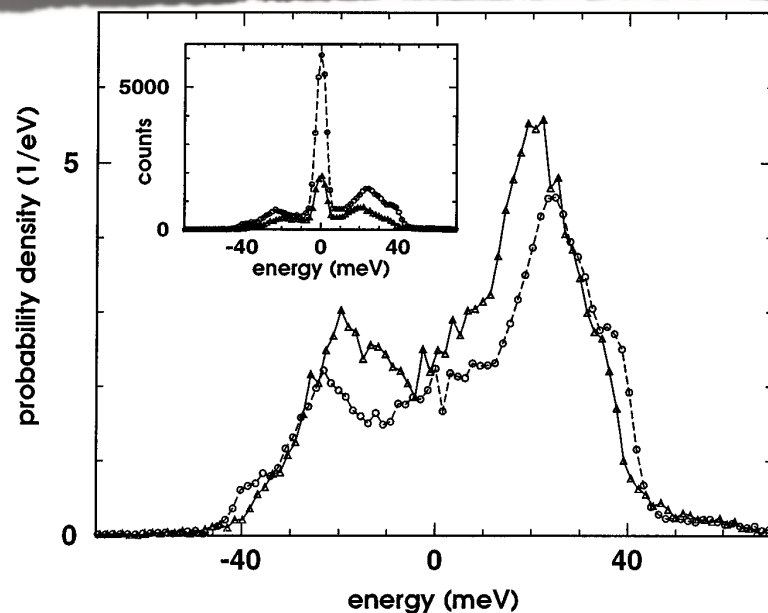
M. Seto

Research Reactor Institute, Kyoto University, Sennan-gun, Osaka 590-04, Japan

C. W. Kimball and B. Dabrowski

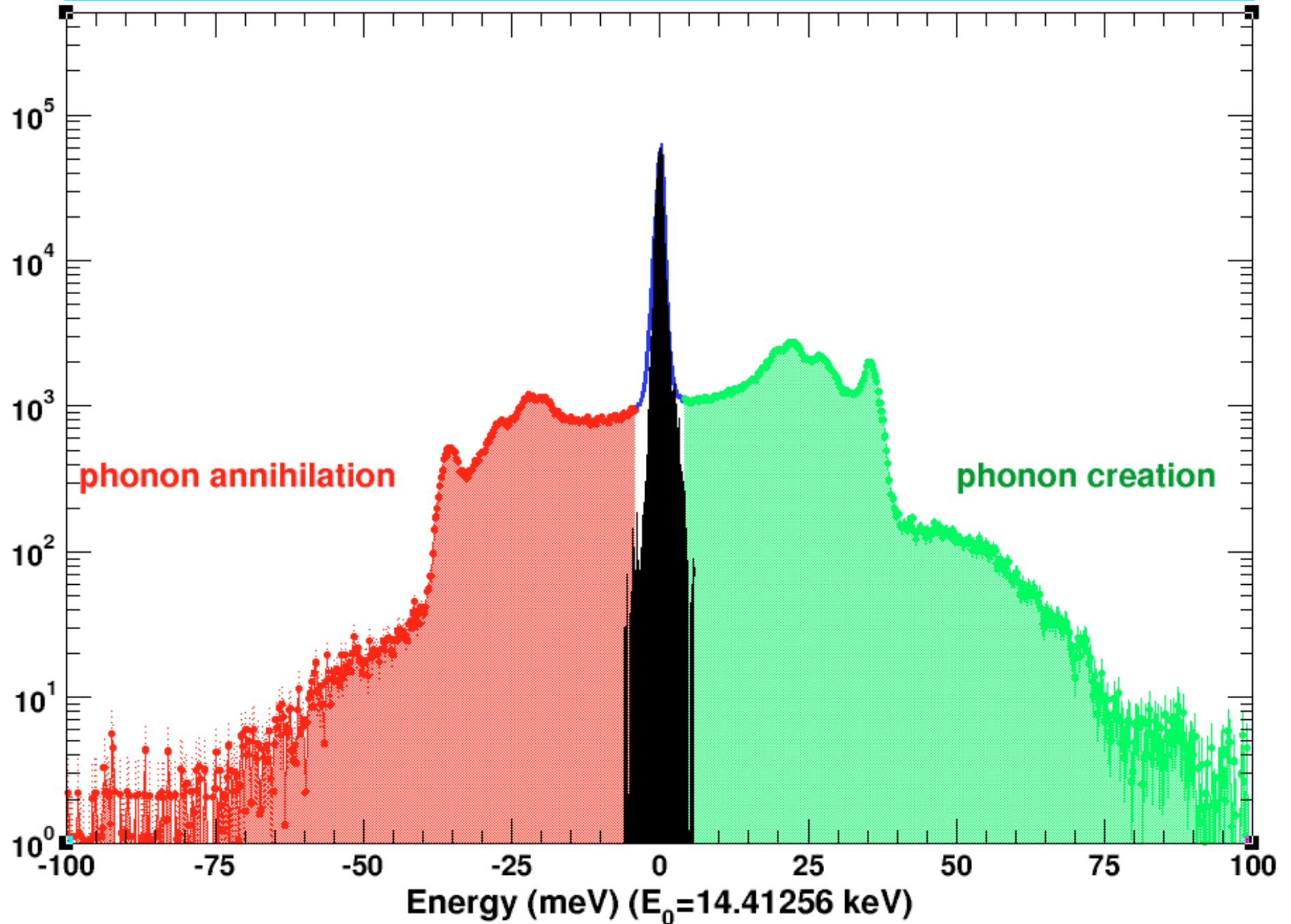
Department of Physics, Northern Illinois University, De Kalb, Illinois 60115

(Received 16 December 1994)

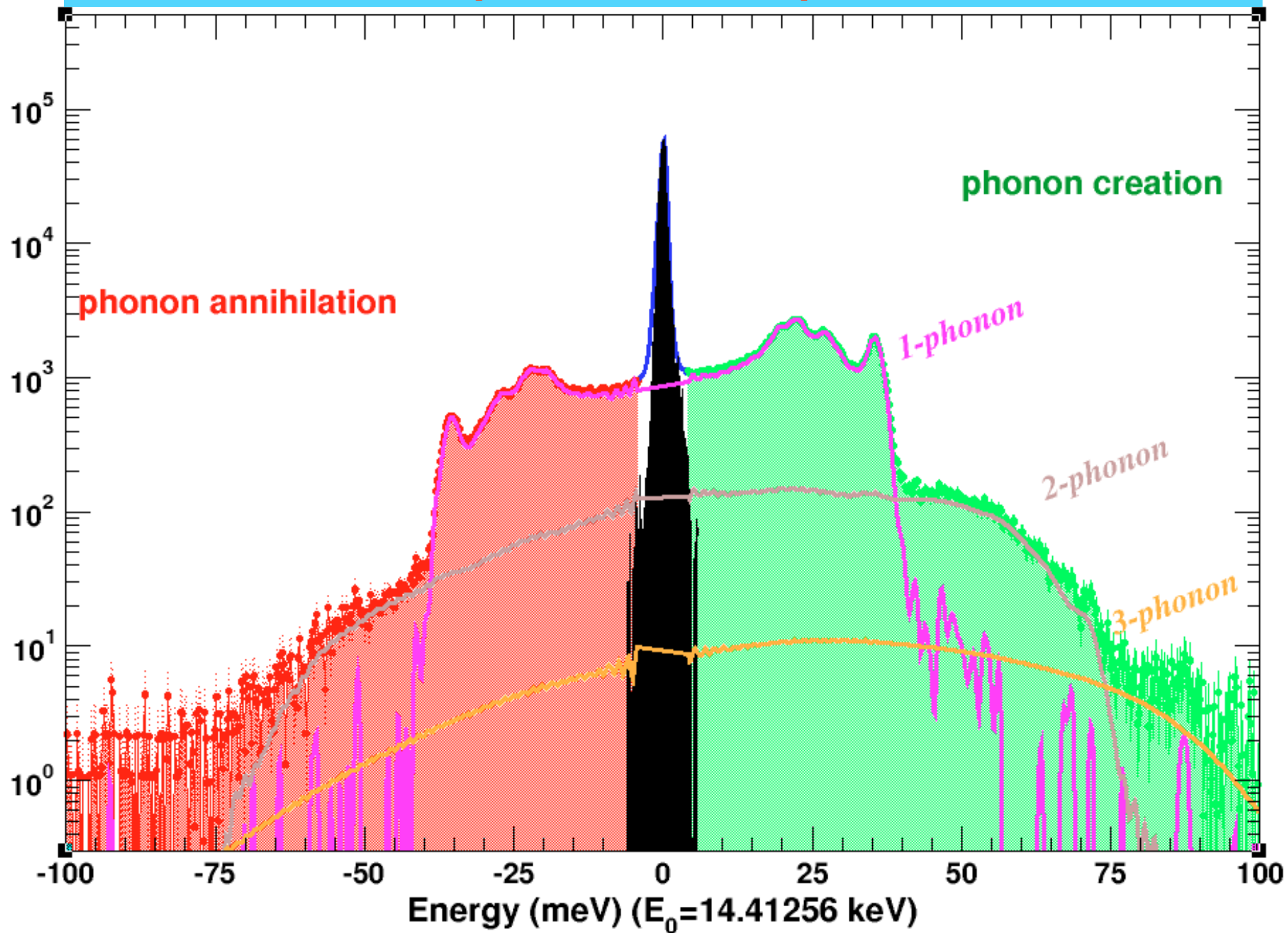


> 400 citations

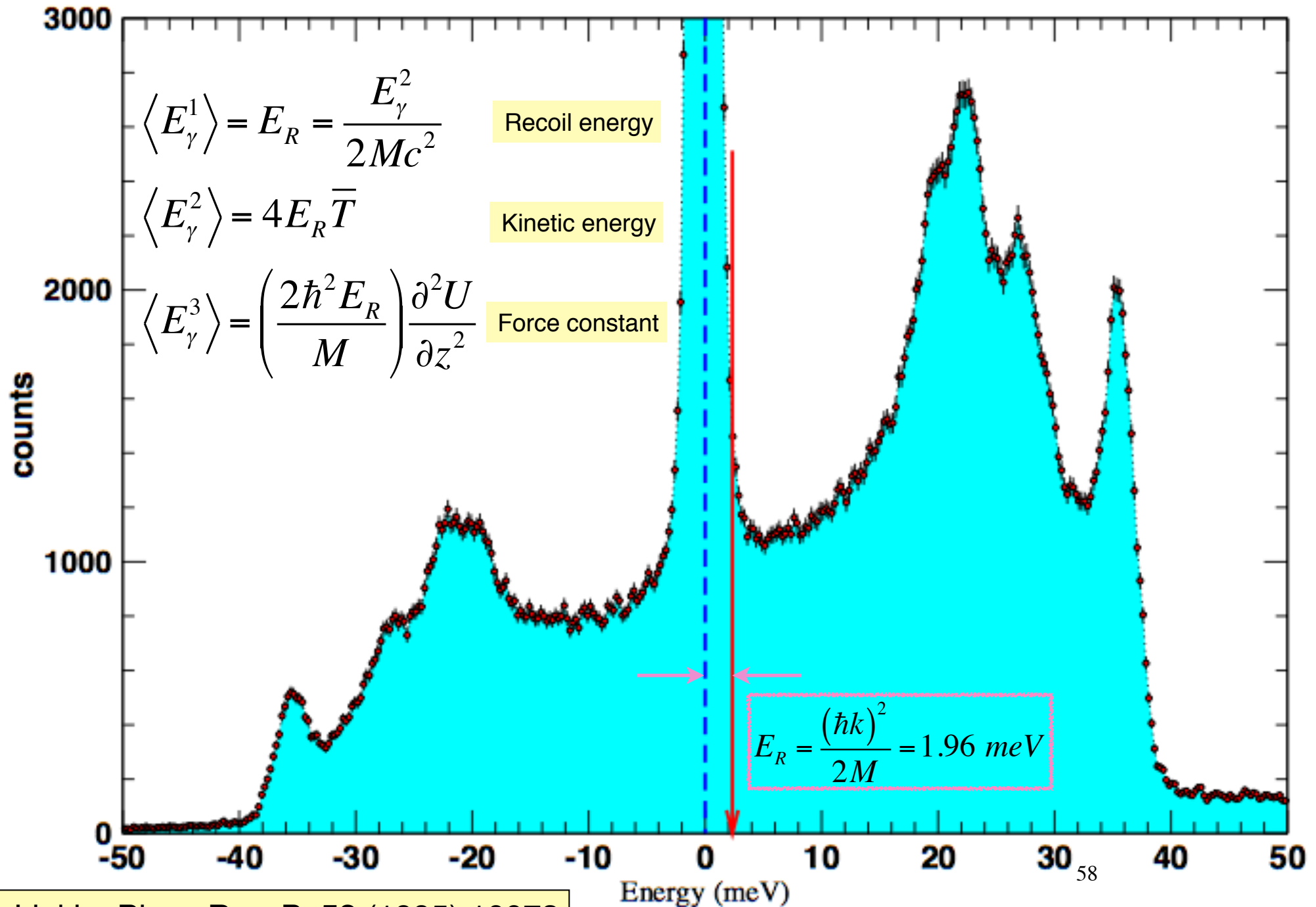
Phonon excitation probability



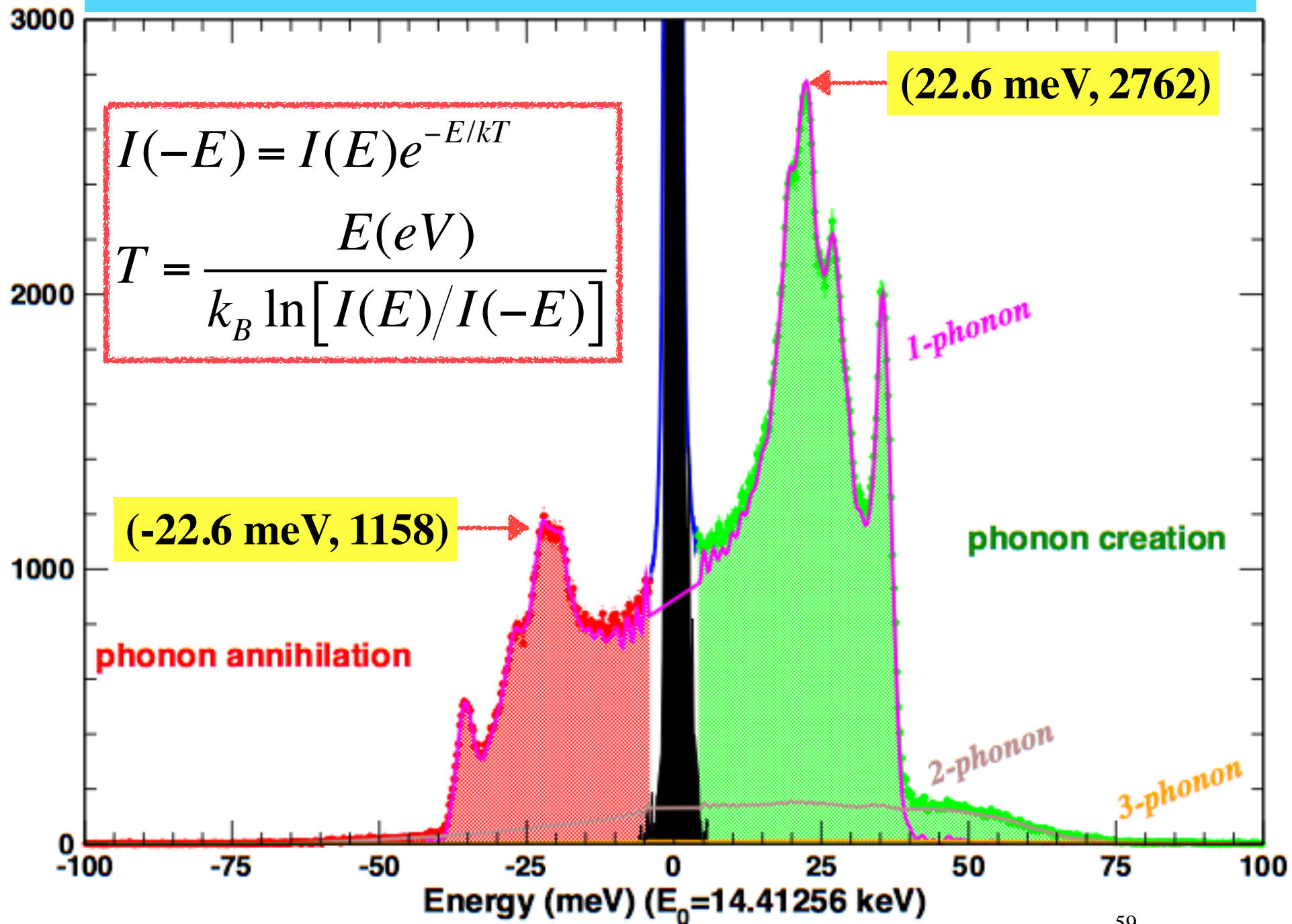
Multi-phonon decomposition



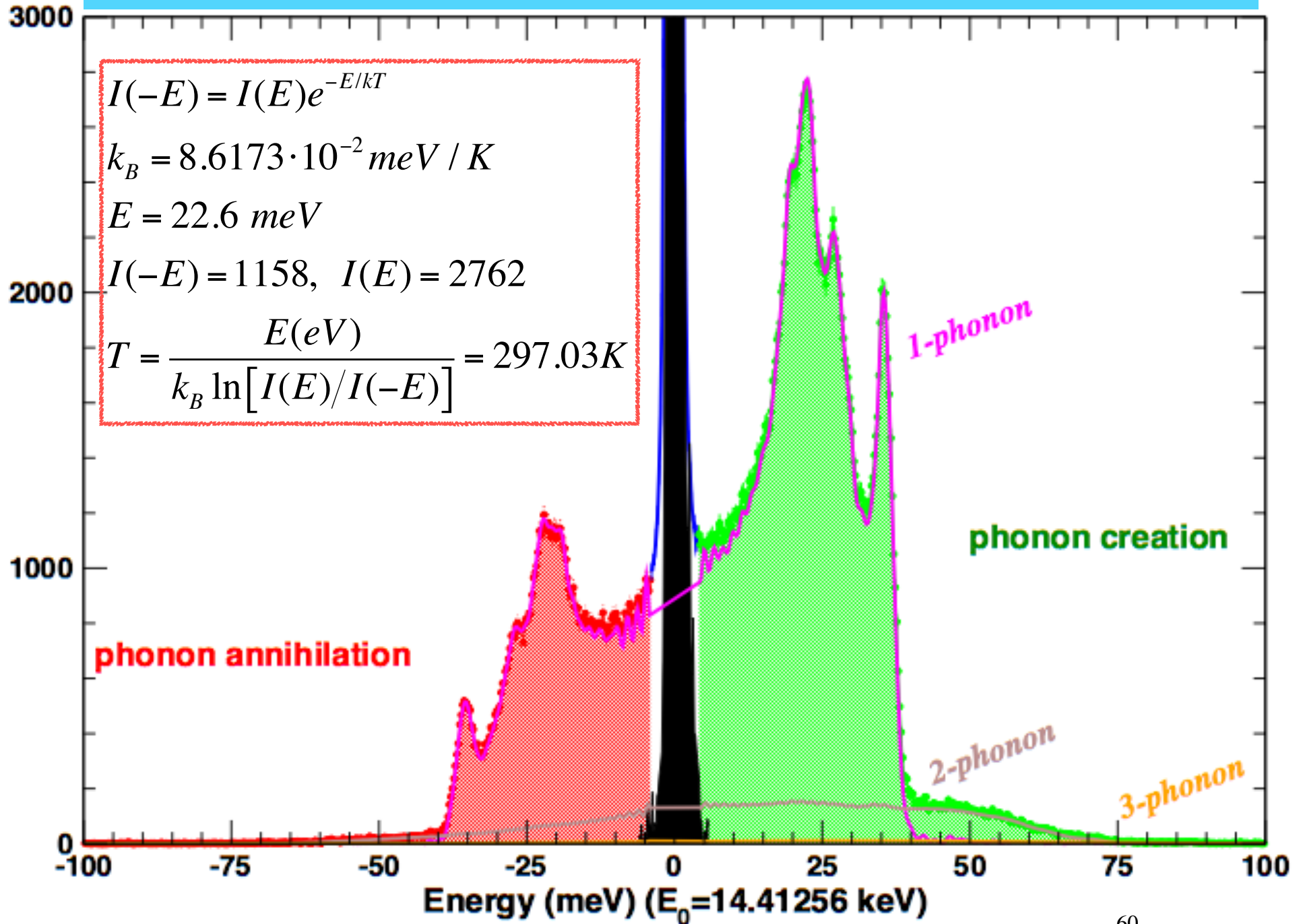
Lipkin's sum rules related to phonon excitation probability



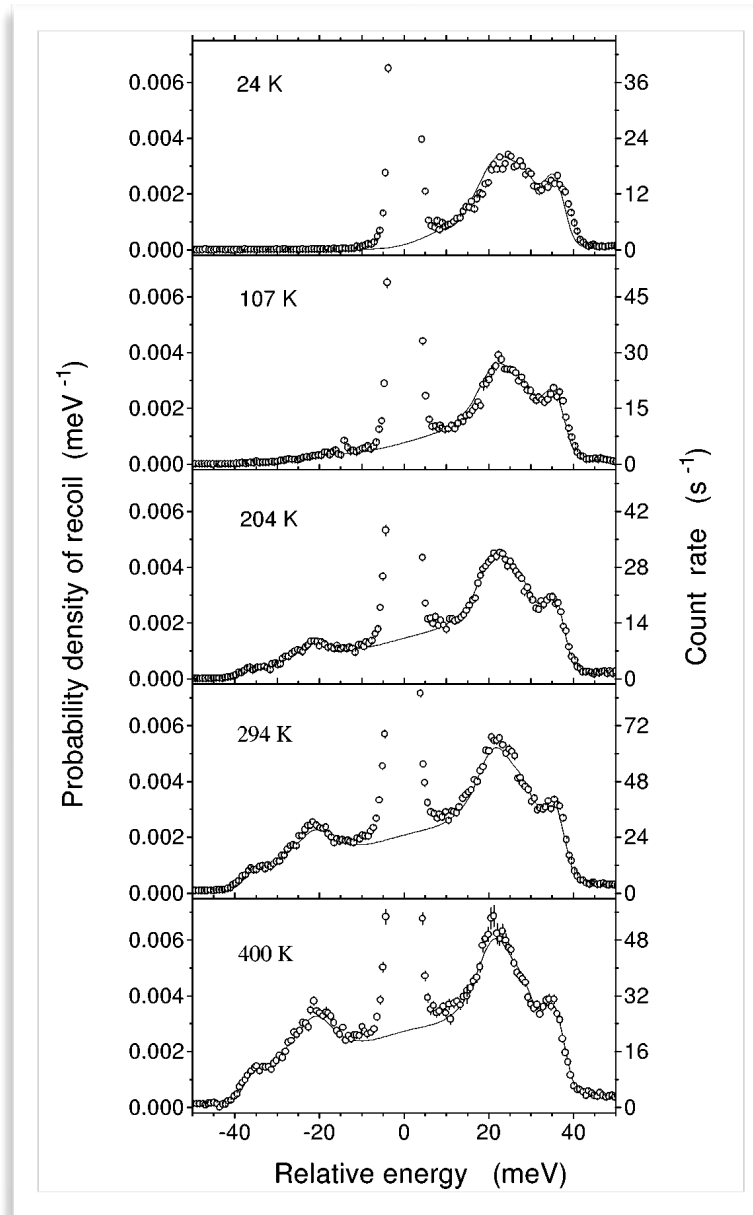
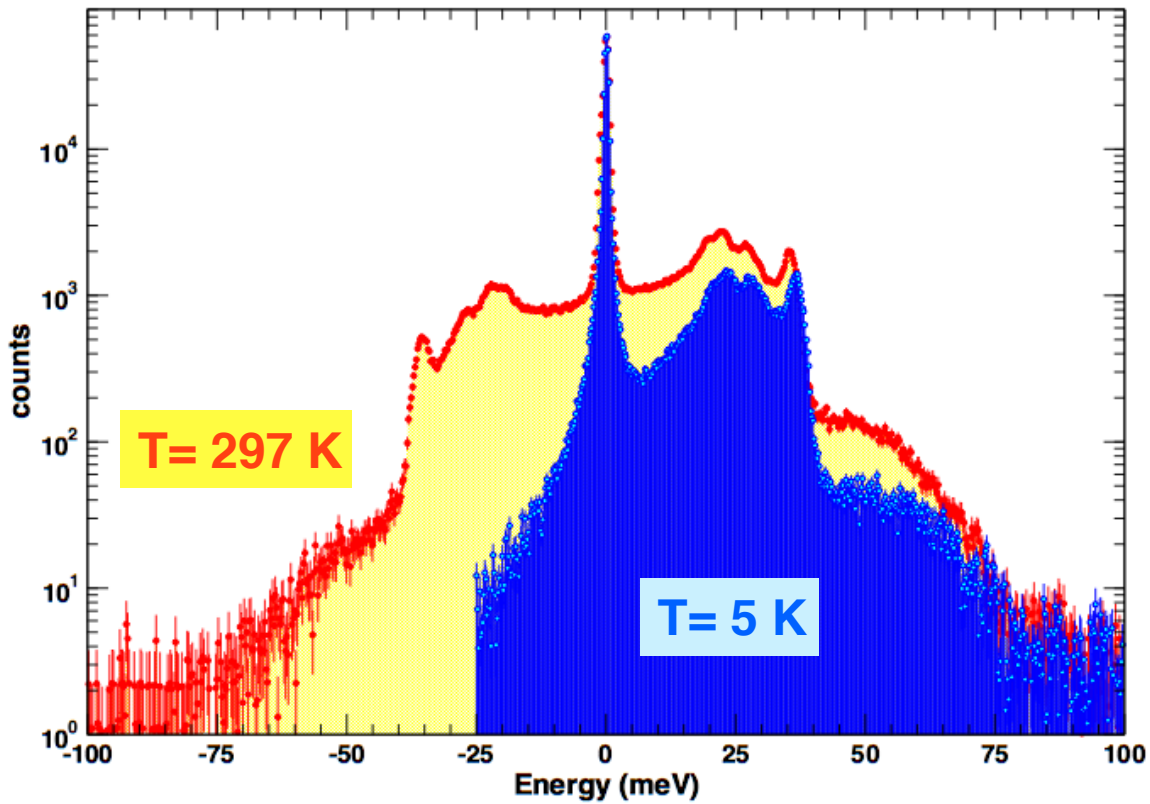
Detailed Balance

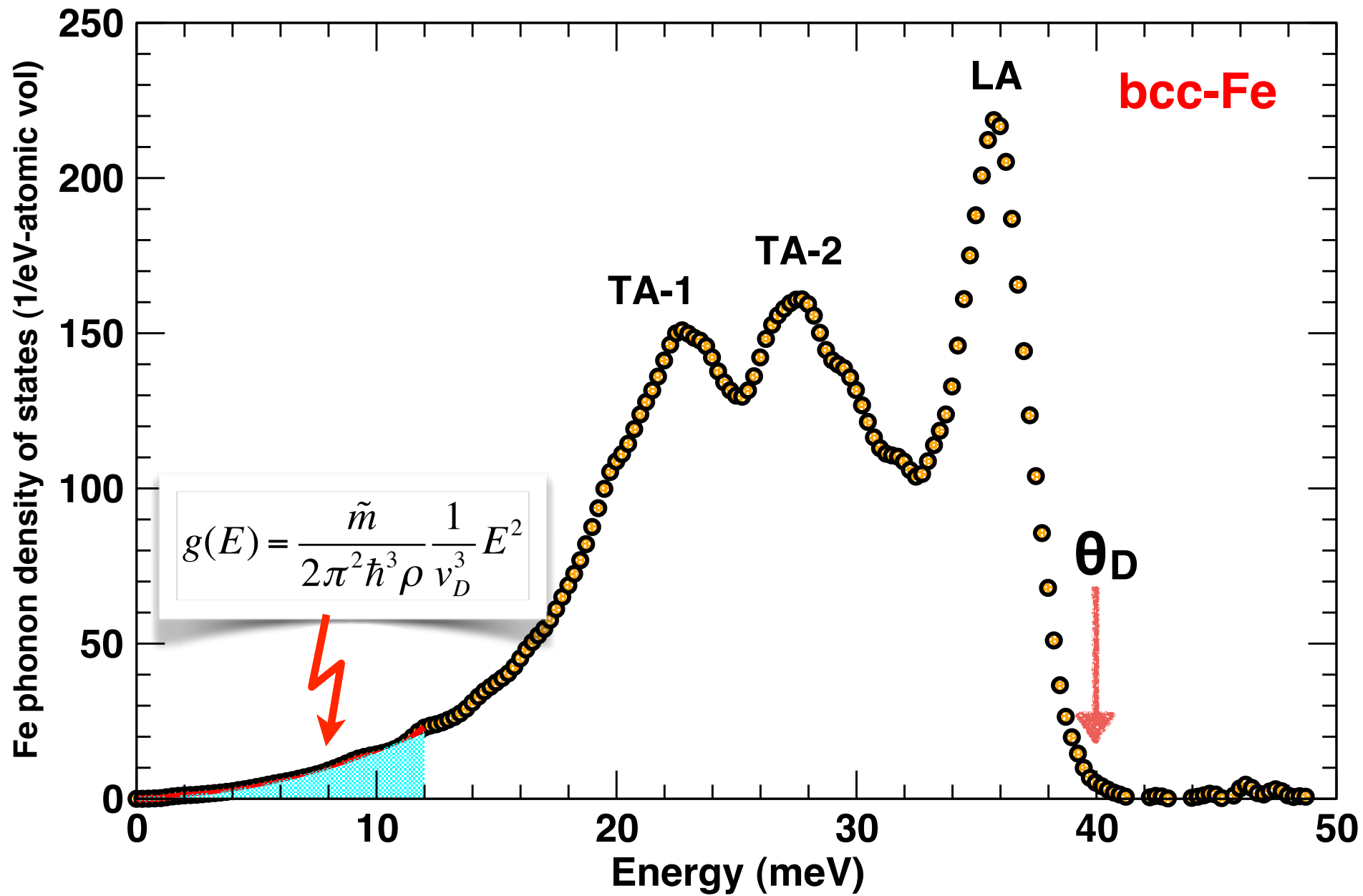


Detailed Balance

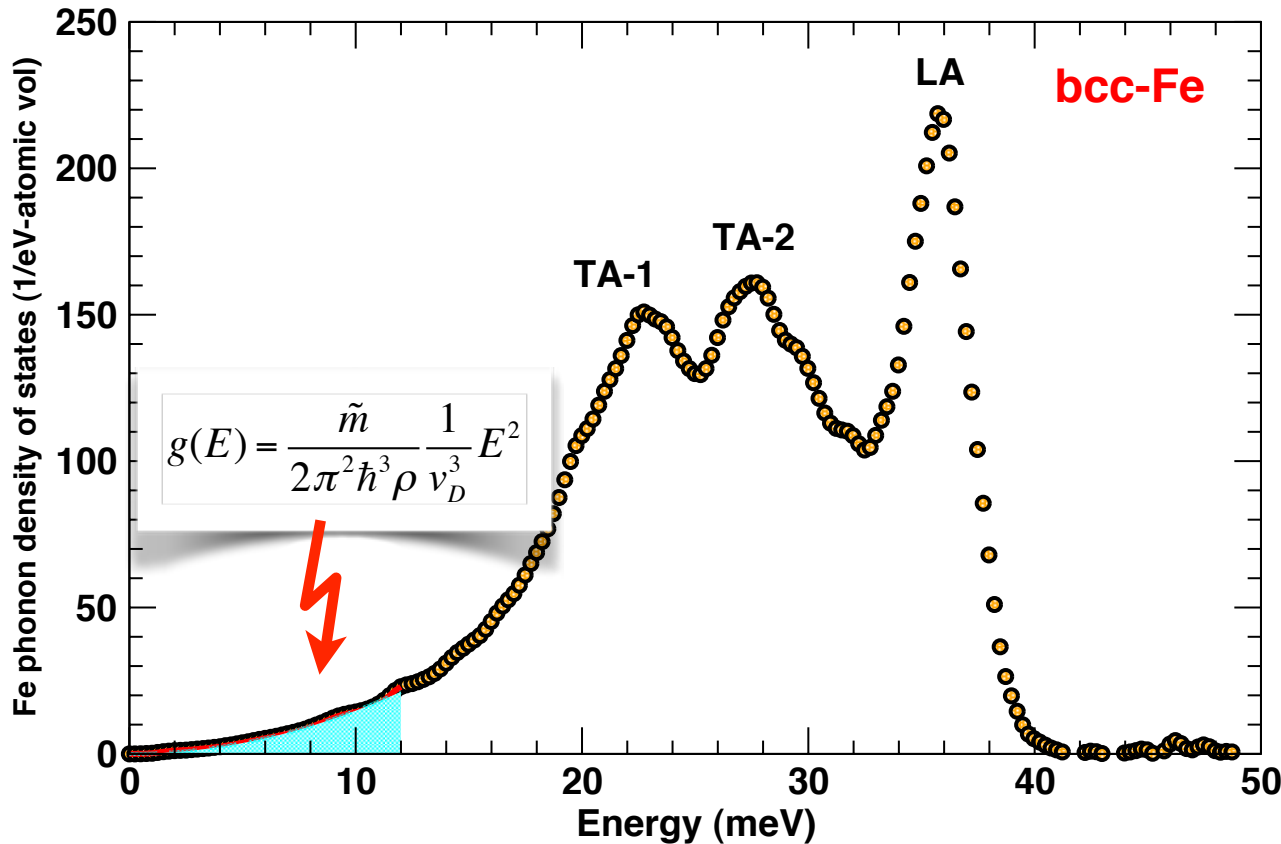


Temperature dependence of phonon excitation probability





Measurement of v_D , Debye sound velocity allows to resolve longitudinal and shear sound velocity, provided that bulk modulus and density, is independently and simultaneously measured by x-ray diffraction.



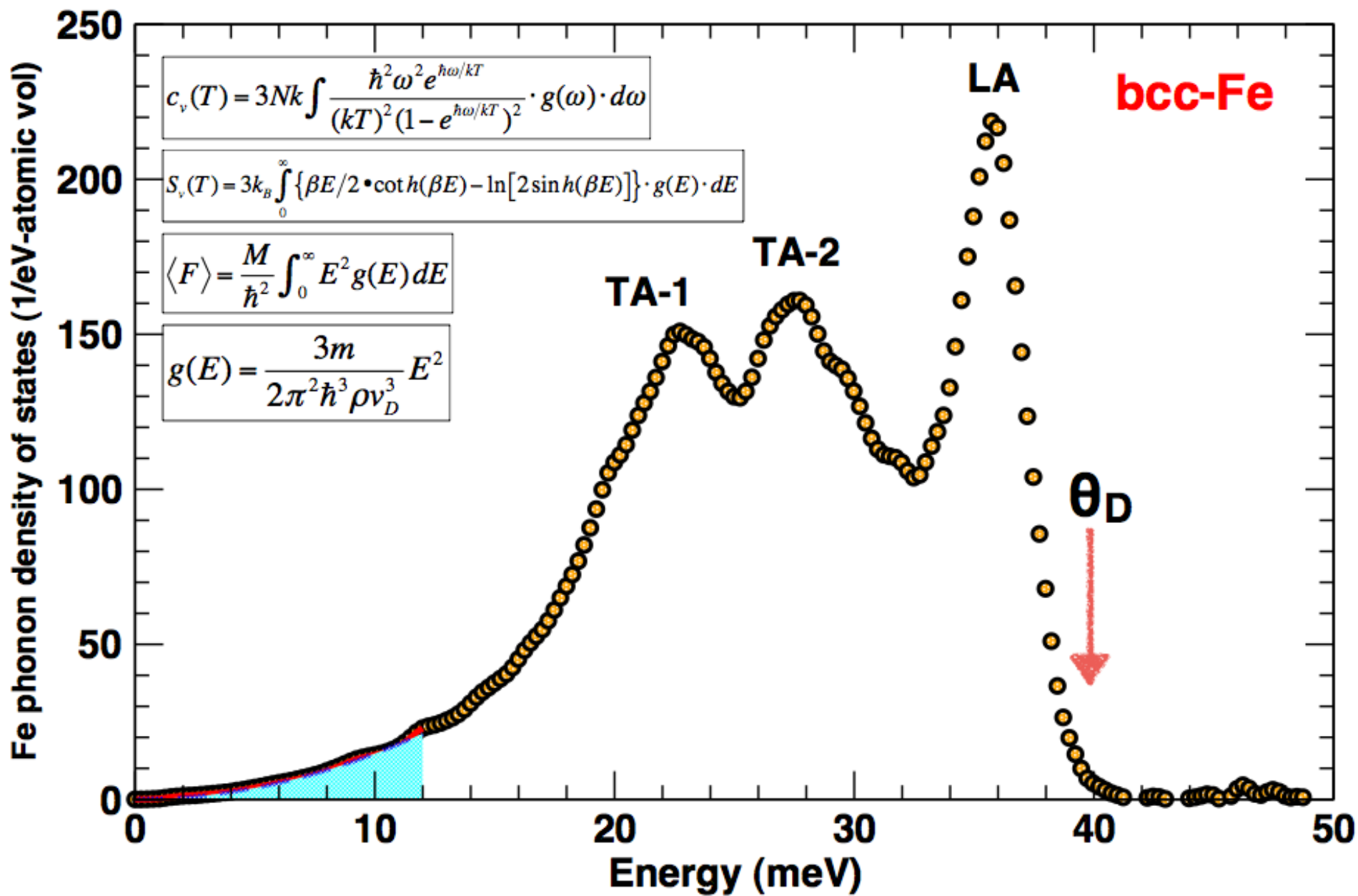
$$\frac{K_S}{\rho} = V_P^2 - \frac{4}{3}V_S^2$$

$$\frac{G}{\rho} = V_S^2$$

$$\frac{3}{V_D^3} = \frac{1}{V_P^3} + \frac{2}{V_S^3}$$

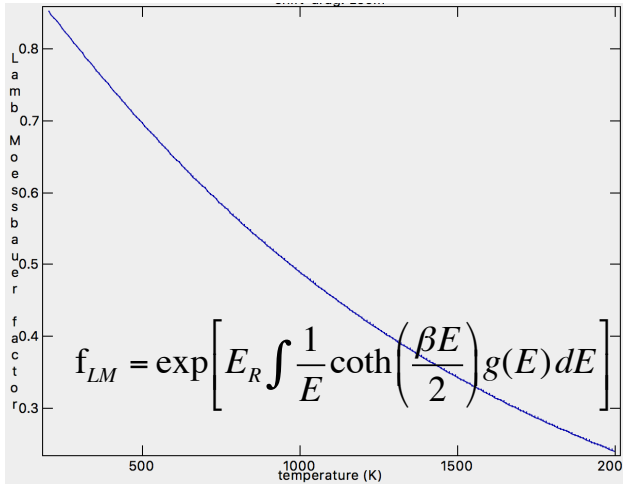
- K_S : adiabatic bulk modulus
- G : shear modulus
- V_P : compression wave velocity
- V_S : shear wave velocity
- V_D : Debye sound velocity
- ρ : density

K (GPa)	ρ (g/cc)	V_D (m/s)	V_P (m/s)	V_S (m/s)	G (GPa)
165 ± 1	8.01	3510 ± 12	5813 ± 13	3146 ± 11	79.3 ± 0.6

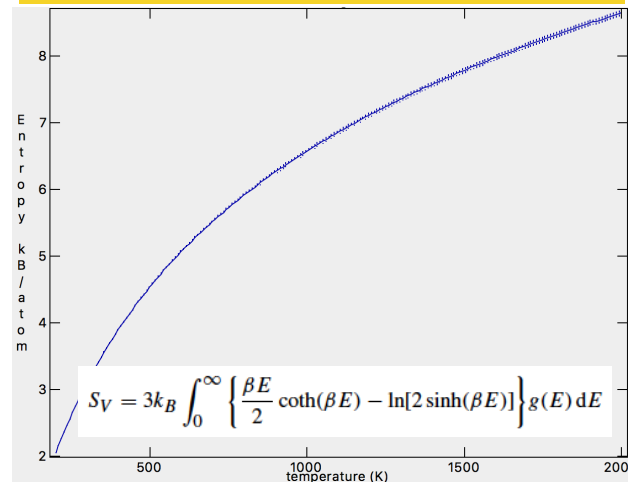


Thermodynamic properties as an additive function of phonon density of states

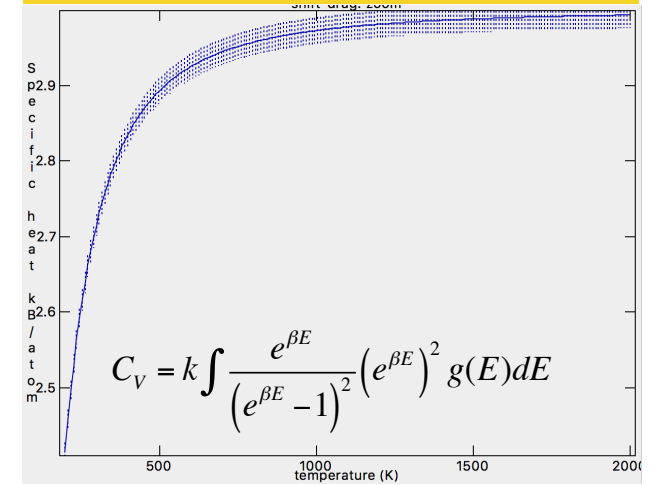
Lamb-Mössbauer factor



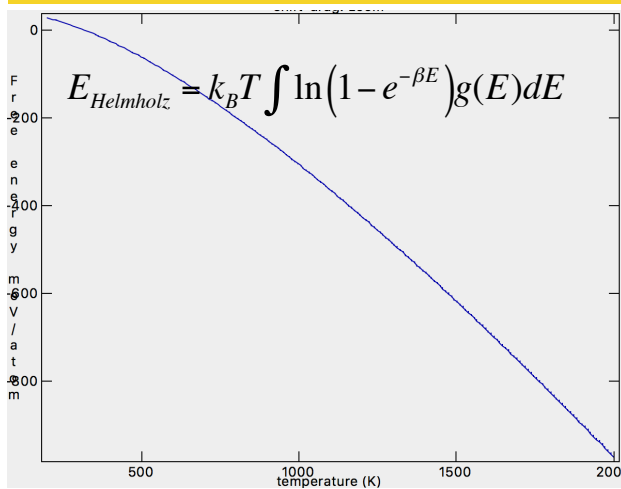
Vibrational entropy



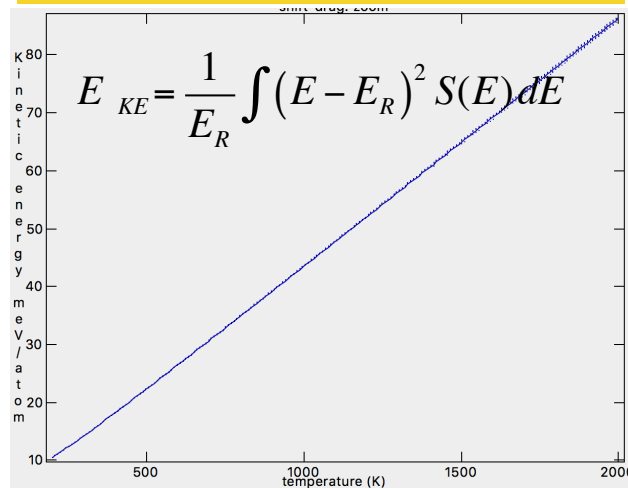
Specific heat



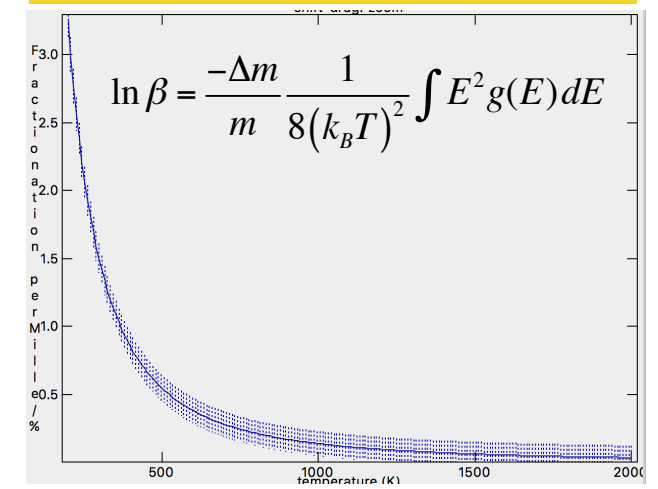
Helmholtz free energy



Kinetic energy



Isotope fractionation



Information from NRIXS spectra:

➤ directly from the data, $S(E)$

⇒ temperature

$$T = -\frac{E}{k_B} \ln \left[\frac{S(-E)}{S(E)} \right]$$

⇒ mean square displacement

$$\langle u^2 \rangle = -\frac{1}{k^2} \ln \left[1 - \int \{S(E) - S(0)\} dE \right]$$

⇒ kinetic energy

$$E_{kin} = \frac{1}{4E_R} \int (E - E_R)^2 S(E) dE$$

⇒ average force constant

$$D = \frac{k^2}{2E_R^2} \int (E - E_R)^3 S(E) dE$$

k ~ wave number of nuclear transition

E_R ~ recoil energy

ρ ~ mass density

➤ quasi-harmonic lattice model

⇒ partial phonon density of states

$$\mathcal{D}(E)$$

⇒ Debye sound velocity

$$v_D = \left(\frac{M}{2\rho\pi^2\hbar^3} \frac{E^2}{\mathcal{D}(E \rightarrow 0)} \right)^{1/3}$$

⇒ Grüneisen parameter

$$\gamma_D = \frac{1}{3} + \frac{\rho}{v_D} \left(\frac{\partial v_D}{\partial \rho} \right)_T$$

⇒ isotope fractionation

$$\ln \beta = -\frac{\Delta m}{M} \frac{1}{8(k_B T)^2} \int E^2 \mathcal{D}(E) dE$$

M ~ mass of resonant isotope

Δm ~ isotope mass difference

k_B ~ Boltzmann's constant

T ~ temperature

Phonon density of states

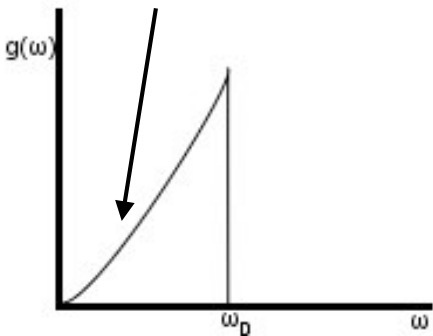
$$g(k) dk = \frac{V}{(2\pi)^3} 4\pi k^2 dk.$$

Number of wave vectors in a spherical shell of radius k per unit volume of reciprocal space.

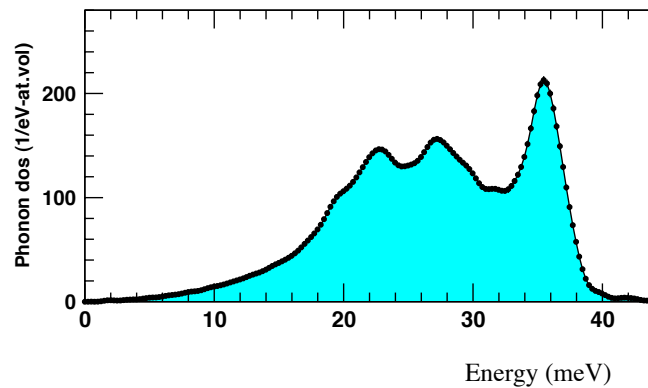
$$g(\omega) = \frac{3V}{2\pi^2 c^3} \omega^2$$

Phonon density of states has a quadratic dependence on frequency, and inversely proportional to the cube of sound velocity.

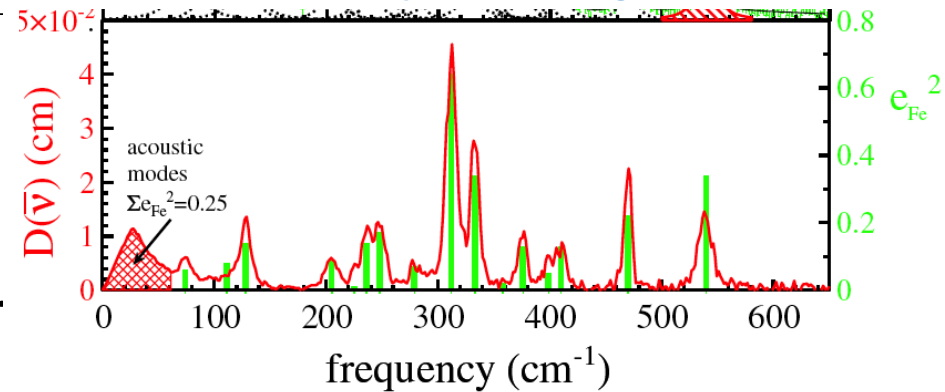
Debye model



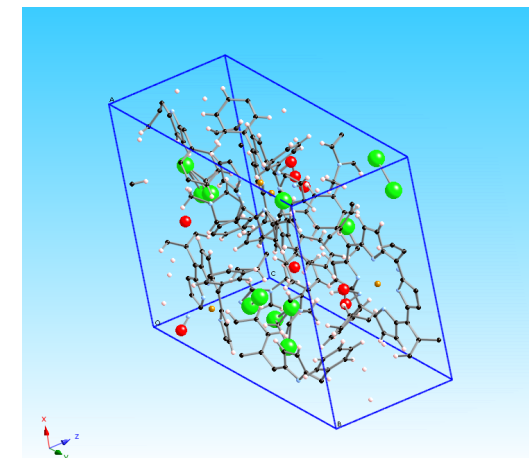
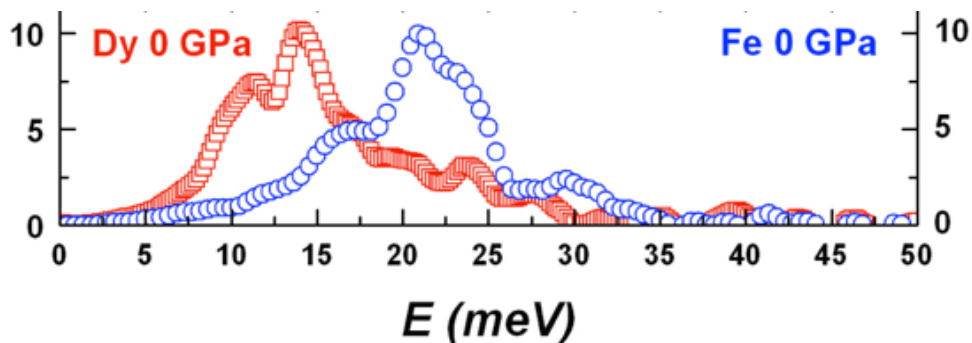
pure iron

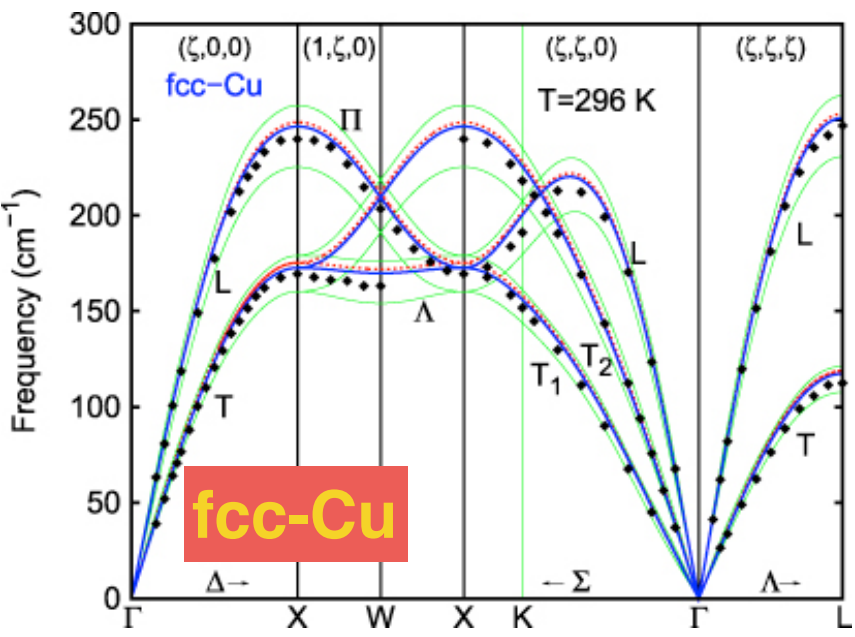
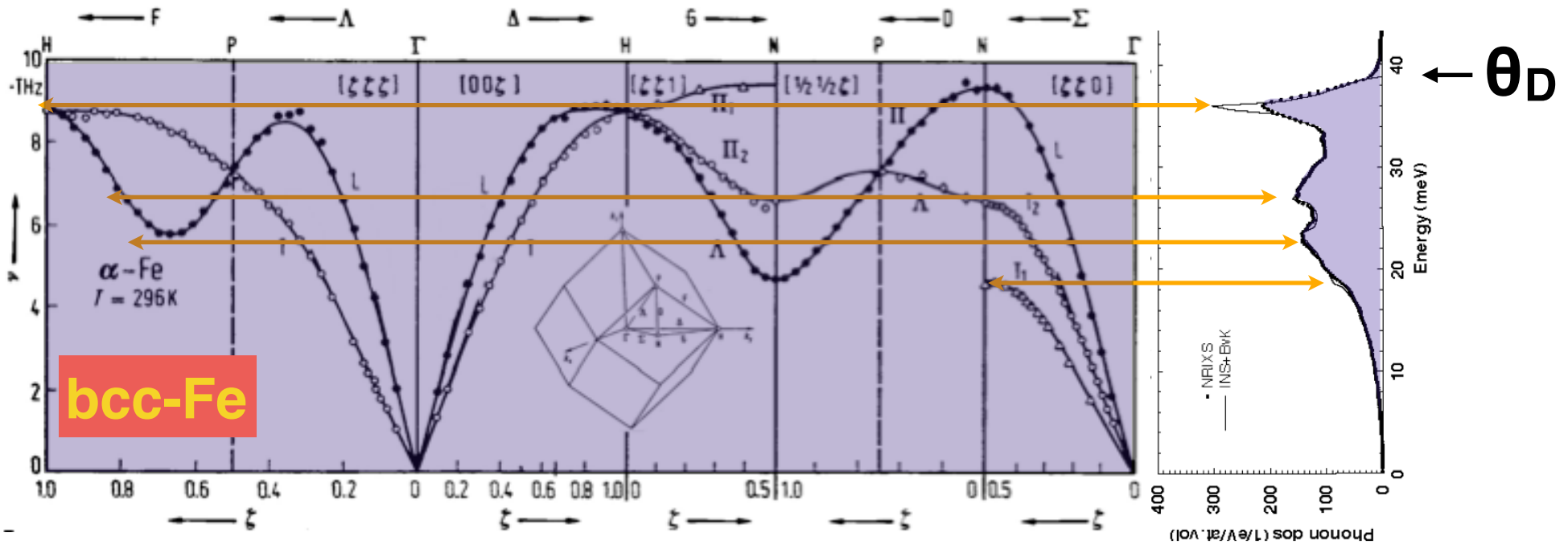


Fe-TPP-NO



DyFe₃

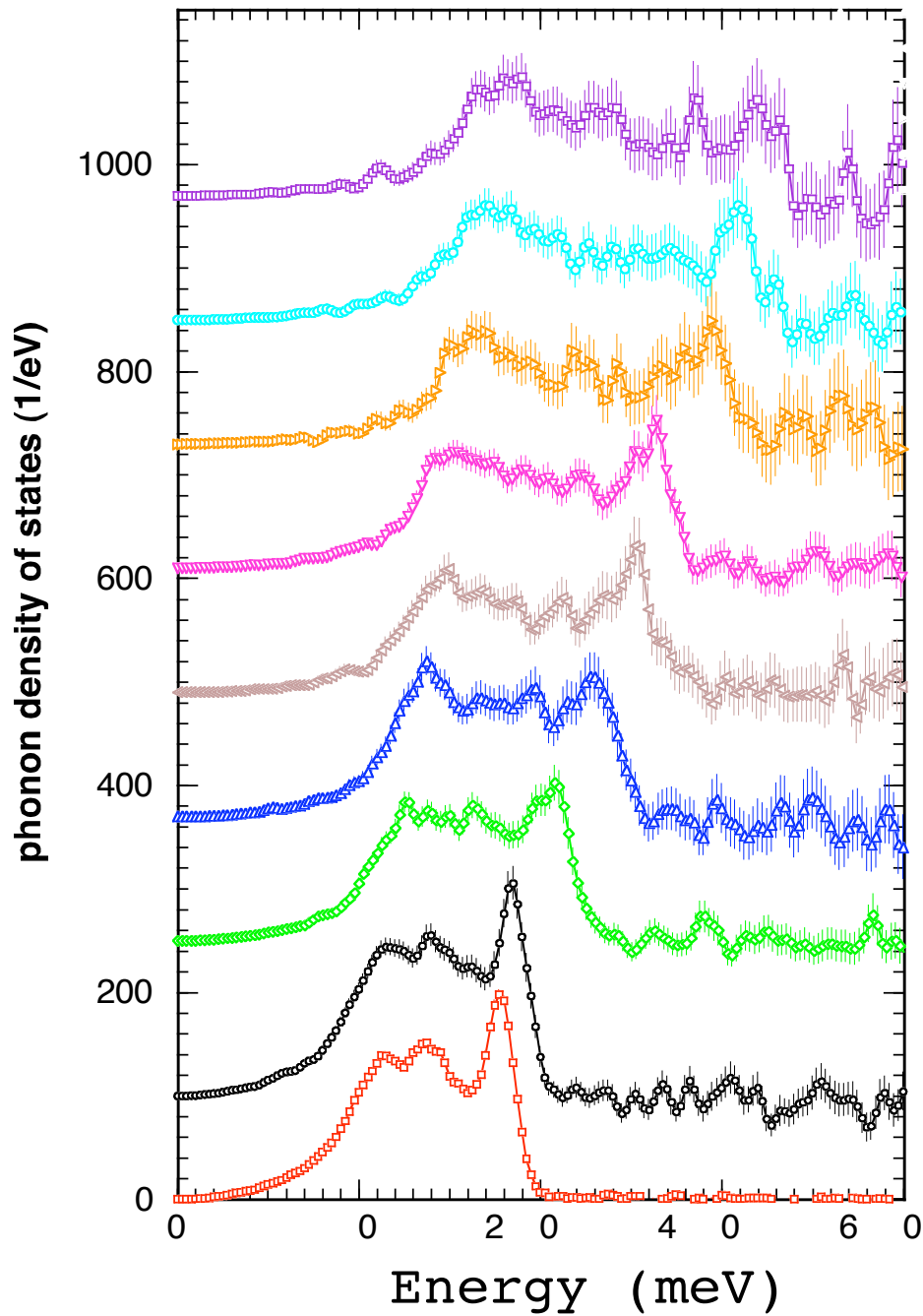




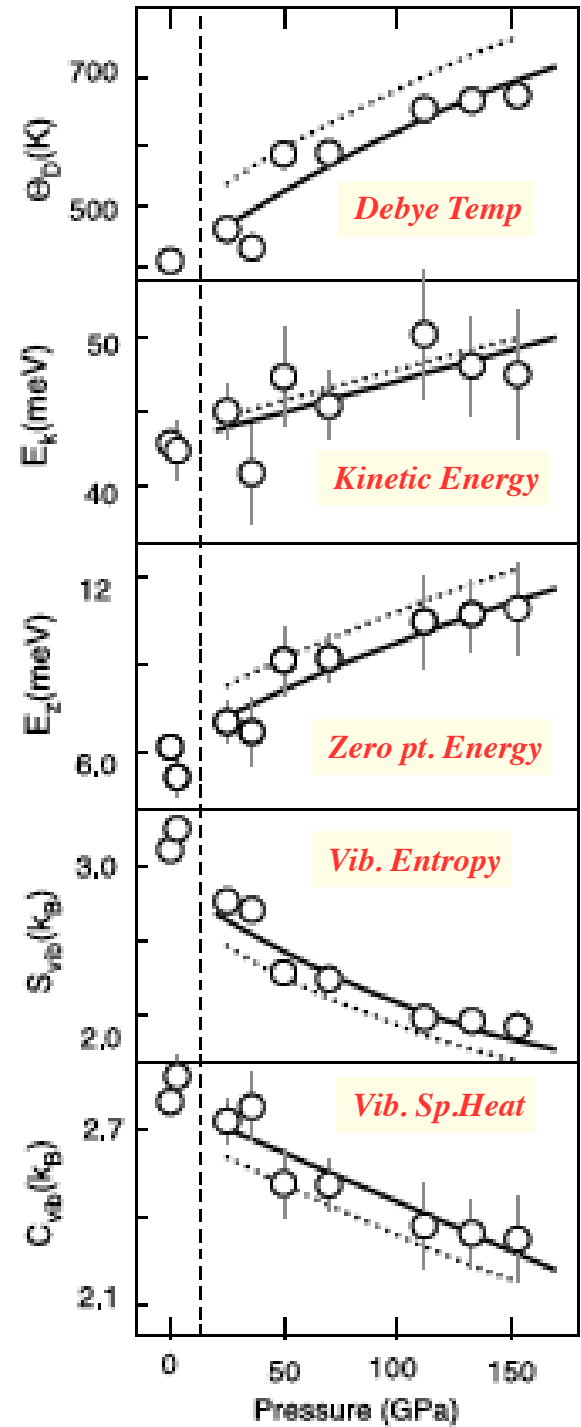
Let's assume that the acoustic modes have a linear relationship between frequency and wave vector:
 $\omega = ck$, where \mathbf{c} is average sound velocity

Maximum frequency cut off is at Debye energy:
 e.g. for Cu, this frequency is 240 cm^{-1} ($\sim 30 \text{ meV}$).
 Considering $1 \text{ meV} = 11.605 \text{ K} = 8.065 \text{ cm}^{-1}$, this corresponds to 348 K , which is close to 344 K .
 For Fe, the measured cut-off value is $\sim 39.5 \text{ meV}$, which corresponds to 458 K , very close to reported 460 K .

Phonon density of states of iron under high pressure



153 GPa

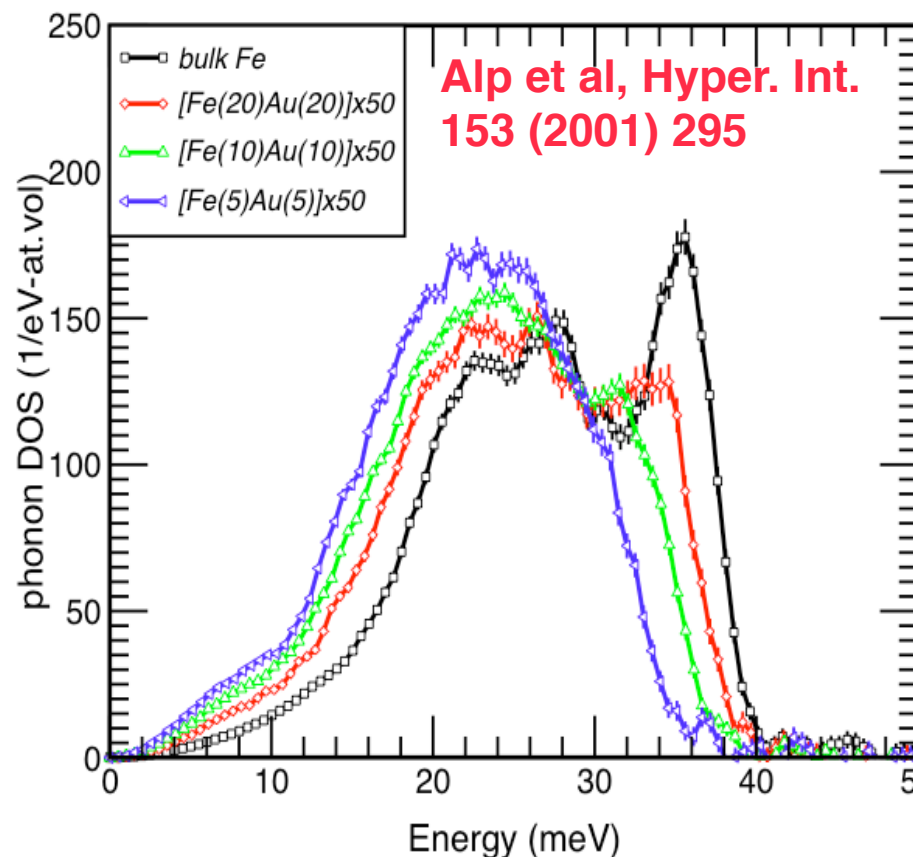
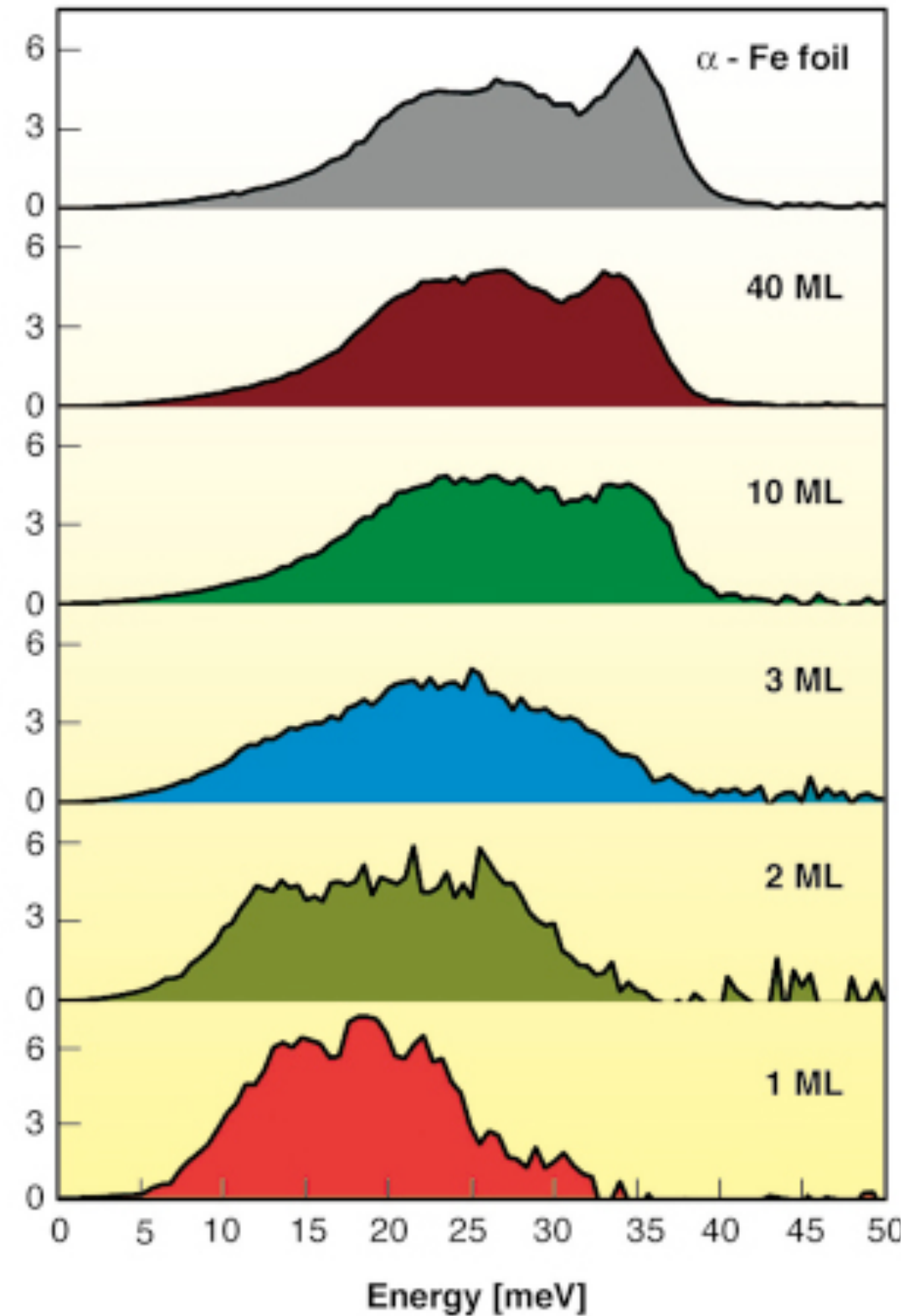


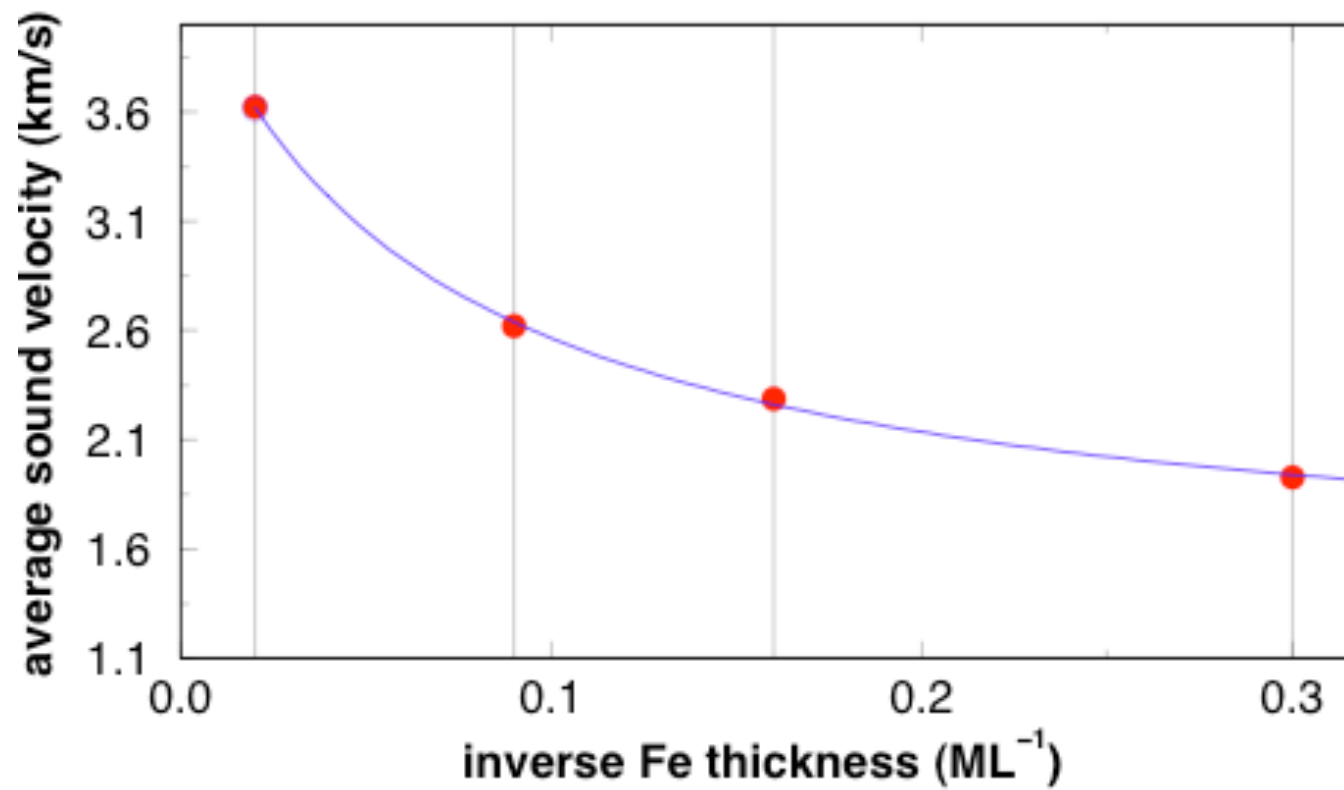
Fe films deposited on W(110)

Transition from the bulk to a single iron monolayer

S. Stankov, R. Röhlberger, T. Slezak, M. Sladeczek, B. Sepiol, G. Vogl, A. I. Chumakov, R. Ruffer, N. Spiridis, J. Lazewski, K. Parlinski, and J. Korecki,

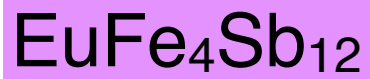
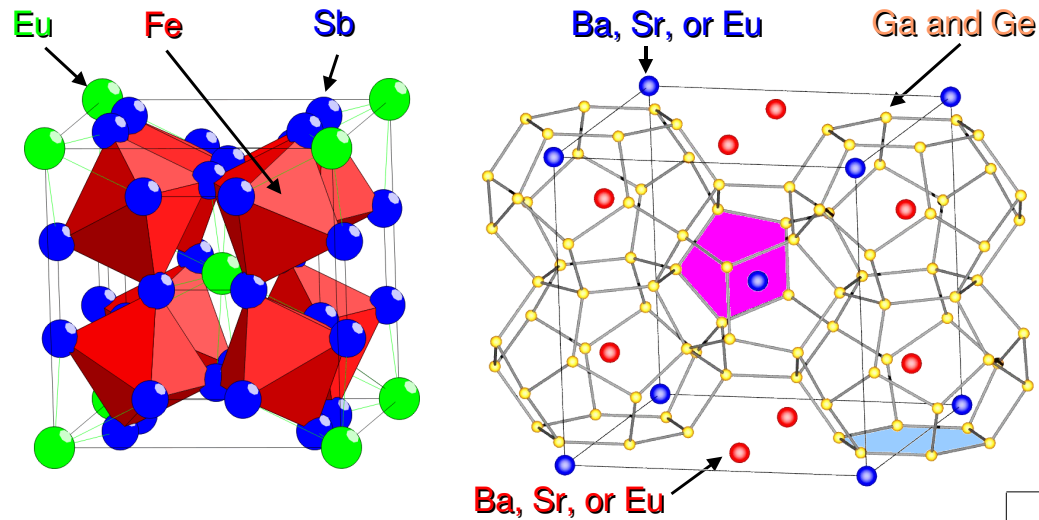
ESRF Highlights 2006





1. Thermoelectric materials: always something new !..

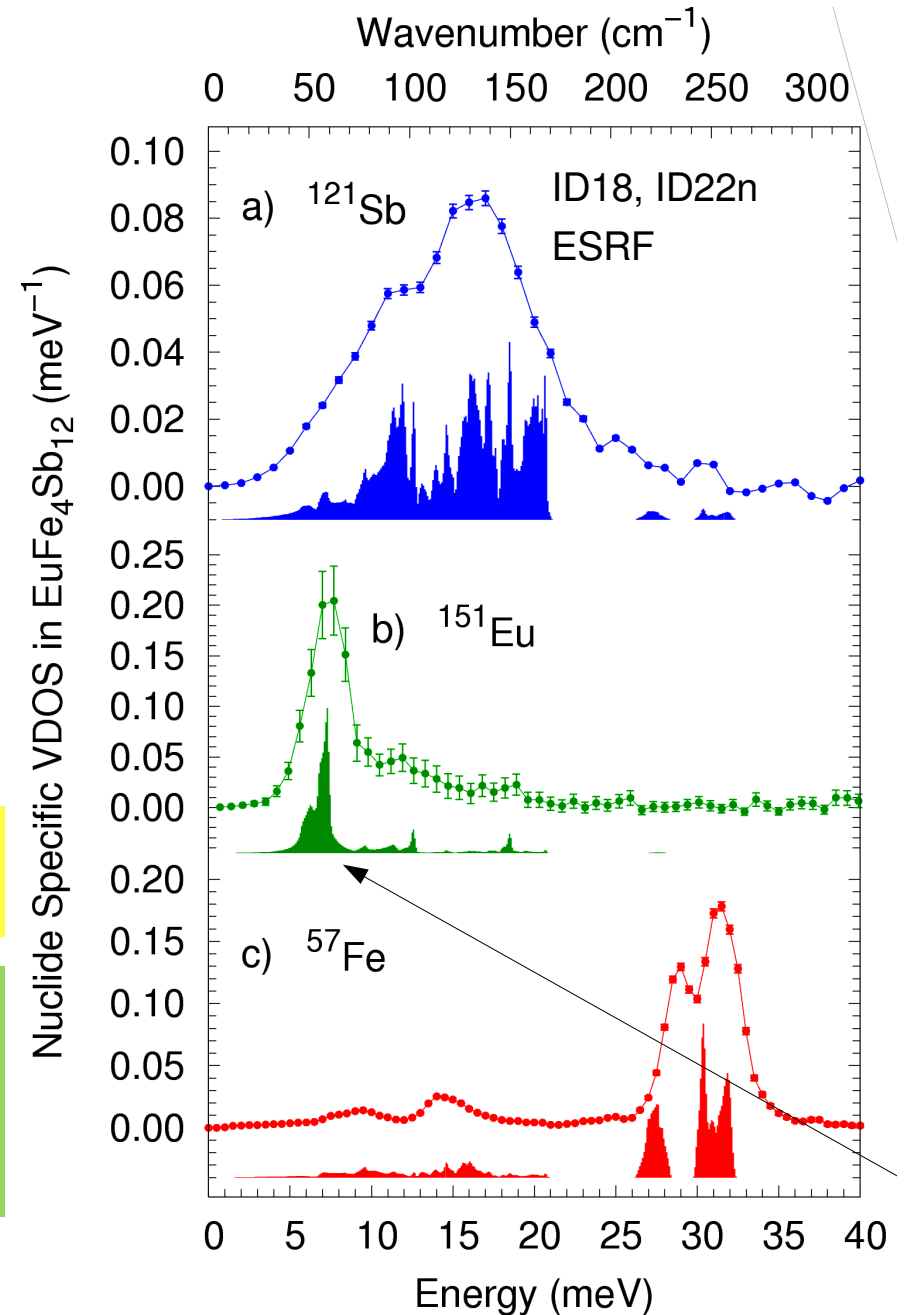
Skutterudites



The loosely bound guests affect the characteristics of the vibrations, and change the thermal conductivity

Many elements in modern thermoelectric materials include **Fe**, rare-earth atoms like **Eu, Sm, Dy**, as well as **Sb**, and **Te**. These are all proper Mössbauer resonances we can exploit, and we do..

Wille, et al, PRB 76 (2007) 140301



Vibrational dynamics of the host framework in Sn clathrates

Bogdan M. Leu,^{1,*} Mihai Sturza,² Michael Y. Hu,¹ David Gosztola,³ Volodymyr Baran,⁴ Thomas F. Fässler,⁴ and E. Ercan Alp¹

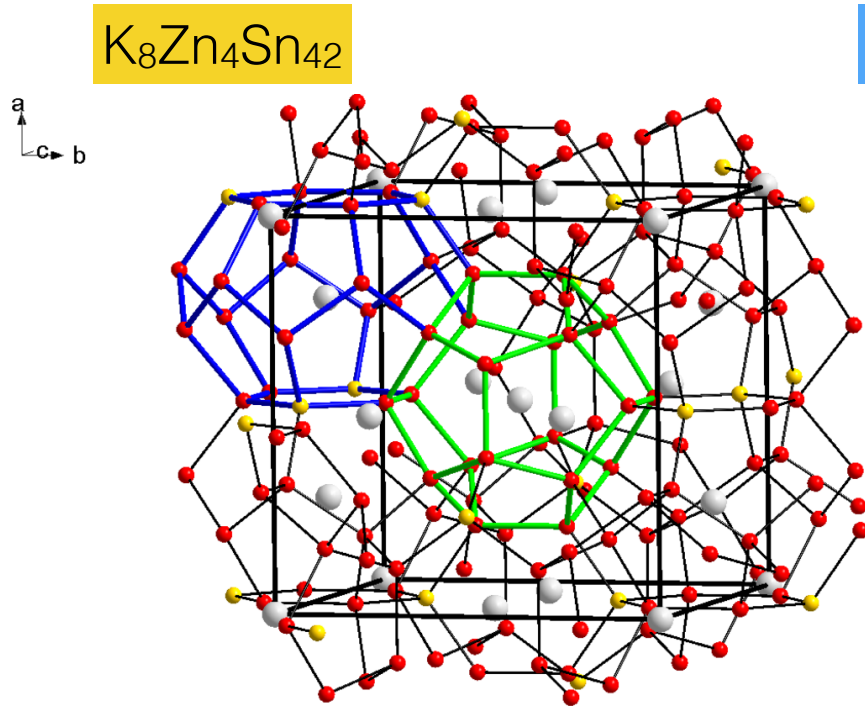


FIG. 1. (Color online) Structure of type-I clathrate $K_8Zn_4Sn_{42}$. Color scheme: gray = K, yellow = Zn/Sn, red = Sn. One small (pentagonal dodecahedron) and large (tetrakaidecahedron) host framework cage are highlighted in green and blue, respectively.

type-I clathrate: pentagonal dodecahedra and tetrakaidecahedra alternating in a 1:3 ratio

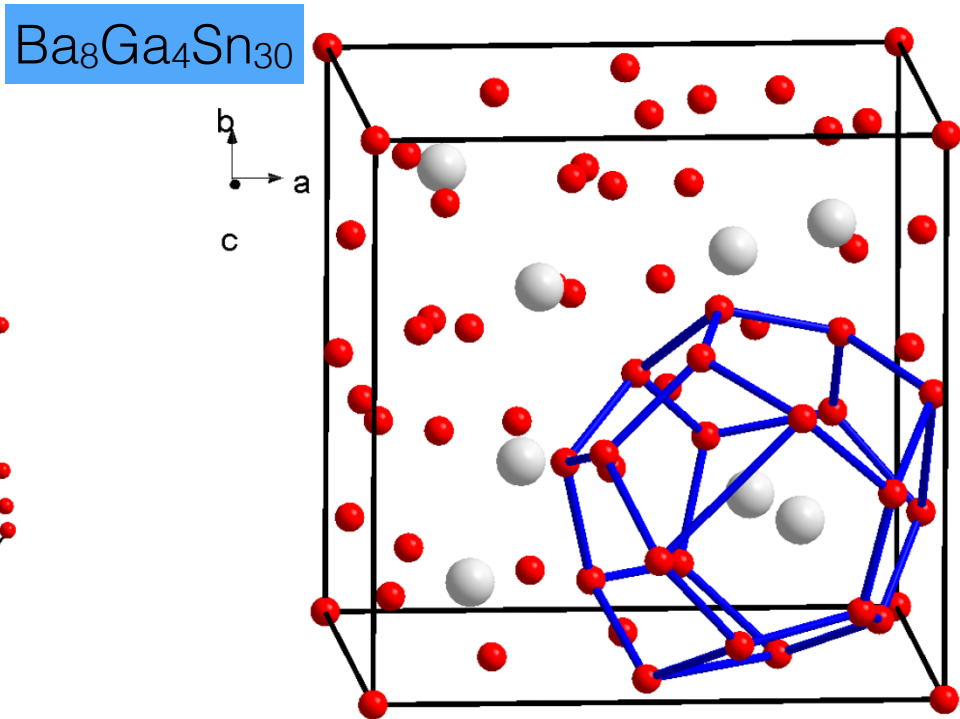
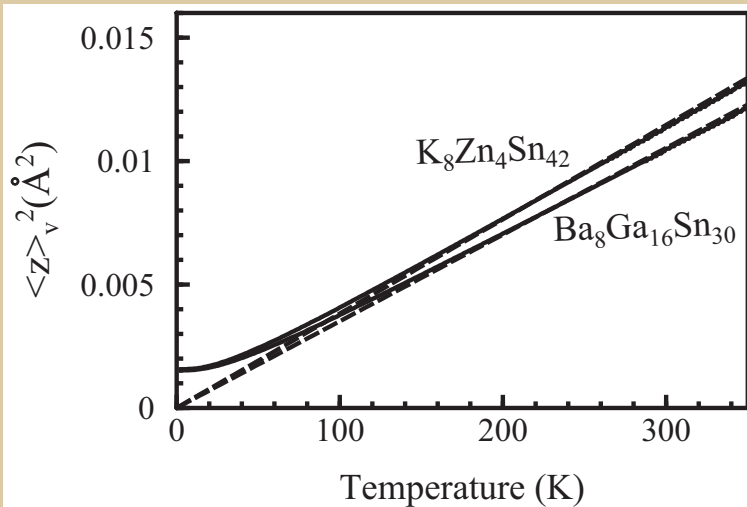
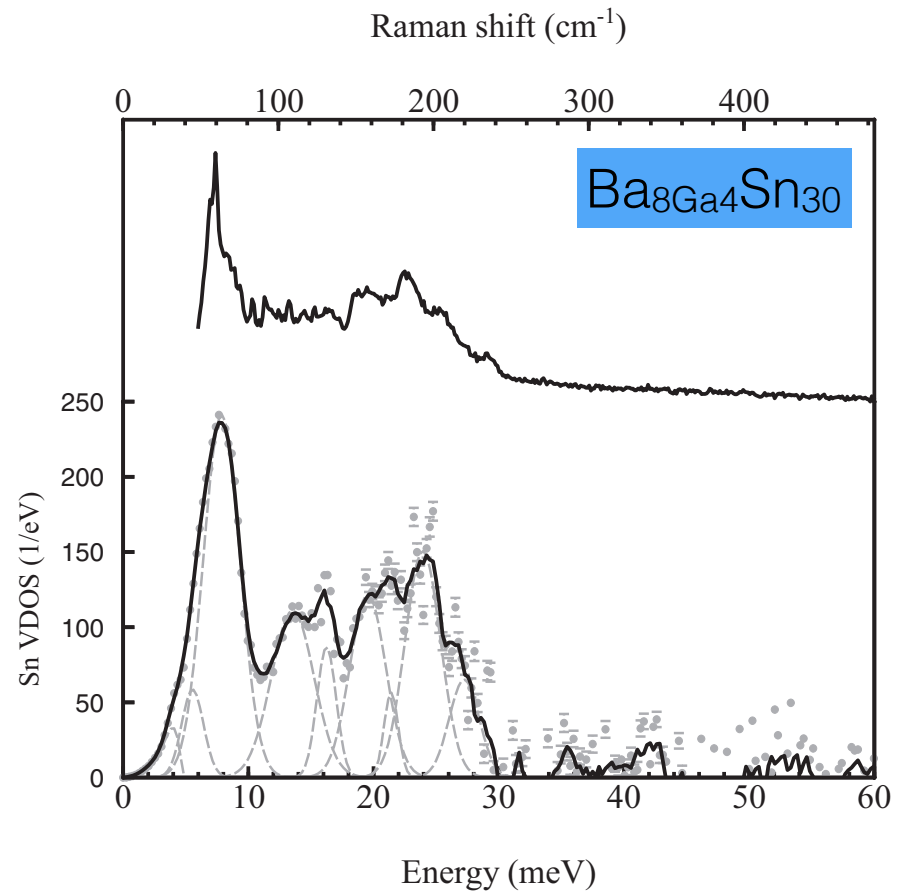
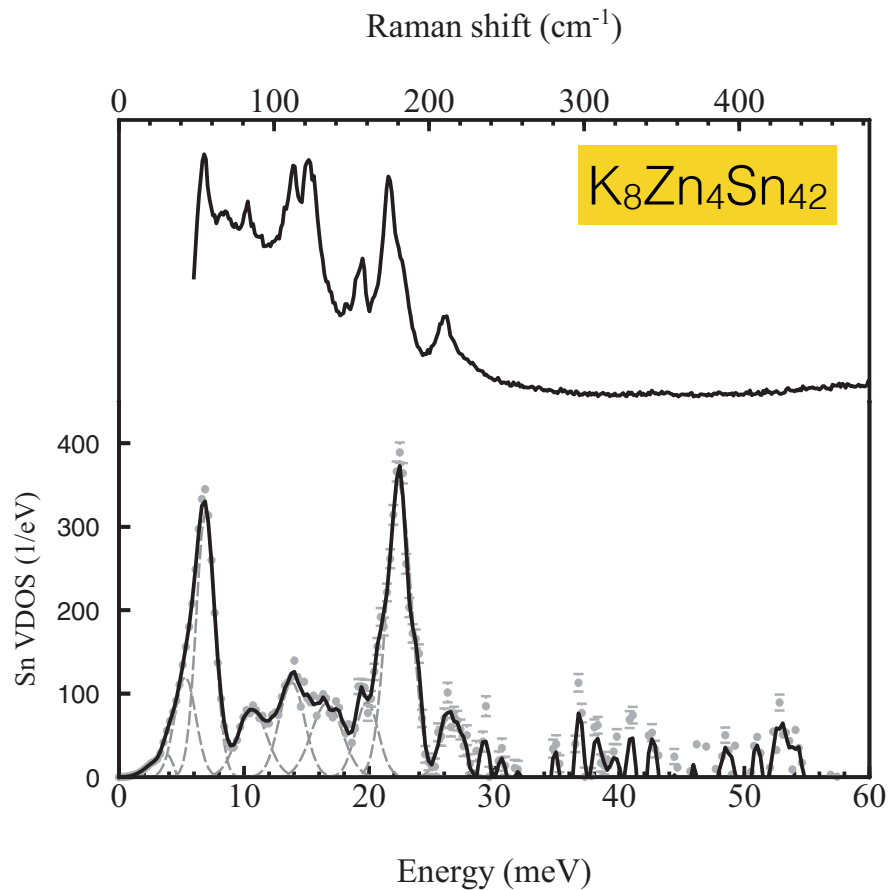


FIG. 2. (Color online) Structure of type-VIII clathrate $Ba_8Ga_4Sn_{30}$. Color scheme: gray = Ba, red = Sn/Ga. One host framework cage (pentagonal dodecahedron) is highlighted in blue.

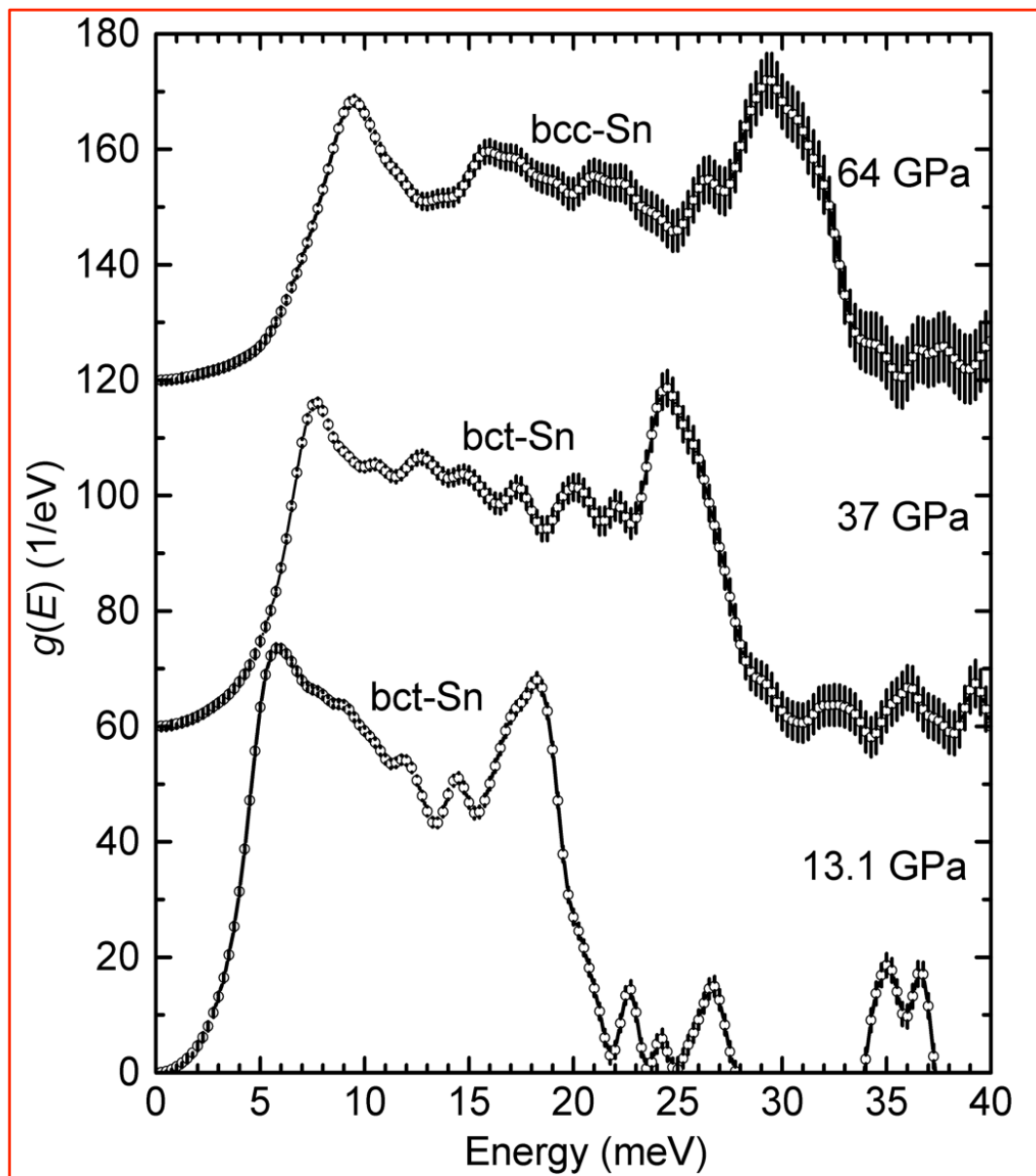
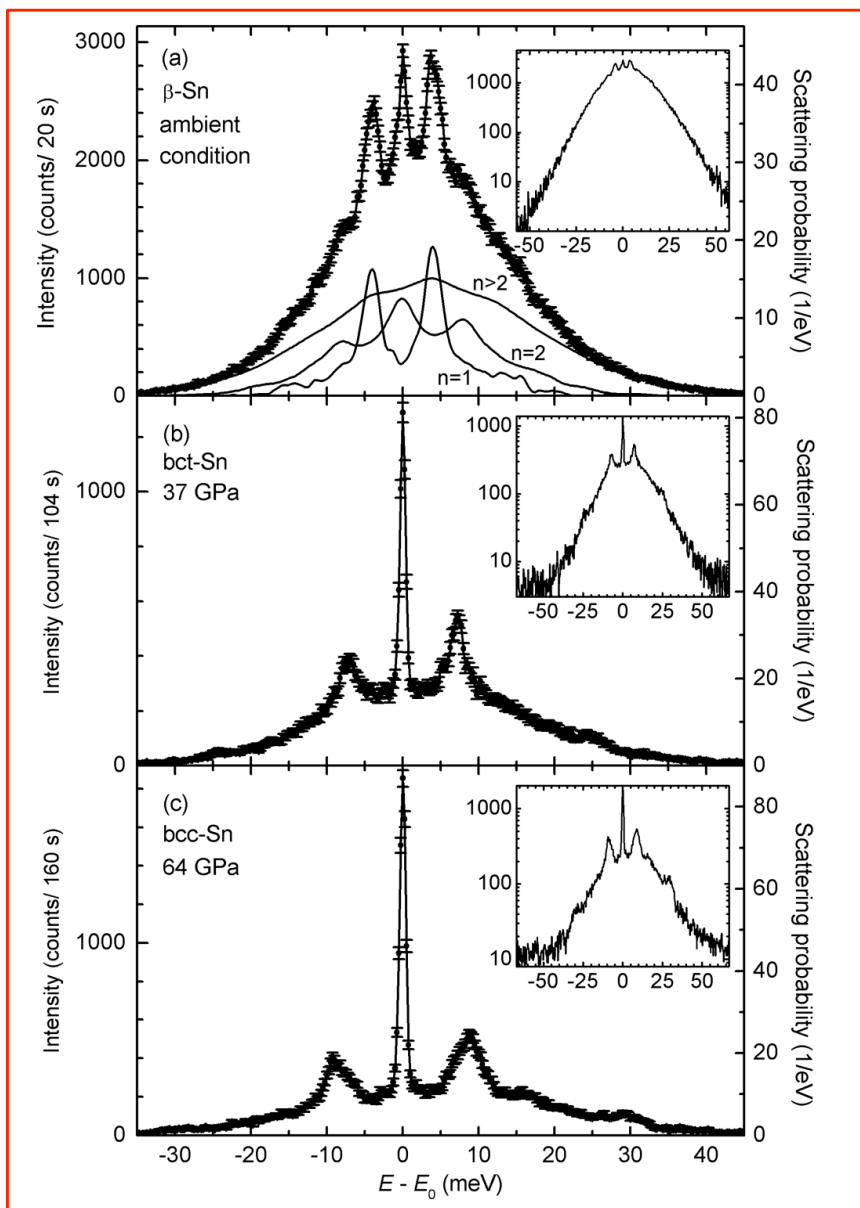
type VIII : pentagonal dodecahedra; however, BGS adopts the type-I clathrate structure at high-temperature



mean square displacement via phonon dos

$$\langle z^2 \rangle_v = \frac{1}{3k^2} \int [2\bar{n}(\bar{\nu}) + 1] \frac{\bar{\nu}_R}{\bar{\nu}} D(\bar{\nu}) d\bar{\nu},$$

3.8×10^{-5} Å²/K for KZS and 3.5×10^{-5} Å²/K for BGS.



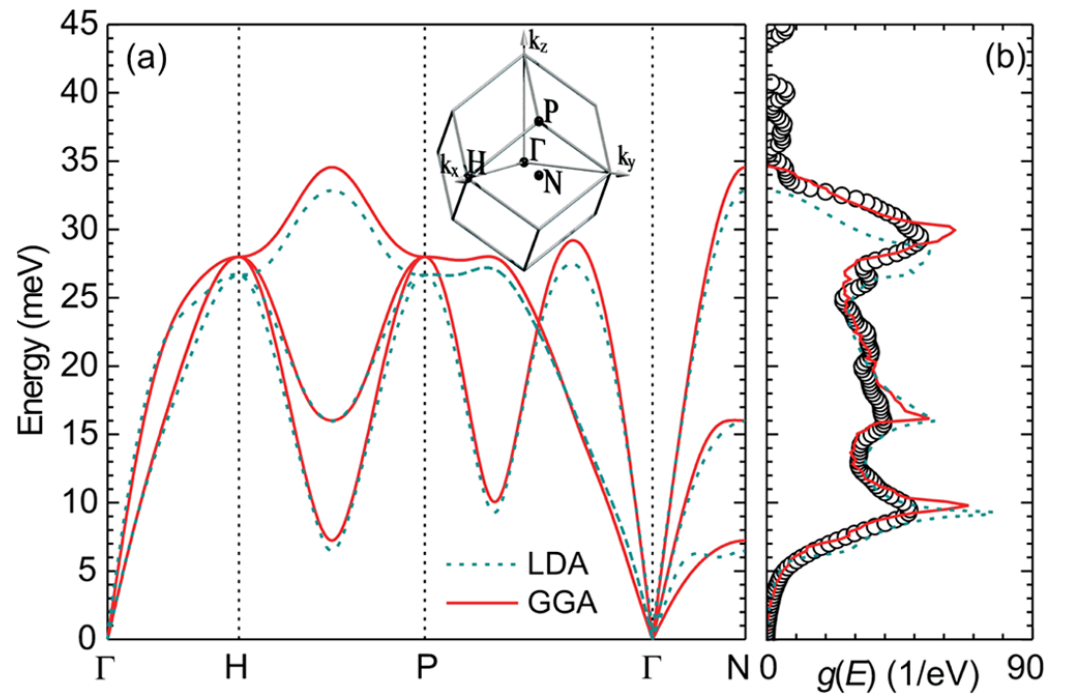
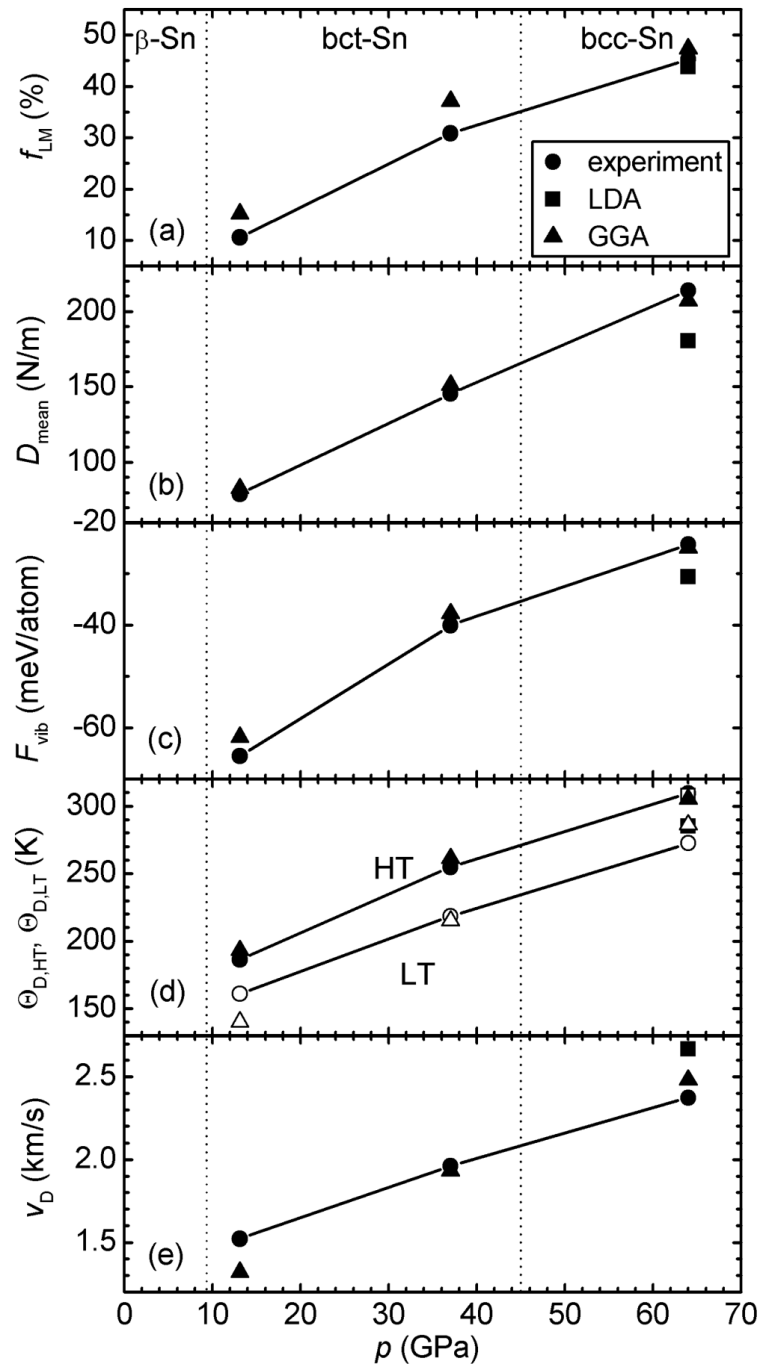
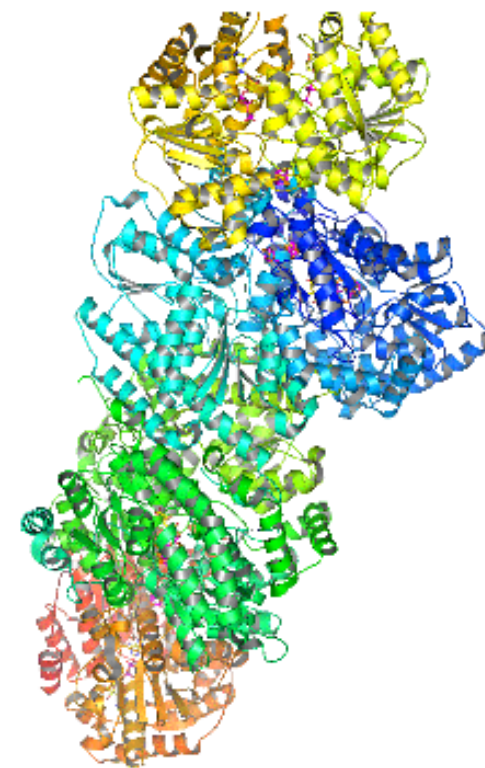
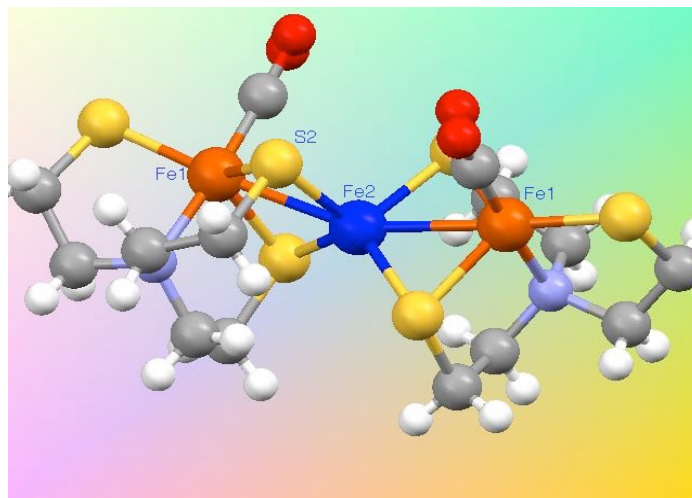
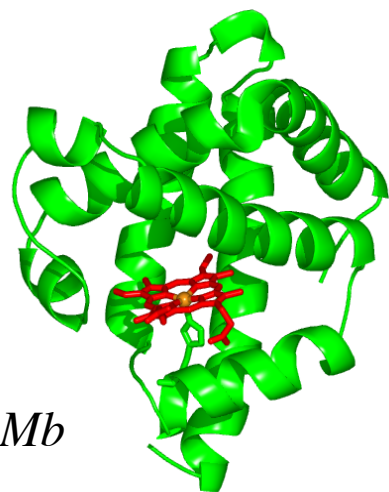


FIG. 3 (color online). (a) Theoretical phonon dispersion relation of bcc-Sn at 64 GPa. The inset shows the Brillouin zone of the bcc-Sn lattice. (b) Comparison between the theoretically calculated phonon DOS (lines) and the experimentally derived phonon DOS at 64 GPa (circles).

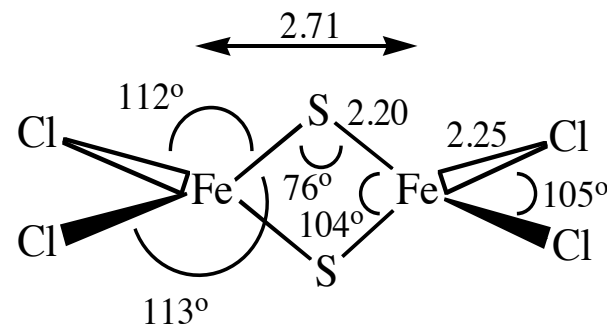
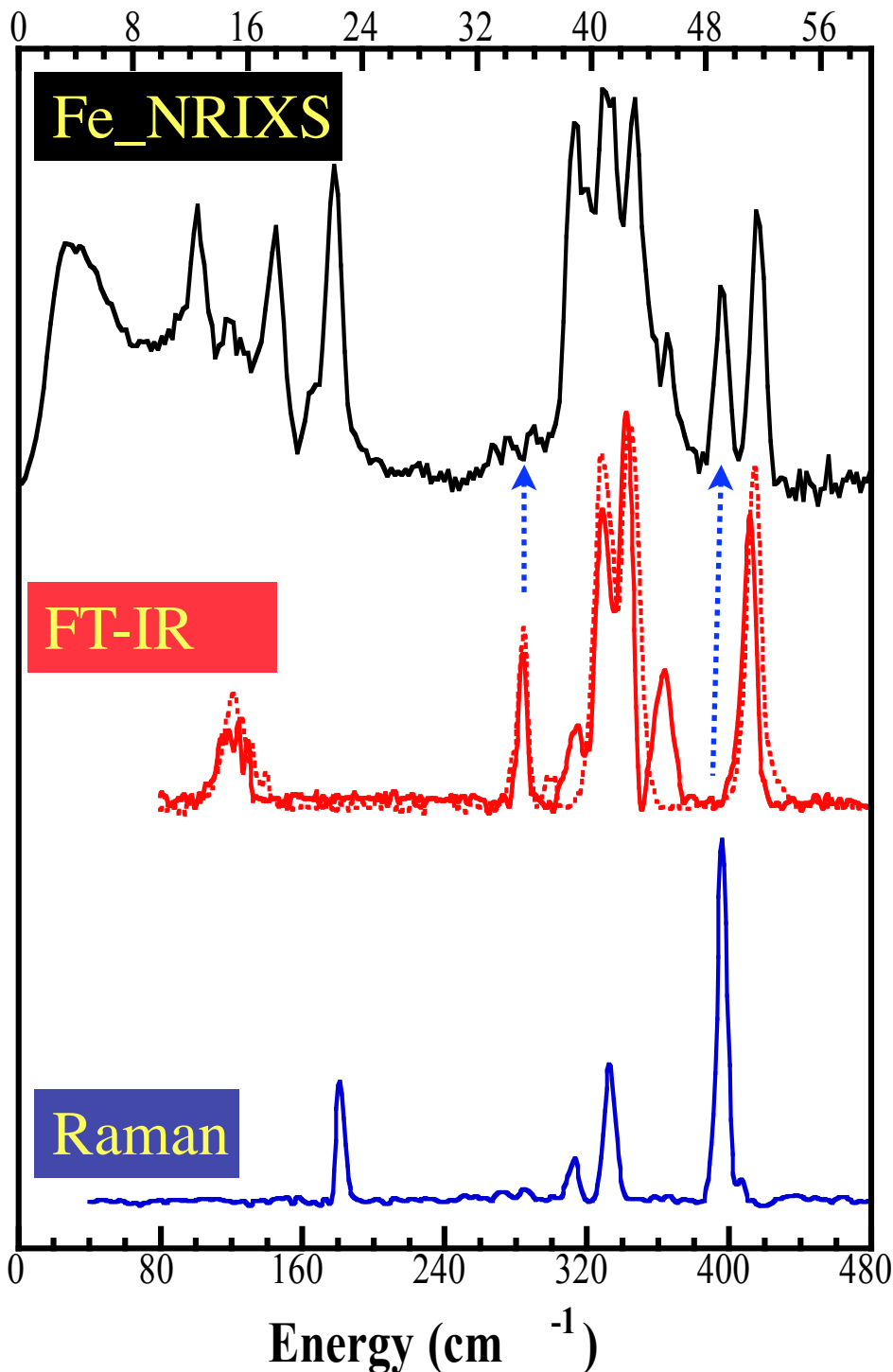
Biology & bio-inorganic chemistry

S. Cramer	University of California-Davis
E. Solomon	Stanford University
T. Sage	Northeastern University
E. Munck	University of Pittsburg
DeBeer George	Cornell University
Nicolai Lehnert	University of Michigan
R. Scheidt	University of Notre Dame



Vibrational spectroscopy of proteins, enzymes and biomimic model porphyrins and cubanes

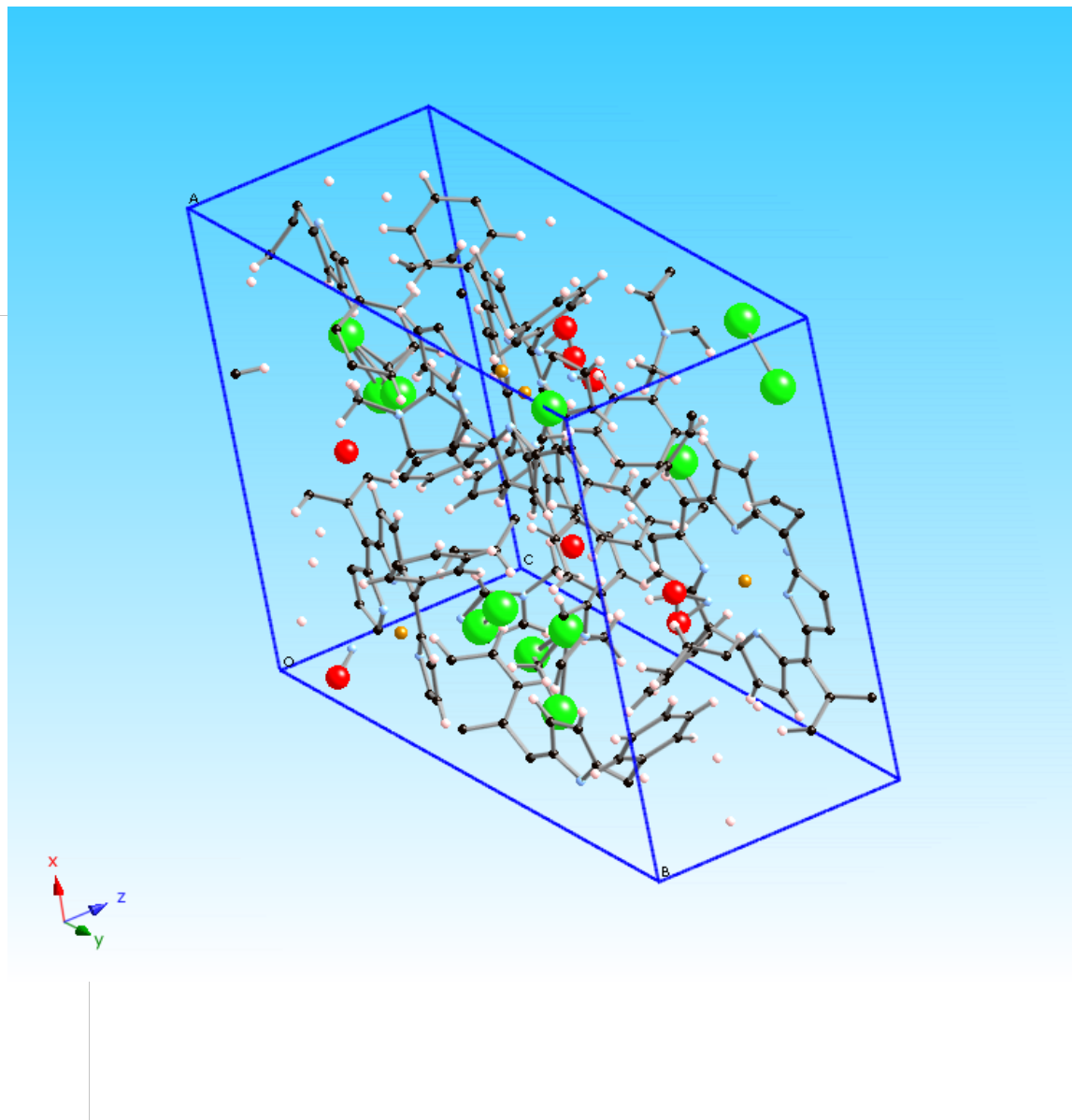
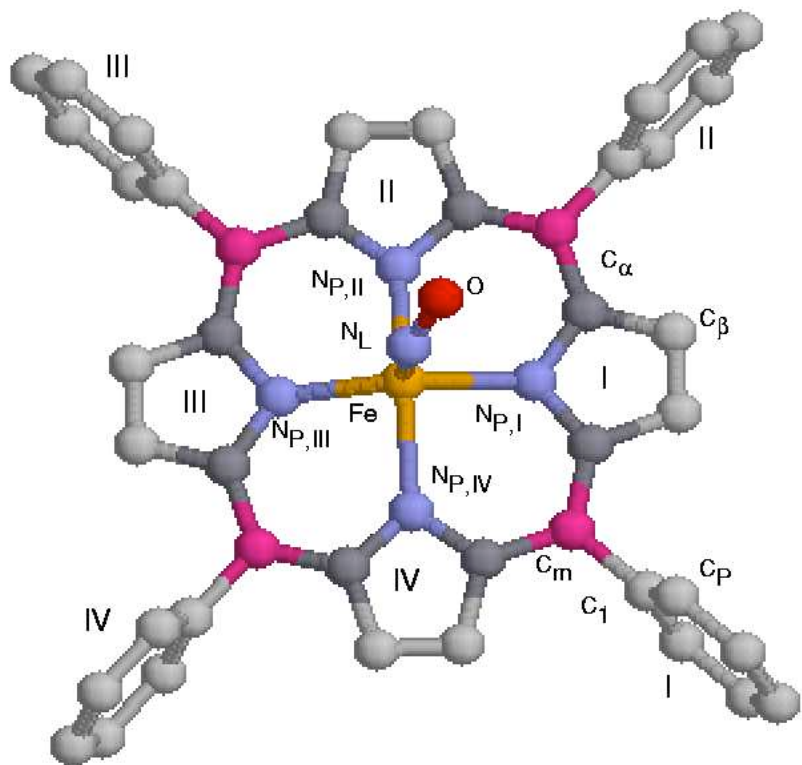
Energy (meV)



Some unique advantages of NRIXS

1. Low frequency motions: ~ total mass
2. No selection rule except motion of atoms along x-ray propagation
3. Peak intensity ~ mode participation ~ actual displacement
4. No matrix effects or limitations
5. Element and isotope selective
6. No unpredictable cancellations in scattering terms

$$\phi_{\alpha} = \frac{1}{3} \frac{\bar{v}_R}{\bar{v}_{\alpha}} e^{2j_{\alpha}} (\bar{n}_{\alpha} + 1) f$$

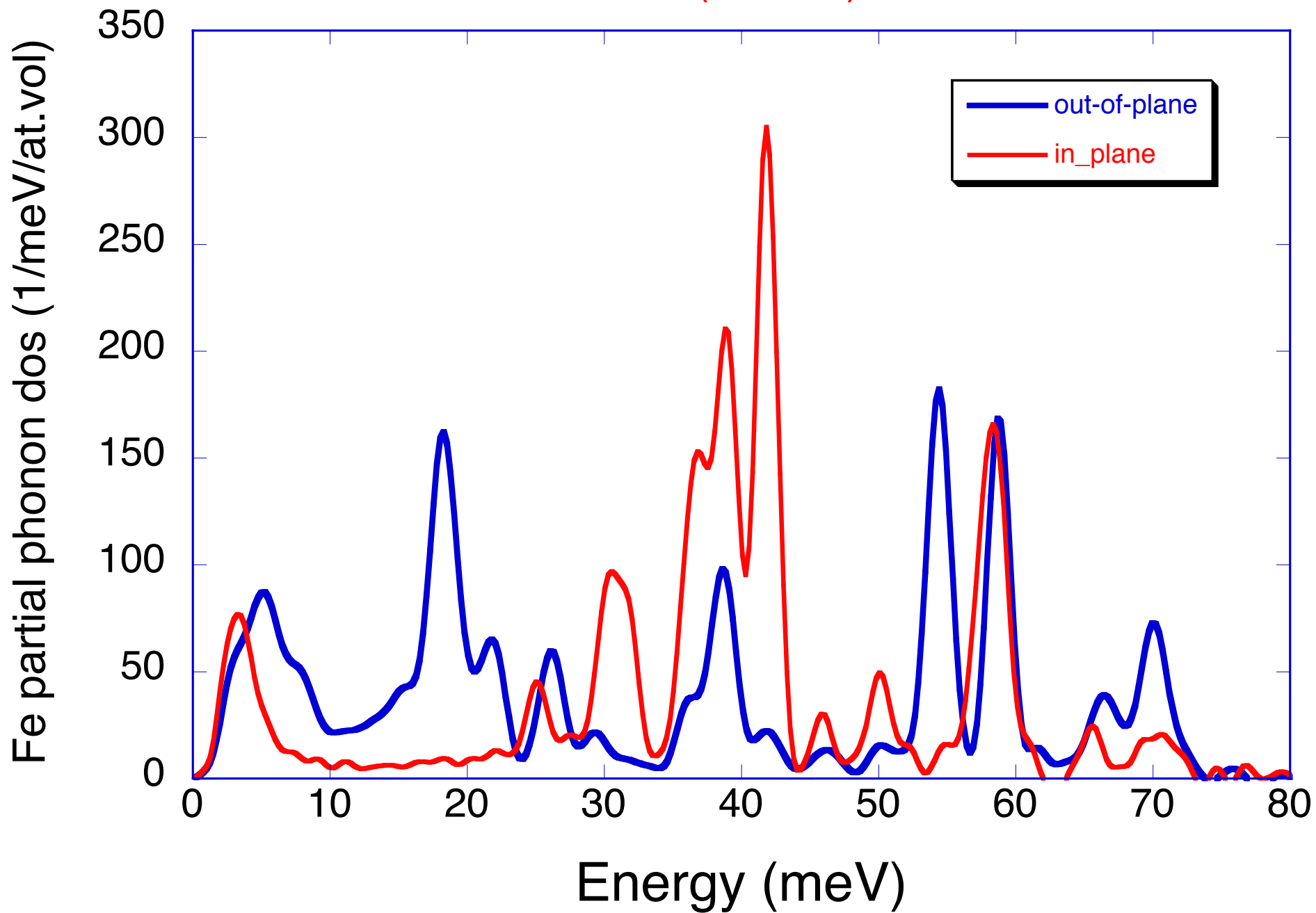


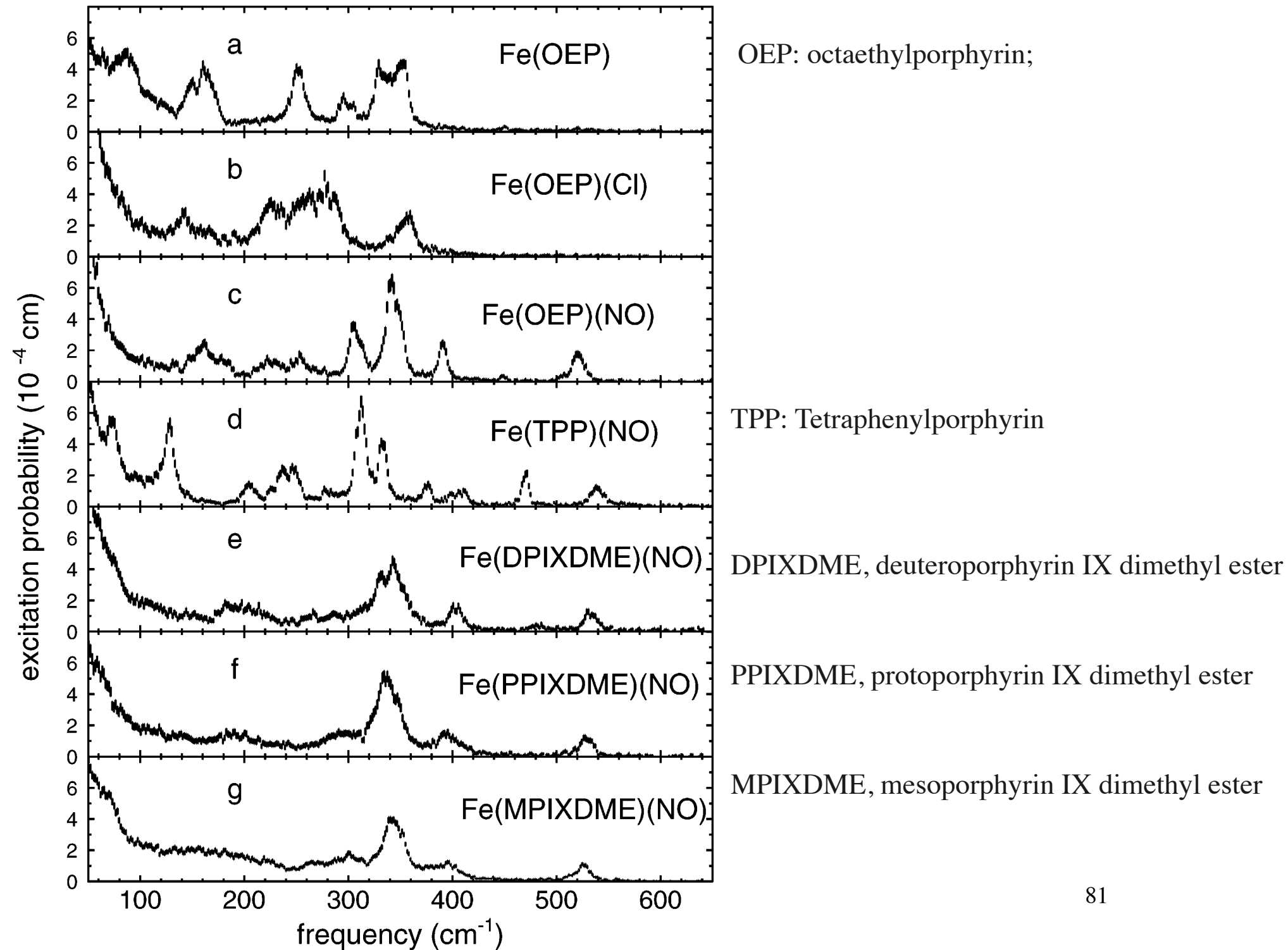
Porphyrins:

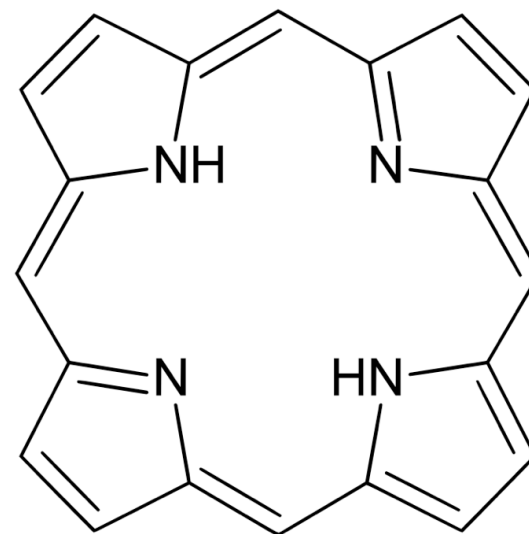
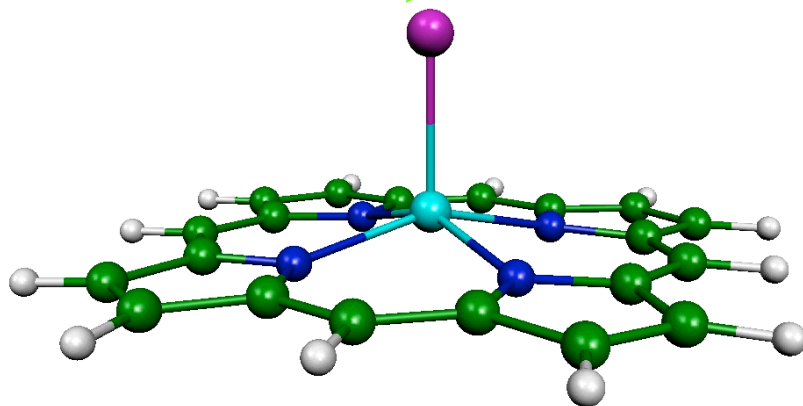
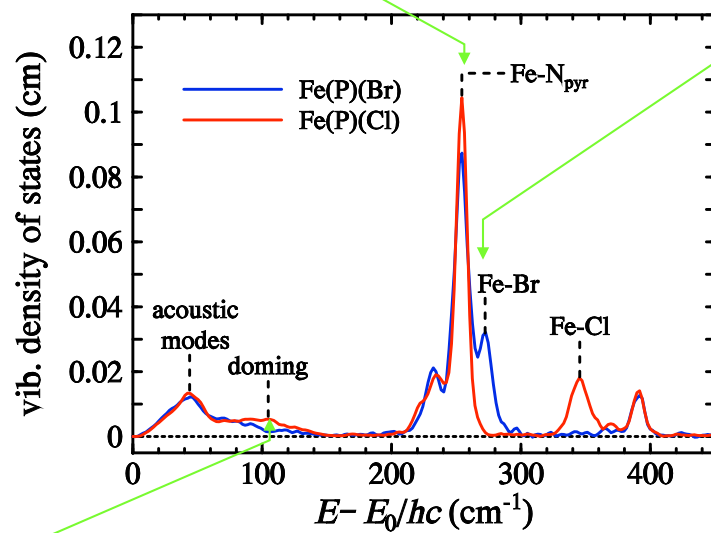
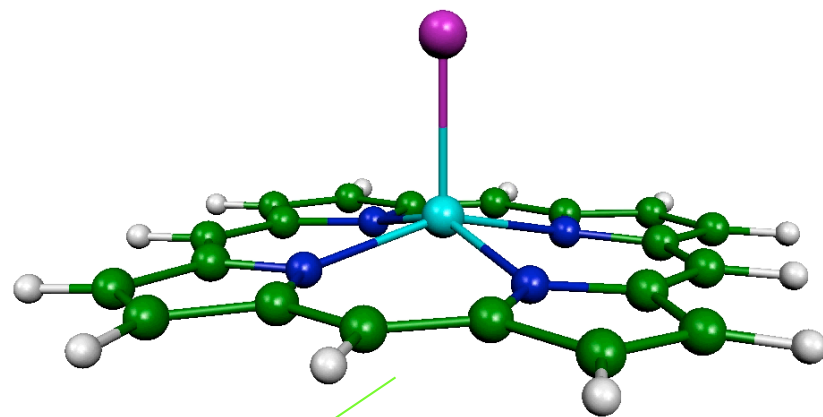
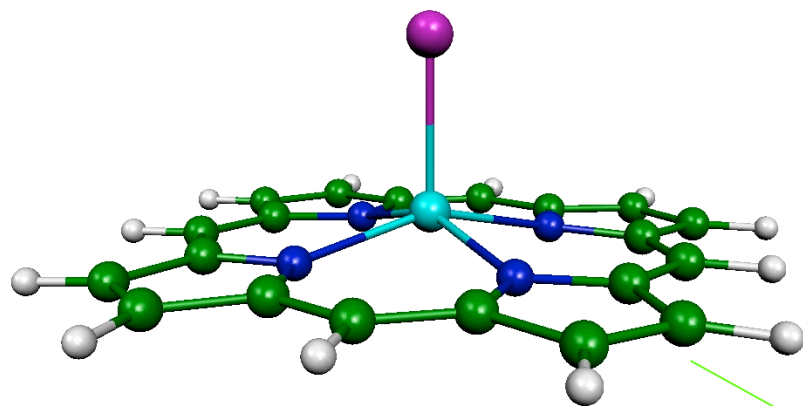
Tetraphenylporphyrin (TPP)
 Octaethylporphyrin (OEP)

<u>A</u>	<u>B</u>
Phenyl	H
H	Ethyl

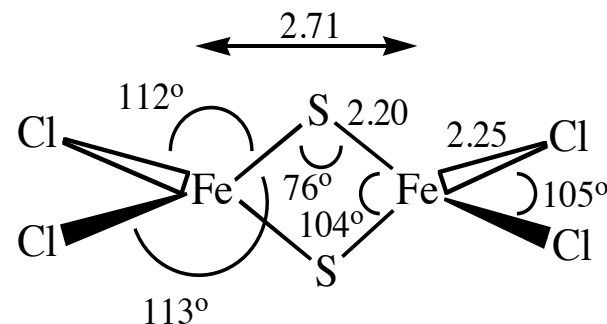
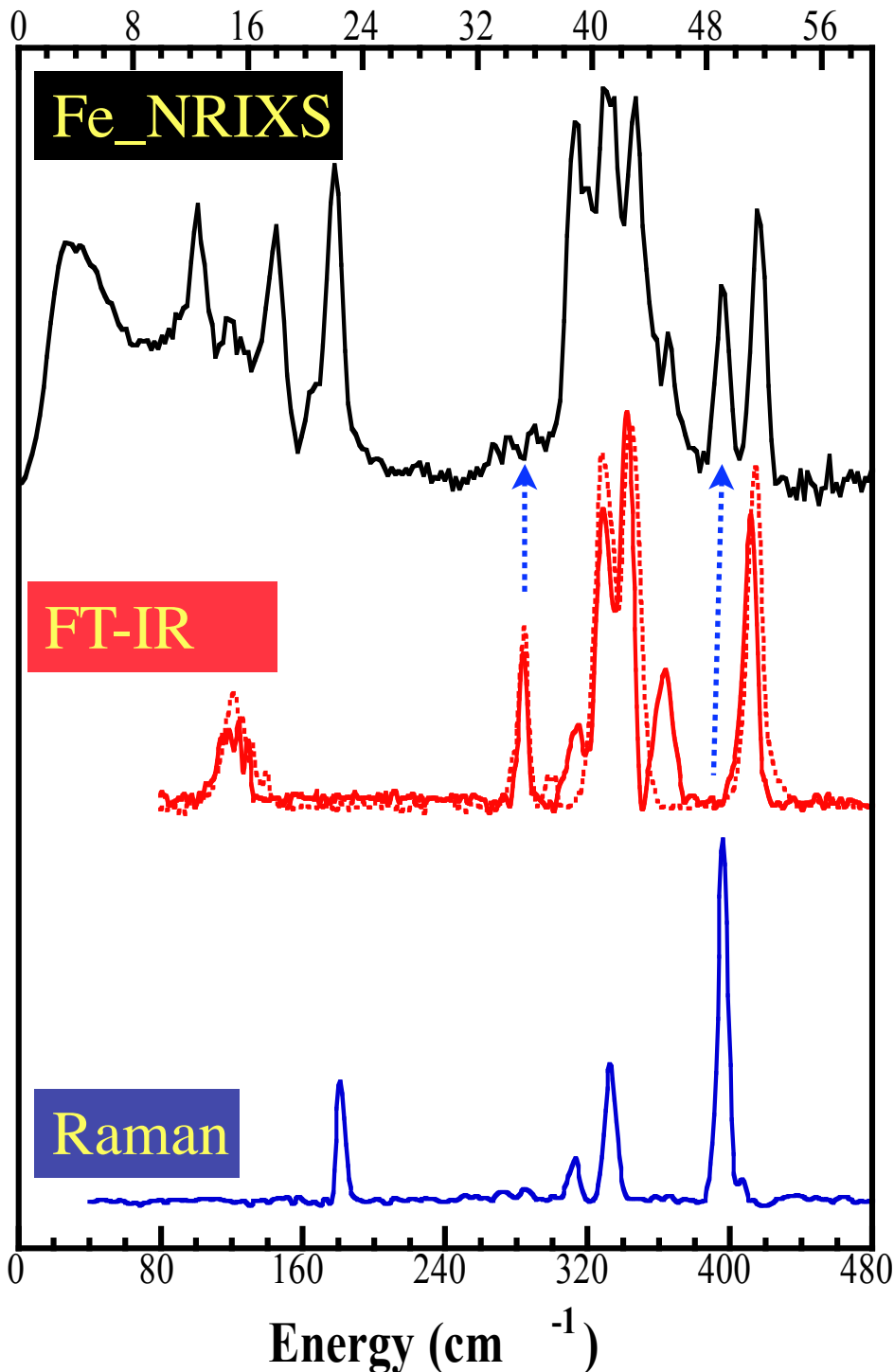
FeTPP(1MeIm)NO







Energy (meV)

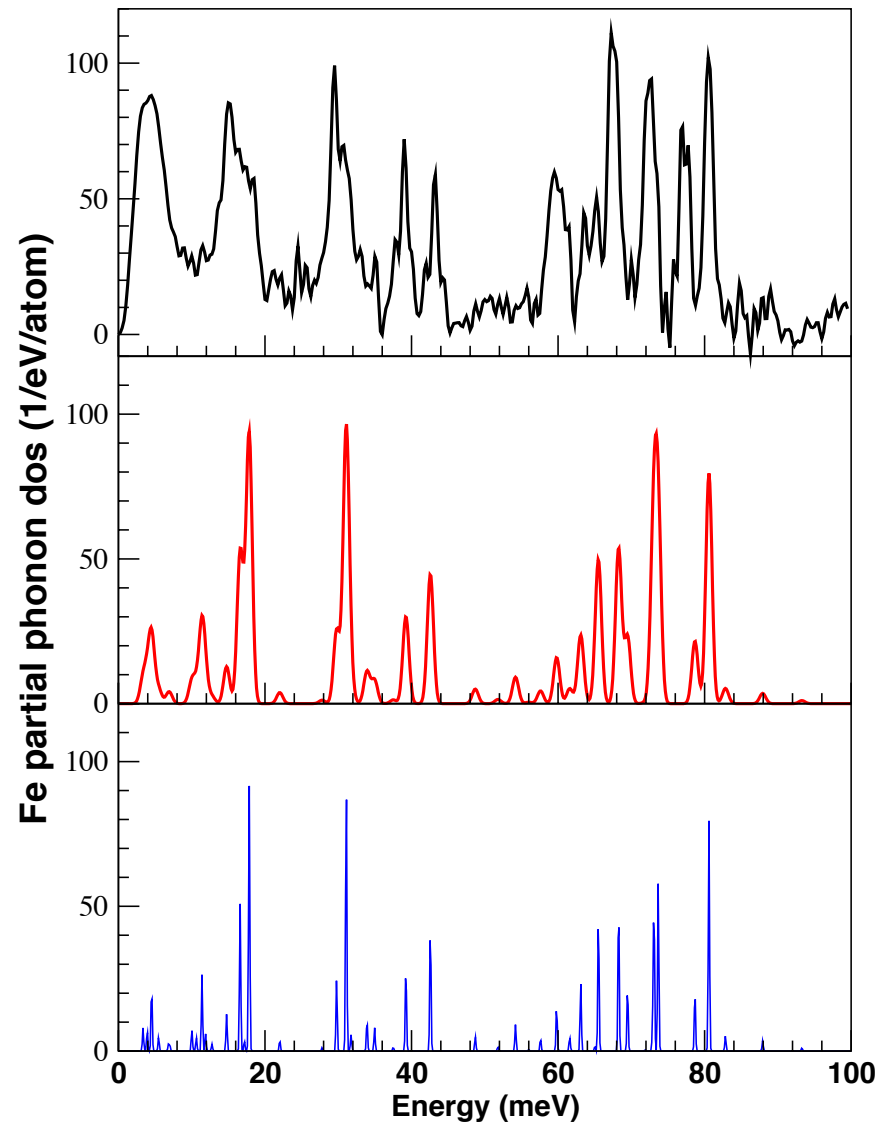
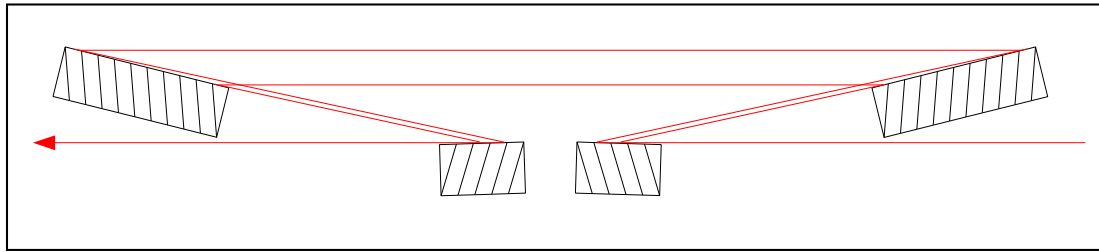


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$$\phi_{\alpha} = \frac{1}{3} \frac{\bar{v}_R}{\bar{v}_{\alpha}} e^{2j_{\alpha}} (\bar{n}_{\alpha} + 1) f$$

$\sim 0.1\text{meV}$, all-vacuum high resolution monochromator



Protonation state of oxo-ligand in heme protein intermediates:

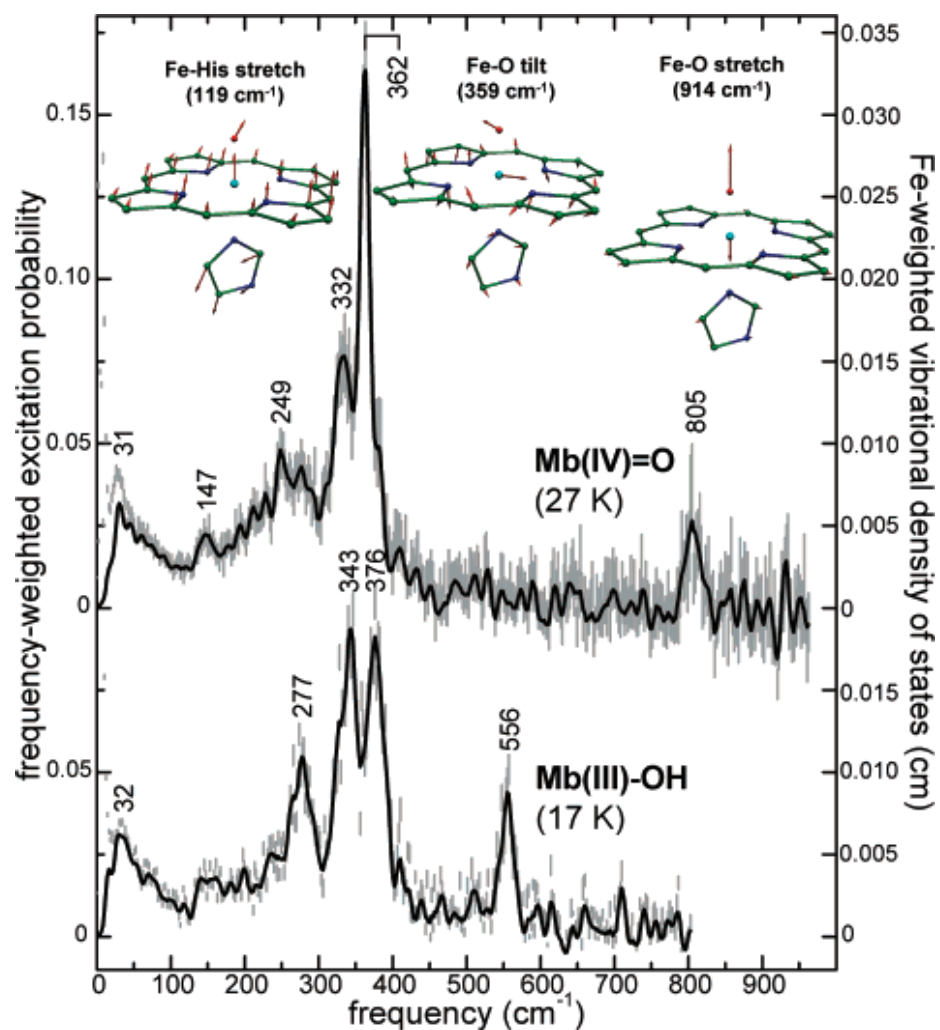
J|A|C|S
COMMUNICATIONS

Published on Web 01/18/2008

Synchrotron-Derived Vibrational Data Confirm Unprotonated Oxo Ligand in Myoglobin Compound II

Weiqiao Zeng,[†] Alexander Barabanschikov,[†] Yunbin Zhang,[†] Jiyong Zhao,[‡] Wolfgang Sturhahn,[‡] E. Ercan Alp,[‡] and J. Timothy Sage^{*†}

J. AM. CHEM. SOC. 2008, 130, 1816–1817



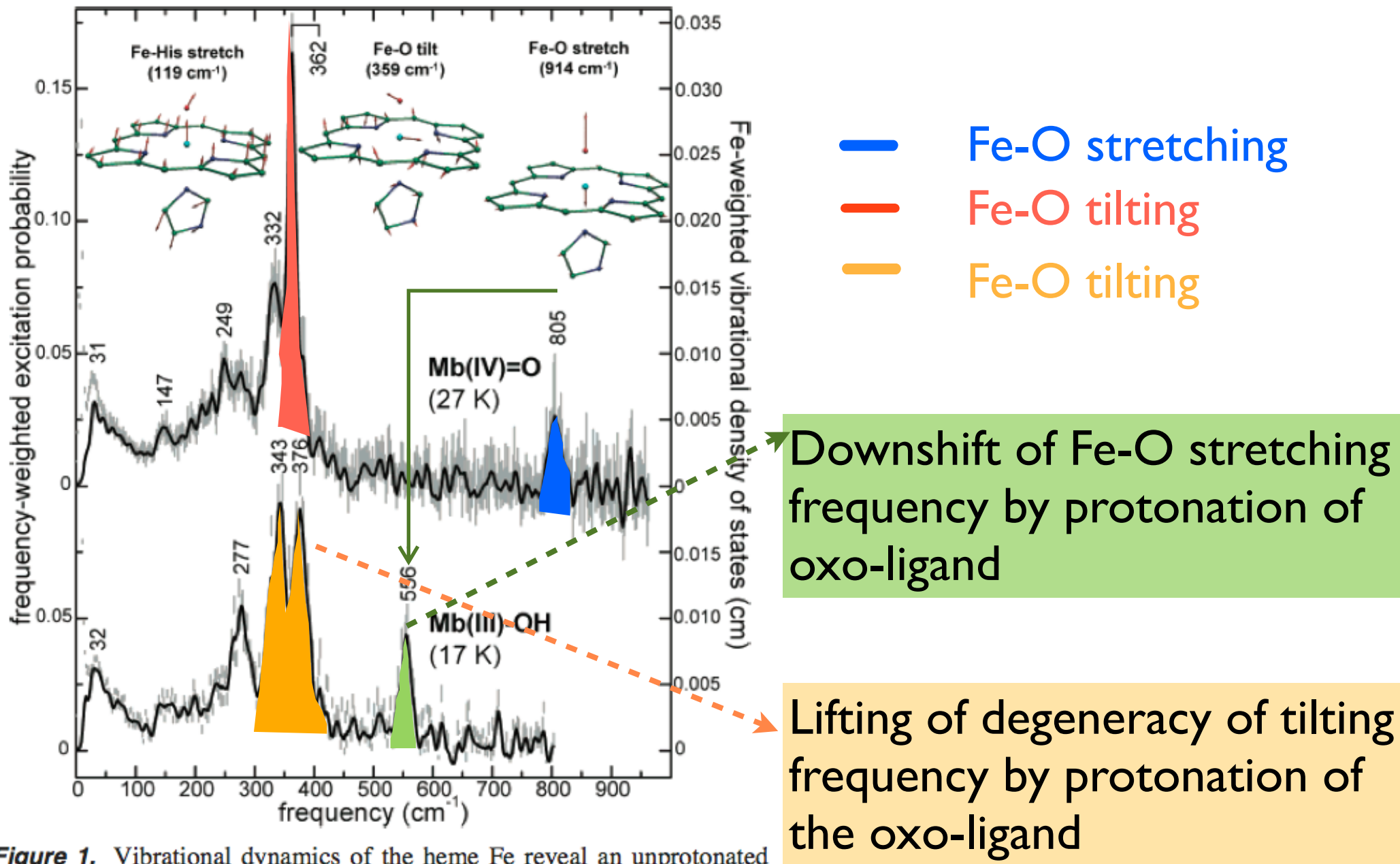


Figure 1. Vibrational dynamics of the heme Fe reveal an unprotonated oxo ligand in Mb(IV)=O, in contrast with the bound hydroxyl group in Mb(III)-OH. Protonation of the oxo ligand results in a downshift of the Fe-O stretching frequency from 805 cm^{-1} to 556 cm^{-1} , and splits the Fe-O tilting vibrations, which are degenerate near 362 cm^{-1} in Mb(IV)=O, but are separated by 33 cm^{-1} in the asymmetrically protonated heme Mb(III)-OH complex. Error bars represent the normalized experimental signal,

The Mössbauer isotopes observed with synchrotron radiation (1985-2016)

Isotope	Energy (eV)	Half-life (ns)	ΔE (neV)	Tabulated E (eV)
^{181}Ta	6215.5	9800.	0.067	6238
^{169}Tm	8401.3	4.	114.0	8409.9
^{83}Kr	9403.5	147.	3.1	9400
^{187}Os	9776.8	2.16	211.	
^{57}Fe	14412.5	97.8	4.67	14413
^{151}Eu	21541.4	9.7	47.0	21532
^{149}Sm	22496.	7.1	64.1	22490
^{119}Sn	23879.4	17.8	25.7	23870
^{161}Dy	25651.4	28.2	16.2	25655
^{129}I	27770.	16.8	27.2	27800
^{40}K	29834.	4.25	107.0	29560
^{125}Te	35460	1.48	308.0	35491.9
^{121}Sb	37129.	4.53	100.0	37133.
^{129}Xe	39581.3	1.465	311.2	39578.
^{61}Ni	67419.	5.1	89.0	67400
^{73}Ge	68752	1.86	245.	68752
^{176}Hf	88349.	1.43	319.4	83000
^{99}Ru	89571.	28.8	15.8	89651.8
^{67}Zn	93300.	9200.	0.049	

Thank you