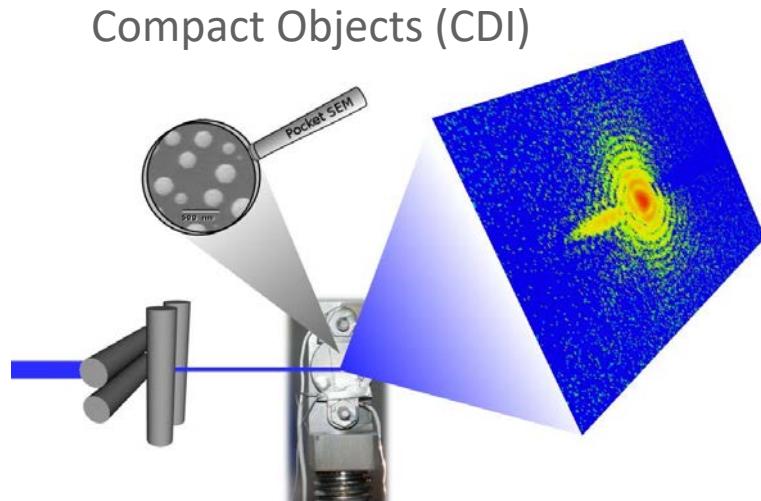


# Coherent Diffraction Imaging

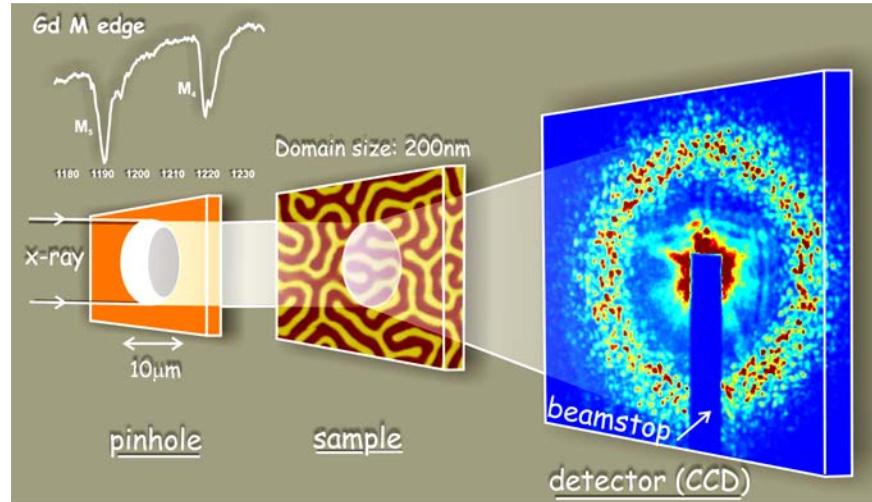
Ross Harder aka “The Imposter”  
34-ID-C  
Advanced Photon Source

<https://tinyurl.com/y2qtrz7c>



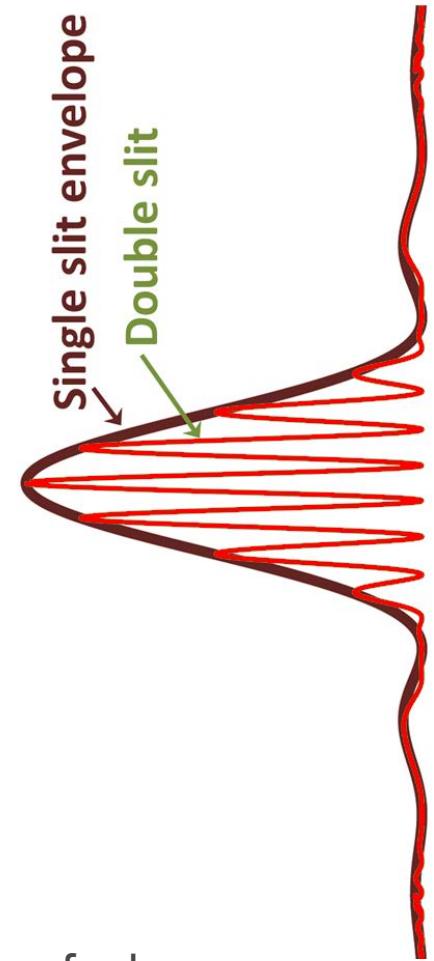
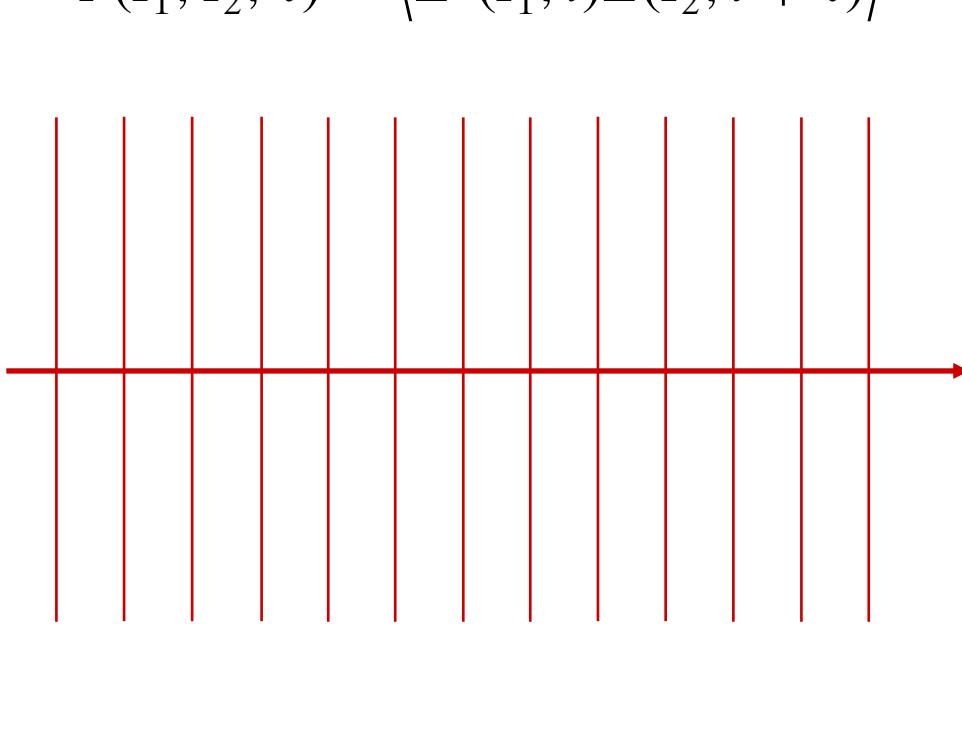
Acknowledgments:  
Prof. Ian Robinson (BNL)  
Dr. Xiaojing Huang (BNL)  
Dr. Jesse Clark (~~PULSE institute, SLAC~~ Amazon)  
Prof. Oleg Shpyrko (UCSD)  
Dr. Andrew Ulvestad (~~ANL – MSD~~Tesla)  
Dr. Ian McNulty (~~ANL – CNM~~ MaxIV)  
Dr. Junjing Deng (ANL – APS)

Non-compact samples (Ptychography)



# COHERENCE

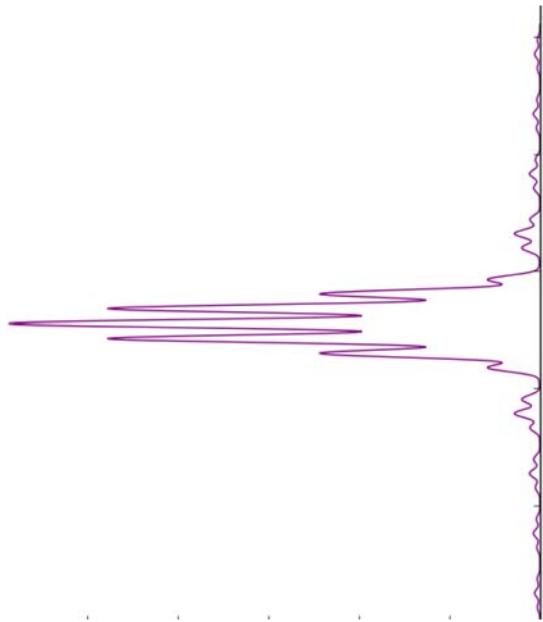
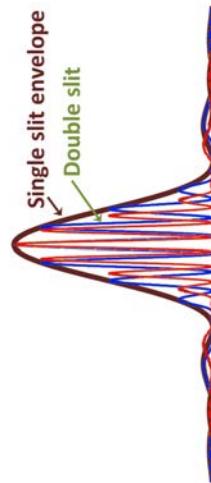
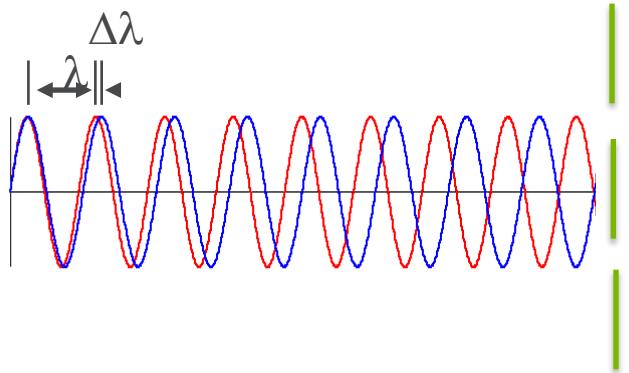
$$\Gamma(\mathbf{r}_1, \mathbf{r}_2; \tau) = \langle E^*(\mathbf{r}_1, t)E(\mathbf{r}_2, t + \tau) \rangle$$



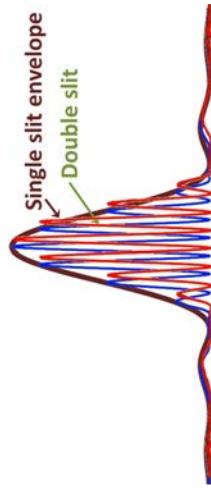
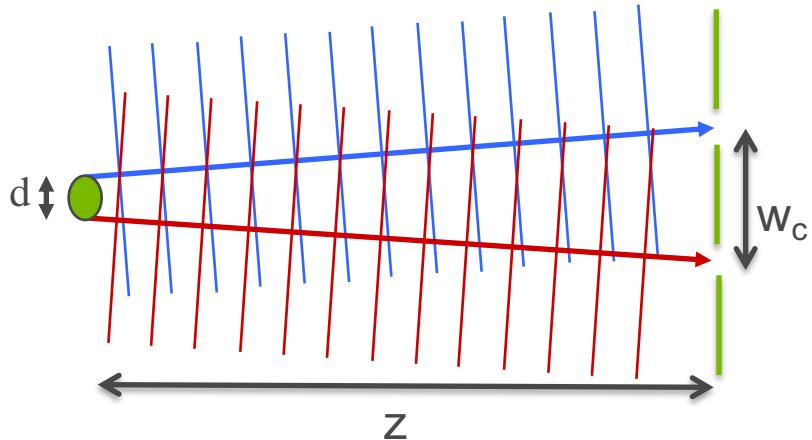
Visibility of fringes is a direct measure of the coherence of a beam.  
If beam is coherent across the spacing of the slits a Fourier Transform  
of the slit structure is observed downstream.

# COHERENCE

longitudinal coherence

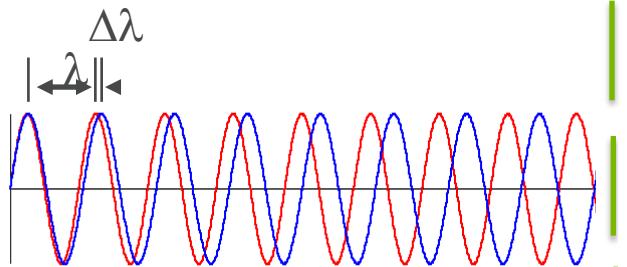


transverse coherence



# COHERENCE

longitudinal coherence

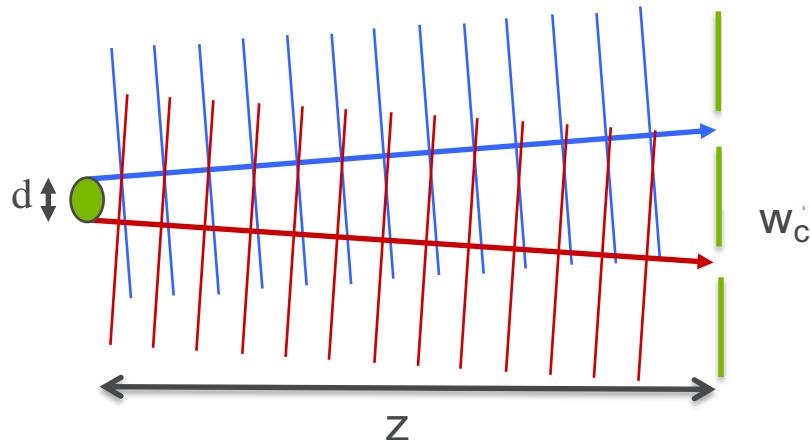


$$l_c \sim \frac{\lambda^2}{\Delta\lambda}$$

$$\tau_c \sim \frac{\lambda^2}{c\Delta\lambda}$$

Si (111)  
0.5 um or 1.5 fs

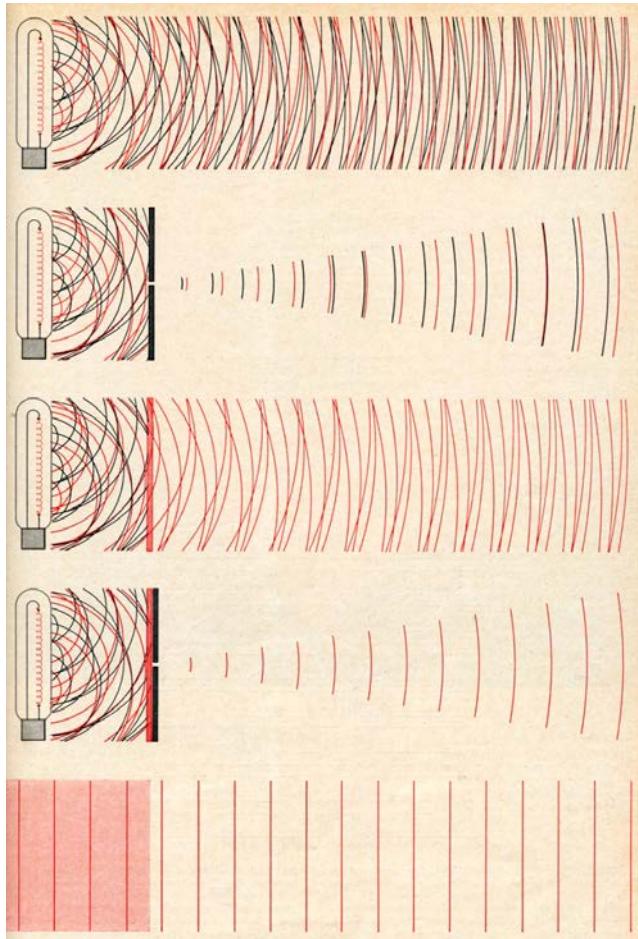
transverse coherence



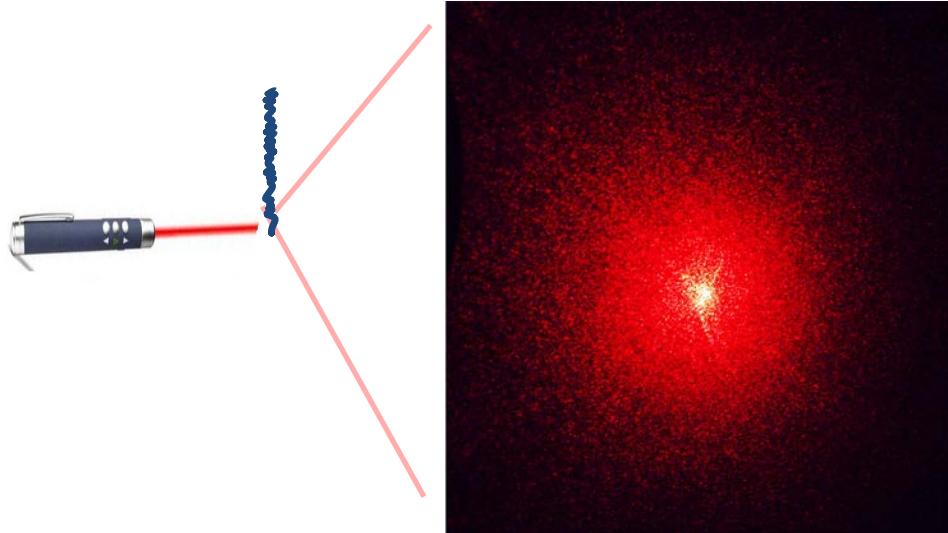
$$w_c \sim \frac{\lambda z}{d}$$

34-ID-C 50m  
25x70 um @ 9 keV

# Coherence: Laser Speckle

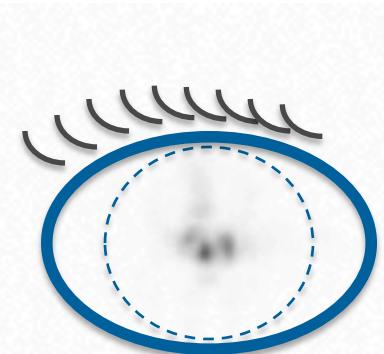
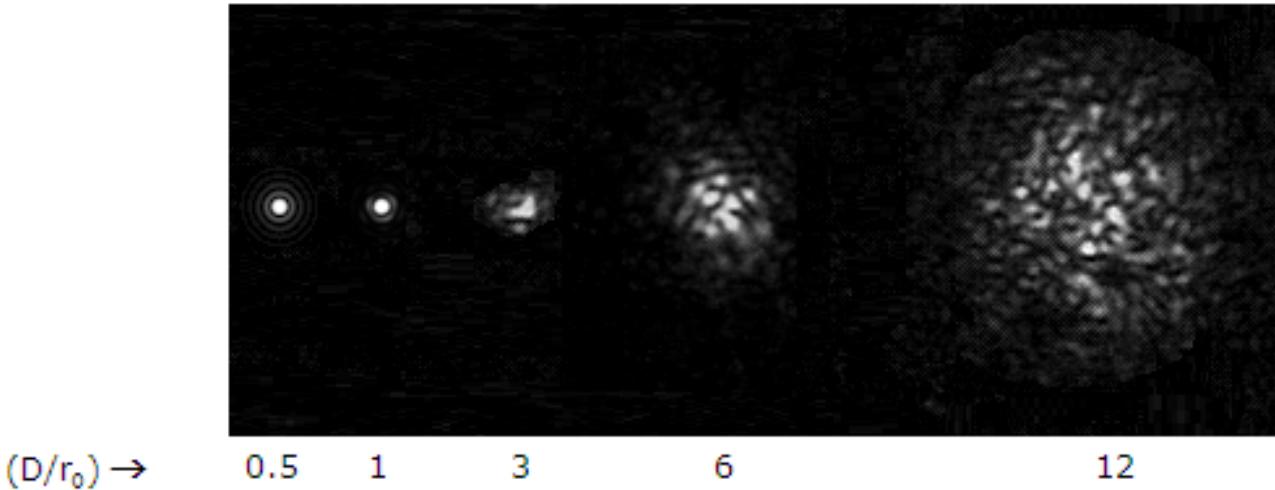


A. L. Schawlow "Laser Light"  
Scientific American, 219 (3), p. 120, (1968)



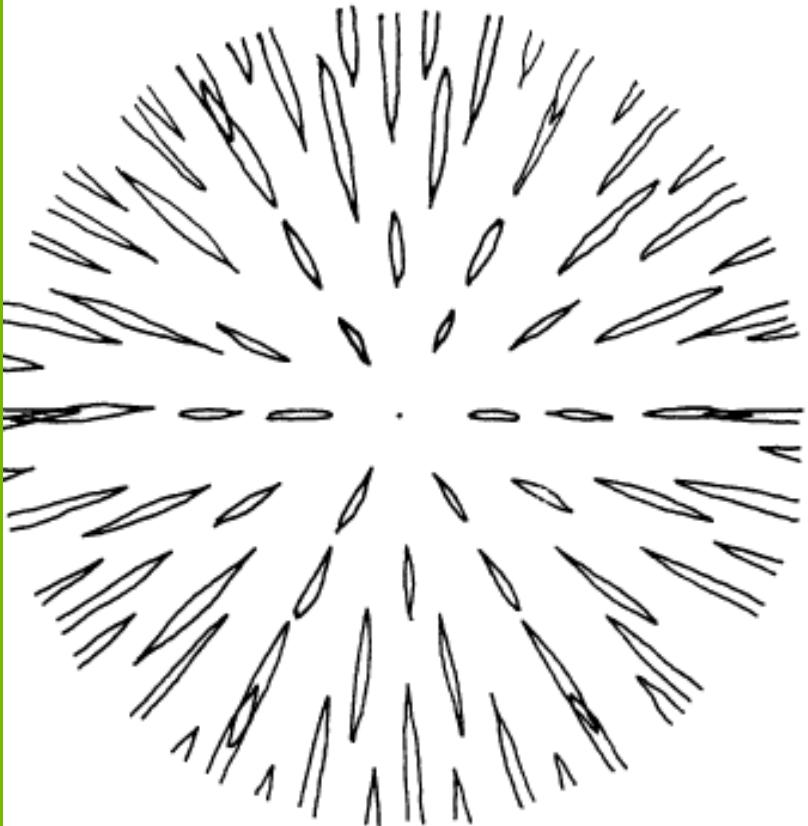
Laser Speckle: Interference pattern arising from randomly distributed scatterers

# SIMPLEST SPECKLE EXPERIMENT: TWINKLE, TWINKLE LITTLE STAR



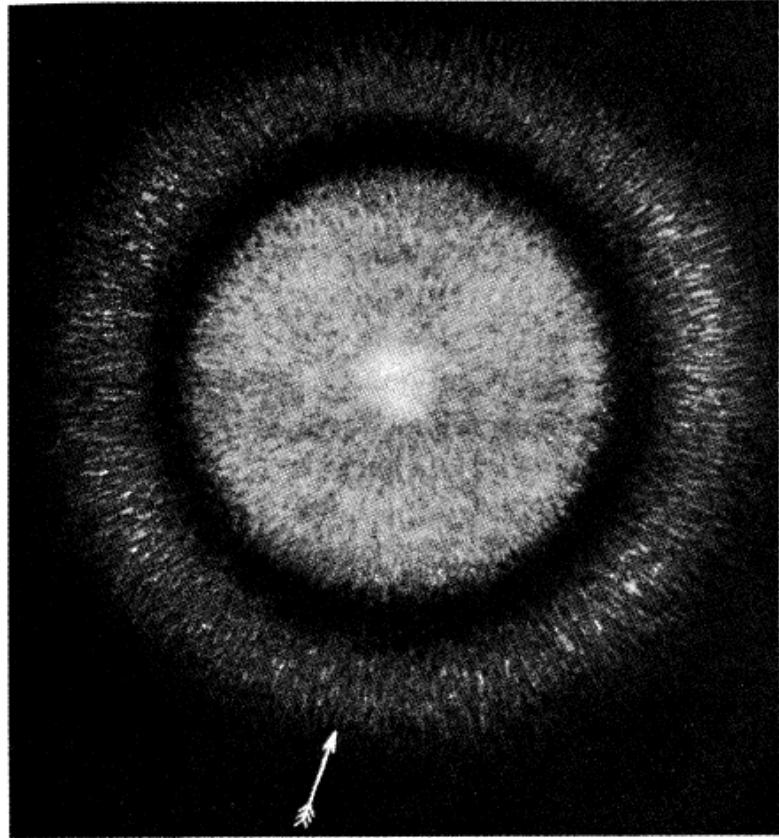
Stars are big, but very far away. As a result, their light has a high transverse coherence. As the light propagates through the atmosphere our eye detects a portion of the coherent diffraction

# First Speckle: Exner, 1877 (using candle light)



K. Exner: Sitzungsber. Kaiserl.  
Akad. Wiss. (Wien) 76, 522 (1877)

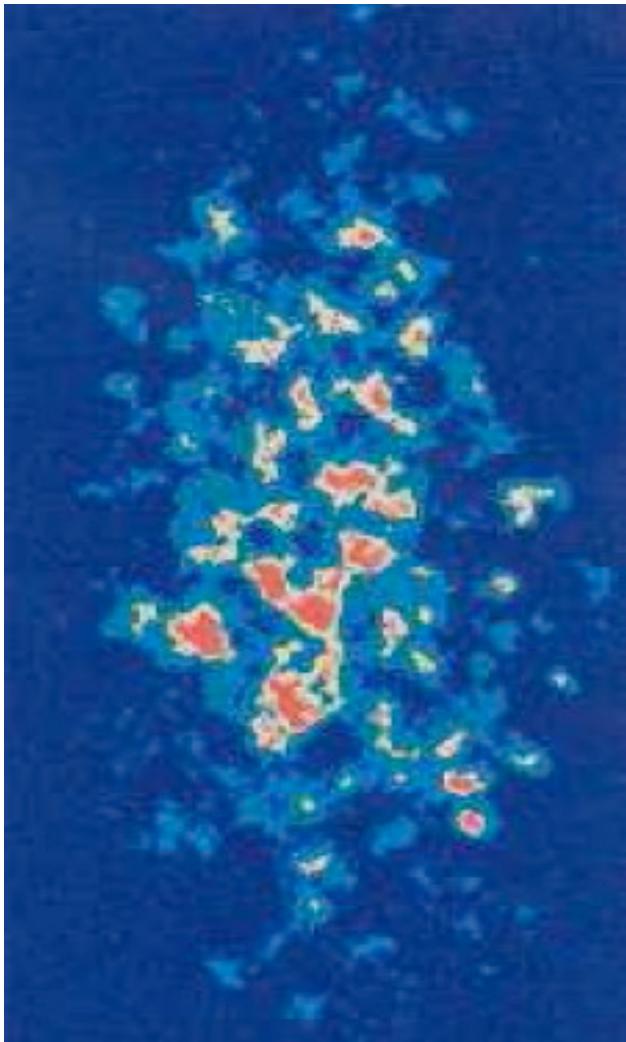
# First Speckle Photo: von Laue, 1914 (using arc discharge lamp)



M. von Laue: Sitzungsber. Akad.  
Wiss. (Berlin) 44, 1144 (1914)

# First X-ray Speckle:

M. Sutton et al., *Nature* 352, 608-610 (1991)



$$I \propto |F(q)|^2$$

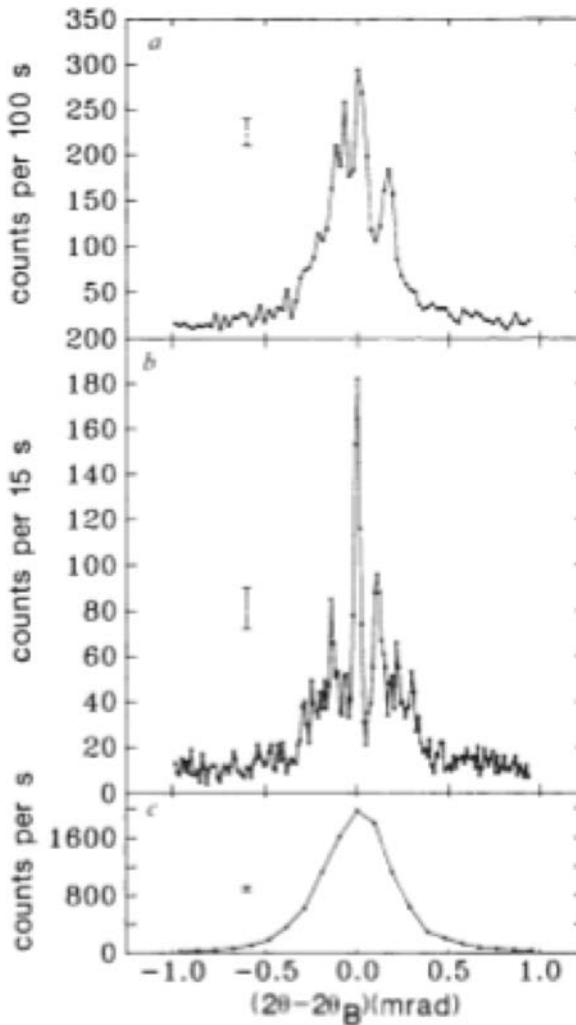


FIG. 4 Speckle patterns measured using a 2.5- $\mu\text{m}$ , b, 5- $\mu\text{m}$  and c, 50- $\mu\text{m}$  collimating pinholes. The analysing pinholes used were 50, 25 and 100  $\mu\text{m}$ , respectively. Representative error bars are indicated, and the solid lines simply connect the data points. The (001) Bragg angle,  $2\theta_0$ , is  $\sim 23.9^\circ$ .

# WHY USE SYNCHROTRON RADIATION?

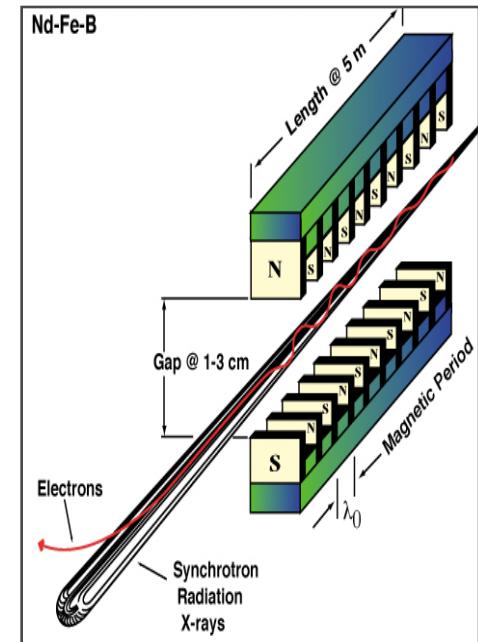
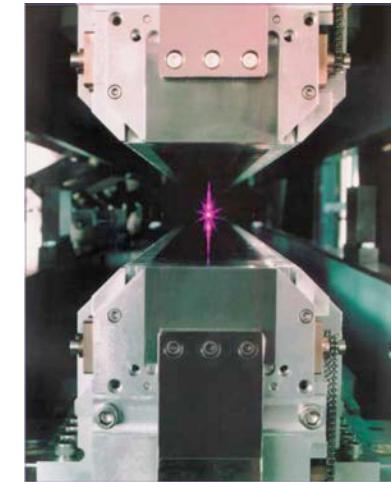
Synchrotron sources offer:

- Brightnesss (small source, collimated)
- Tunability (IR to hard x-rays)
- Polarization (linear, circular)
- Time structure (short pulses)

Source brightness is the key figure of merit  
for coherent imaging

**B = photons/source area, divergence, bandwidth**

$$F_c \sim \lambda^2 B$$



# COHERENT X-RAY REFERENCES

- Vartanyants, I A, and A Singer. 2010 “Coherence Properties of Hard X-Ray Synchrotron Sources and X-Ray Free-Electron Lasers.” *New Journal of Physics* 12 (3): 035004.
- Singer, Andrej, and Ivan A Vartanyants. 2014. “Coherence Properties of Focused X-Ray Beams at High-Brilliance Synchrotron Sources.” *Journal of Synchrotron Radiation* 21 (1). International Union of Crystallography: 5–15. doi:10.1038/nano.2008.246.
- Nugent, Keith. 2009. “Coherent Methods in the X-Ray Sciences.” *Advances in Physics* 59 (1): 1–99. doi:doi: 10.1080/00018730903270926.

# X-RAYS, TWO EXTREMES FOR STRUCTURAL STUDY:

## X-ray Imaging (Shadowgraphs)

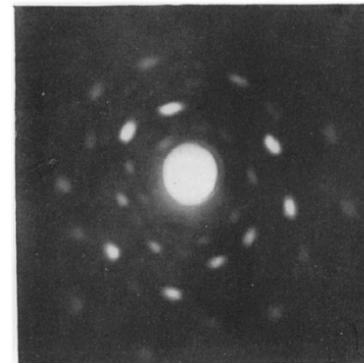
- Inhomogeneous, non-periodic materials
- Limited spatial resolution (~0.001 mm)



Roentgen, Nobel 1900

## X-ray Diffraction (Scattering)

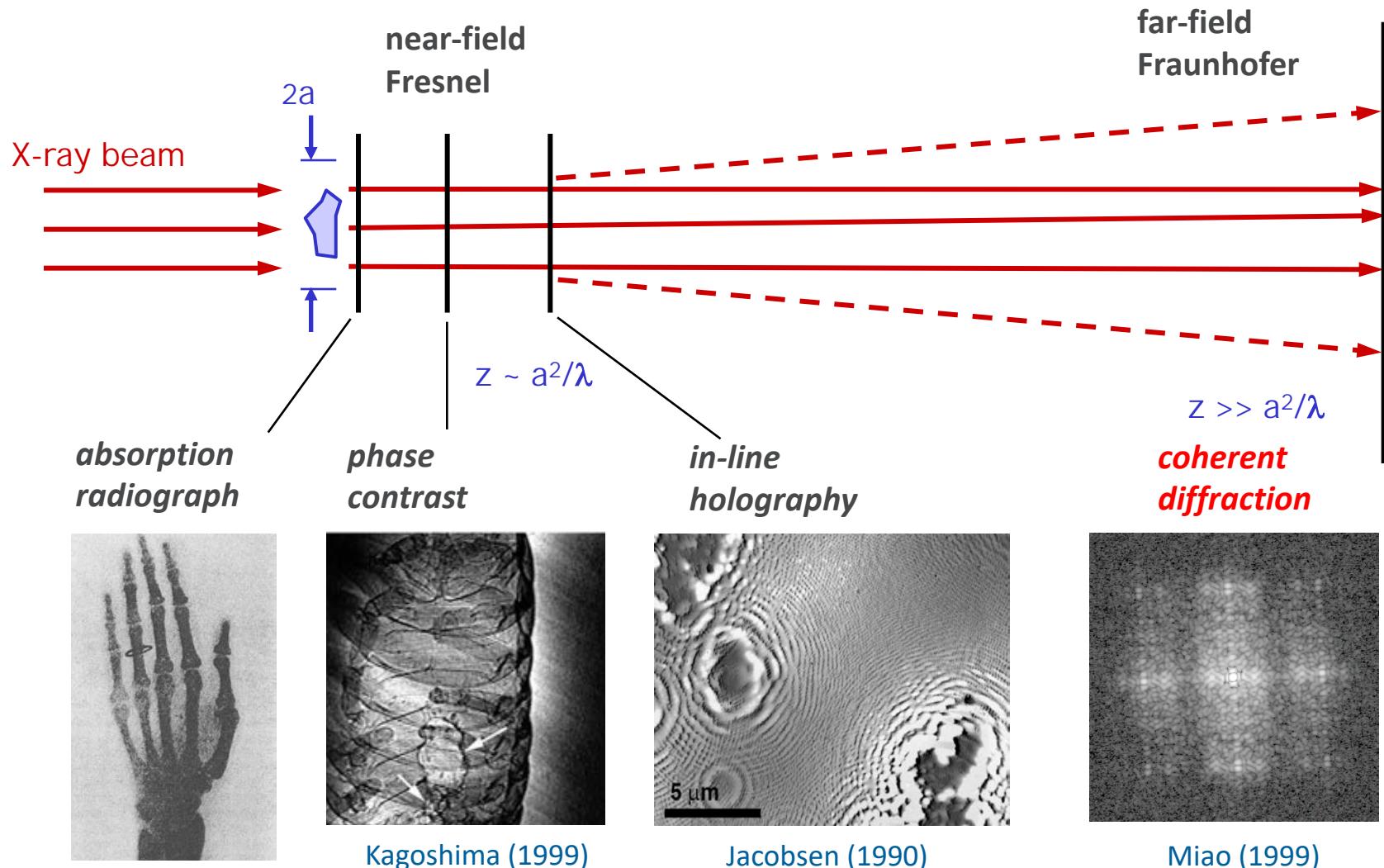
- Is particularly sensitive to periodicity in the sample (Crystals)
- Atomic resolution (unit cell)



Von Laue, Nobel 1914  
Bragg & Bragg, Nobel 1915

Coherent Imaging  
is scattering

# IMAGING REGIMES WITH COHERENT X-RAYS



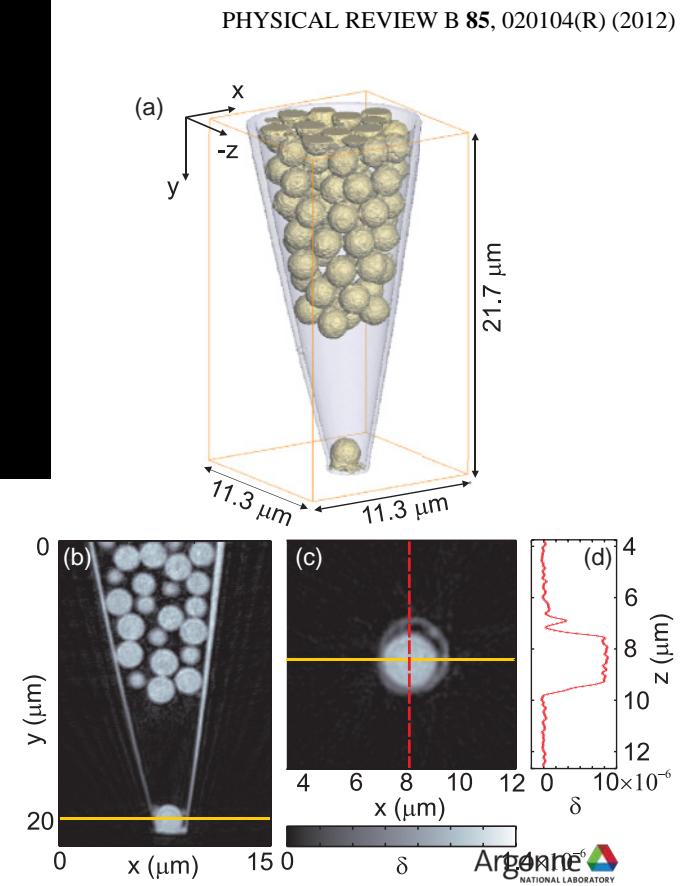
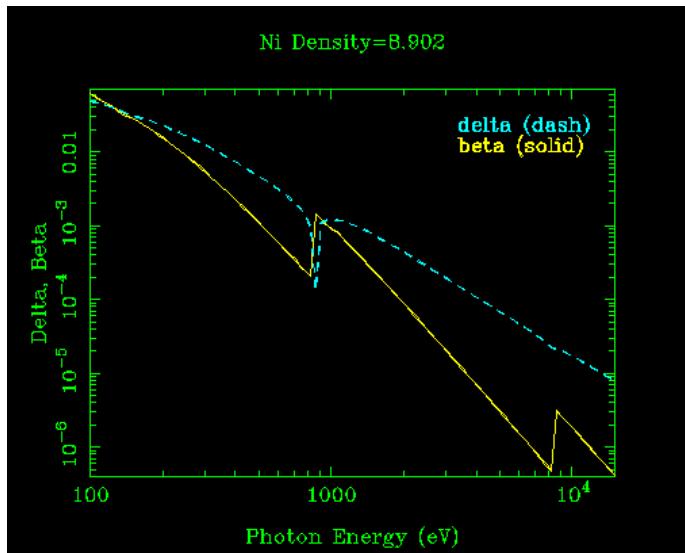
# REFRACTIVE INDEX AND CONTRAST IN THE X-RAY REGION

$$n = 1 - \delta - i\beta = 1 - \frac{r_e}{2\pi} \lambda^2 \sum_i n_i f_i(0)$$

$$A = A_0 \exp(-inkt)$$
$$k = 2\pi/\lambda$$

- Absorption contrast:  
sensitive to  $\text{Im}(n)$   
 $\sim 4\pi\beta(x,y)t/\lambda$

- Phase contrast:  
sensitive to  $\text{Re}(n)$   
 $\sim 2\pi\delta(x,y)t/\lambda$

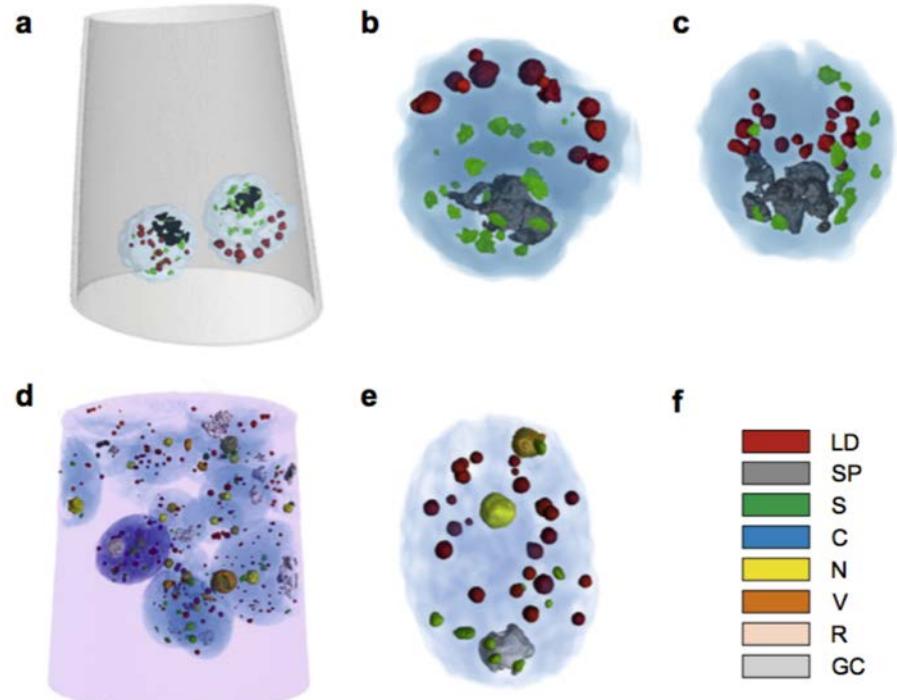
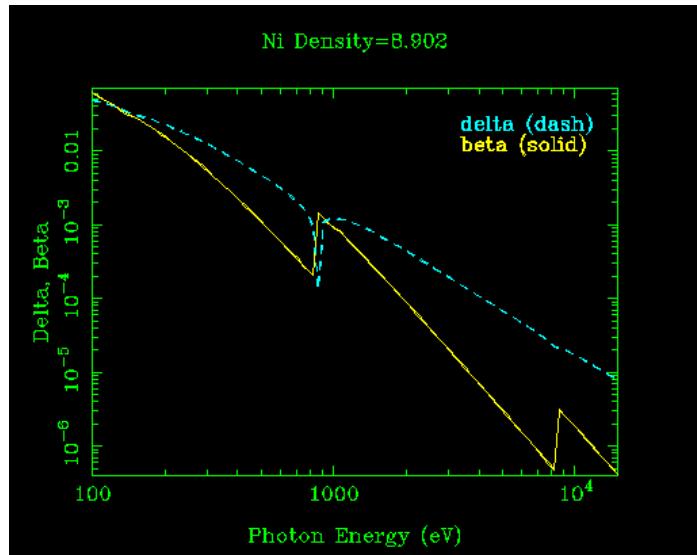


Diaz, Ana, et al, 2012. "Quantitative X-Ray Phase Nanotomography." *Physical Review B* 85.

# REFRACTIVE INDEX AND CONTRAST IN THE X-RAY REGION

$$n = 1 - \delta - i\beta = 1 - \frac{r_e}{2\pi} \lambda^2 \sum_i n_i f_i(0)$$

$$A = A_0 \exp(-inkt)$$
$$k = 2\pi/\lambda$$



A. Diaz, et al., Journal of Structural Biology, vol. 192, no. 3, pp. 461–469, Oct. 2015.

Absorption contrast:

sensitive to  $\text{Im}(n)$

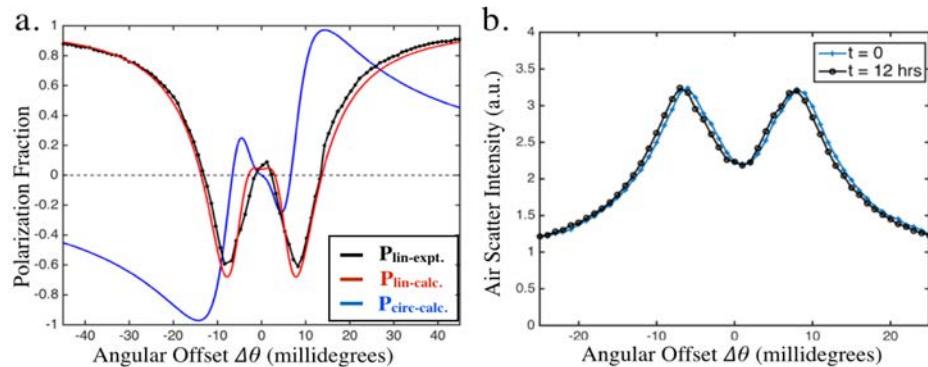
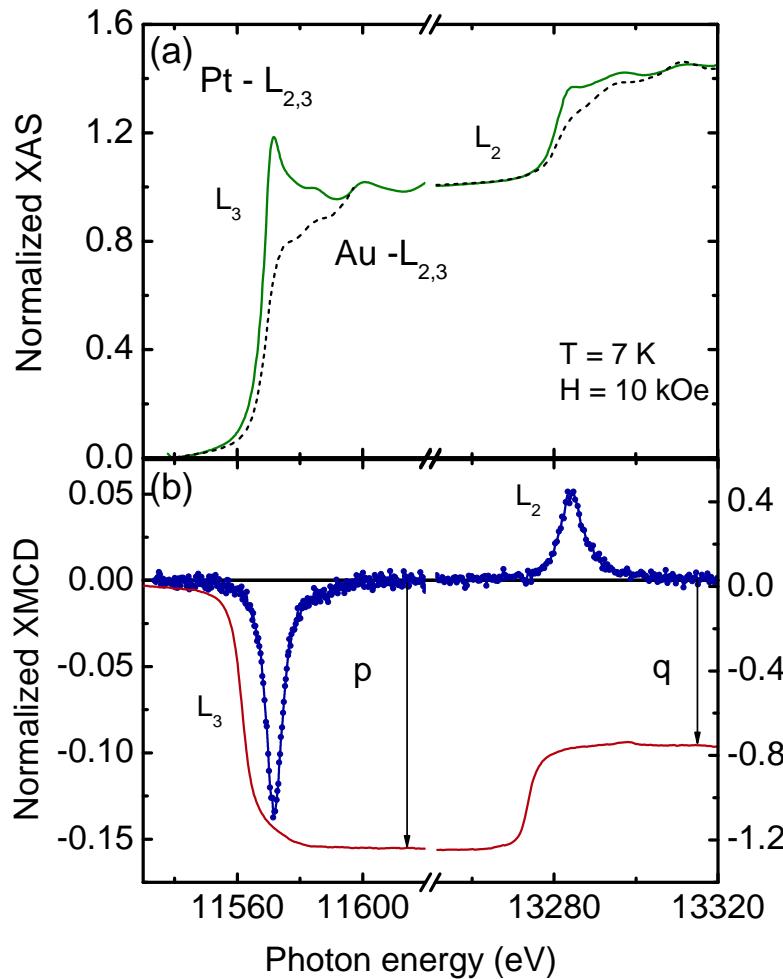
$\sim 4\pi\beta(x,y)t/\lambda$

Phase contrast:

sensitive to  $\text{Re}(n)$

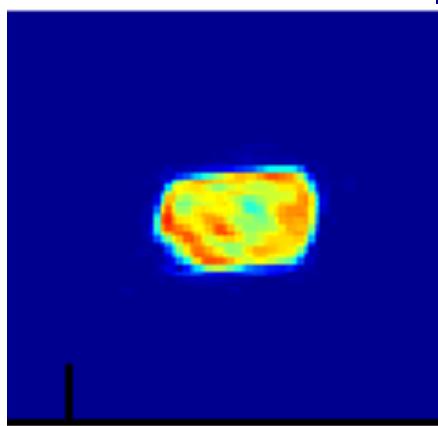
$\sim 2\pi\delta(x,y)t/\lambda$

# POLARIZED X-RAYS GIVE SENSITIVITY TO ELECTRON SPIN in PtCo

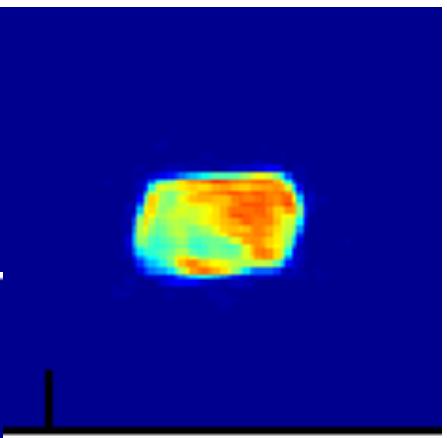


LCP @ 11.565keV

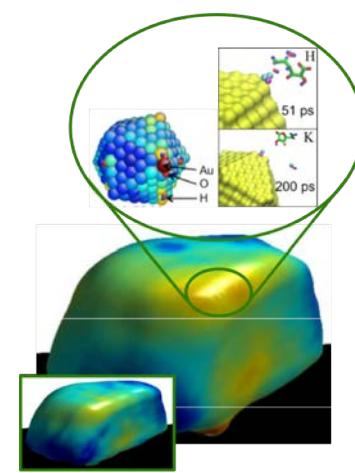
XMC  
D integrat  
al



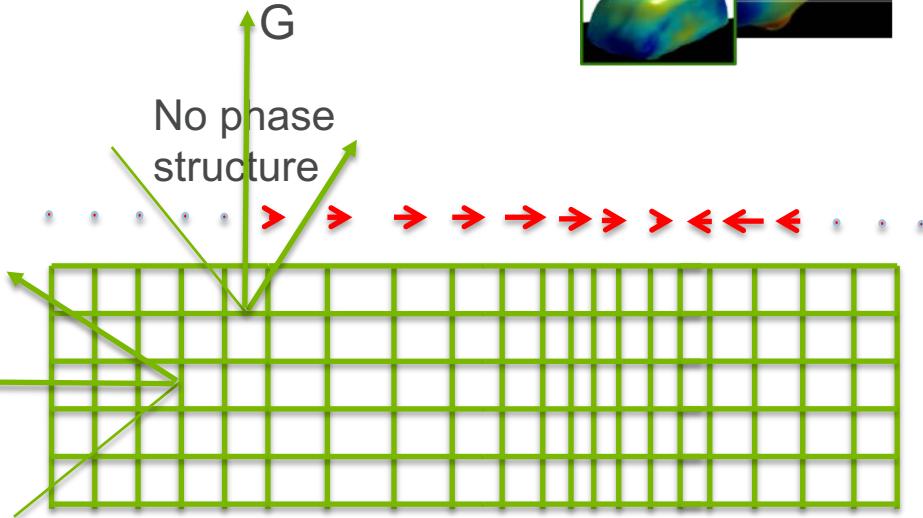
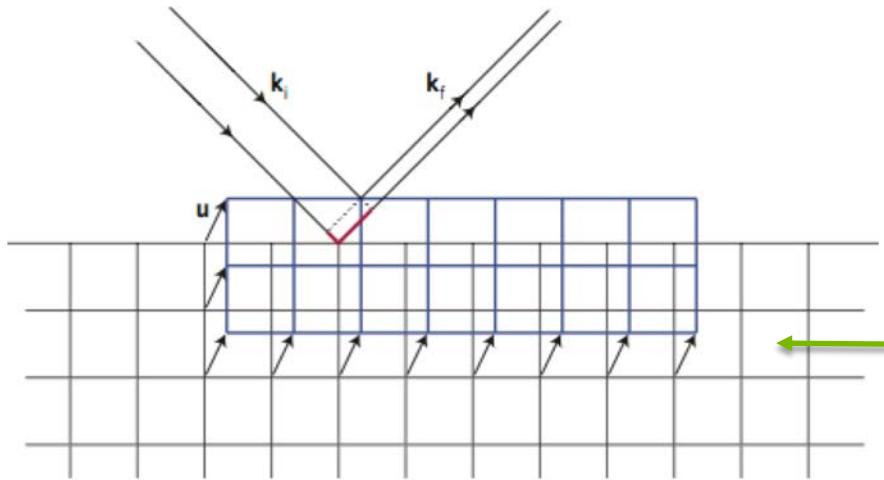
RCP @ 11.565keV



# CDI IN BRAGG GEOMETRY: IMAGING DISPLACEMENT FIELD (STRAIN)



Displacement field  $u(r)$ :

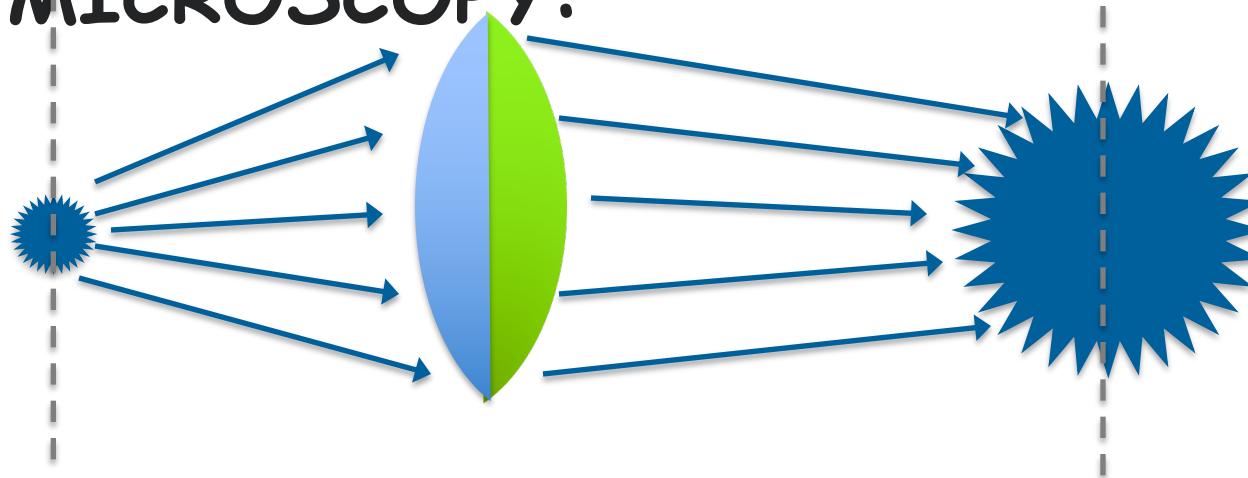


Coherent X-ray Diffraction measures:

$$\tilde{\rho}(\mathbf{r}) = \rho_{\mathbf{G}_{hkl}}(\mathbf{r}) \exp[-i\mathbf{G}_{hkl} \cdot \mathbf{u}(\mathbf{r})]$$

Strain is a gradient of  $u(r)$ , the phase component of the complex-valued density

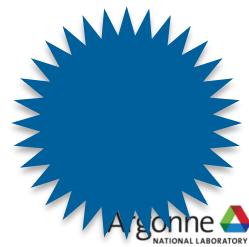
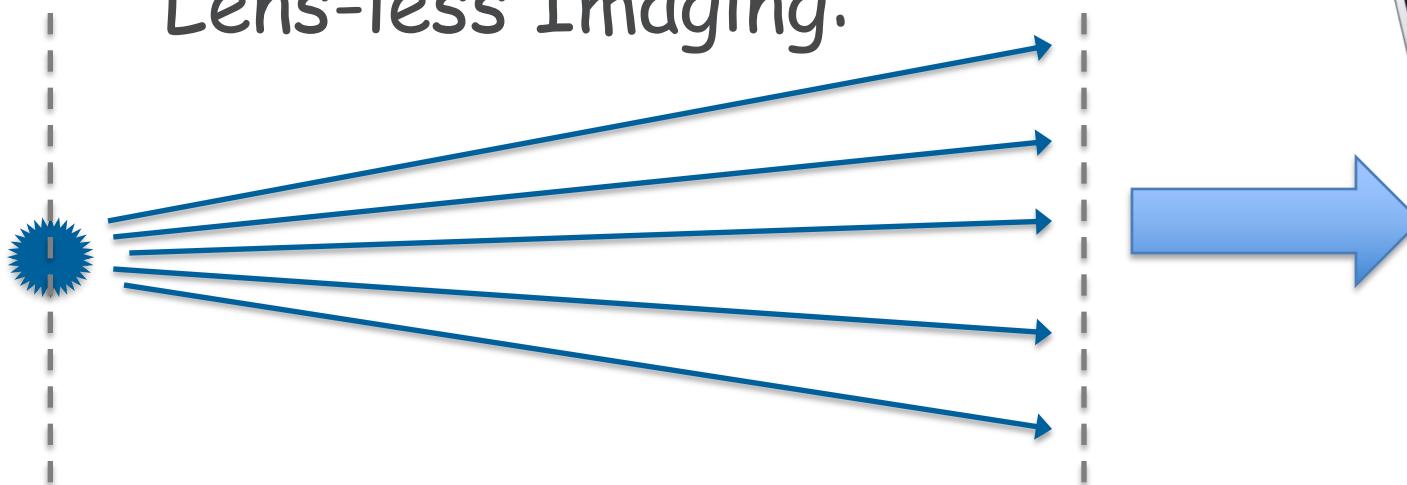
# TRADITIONAL MICROSCOPY:



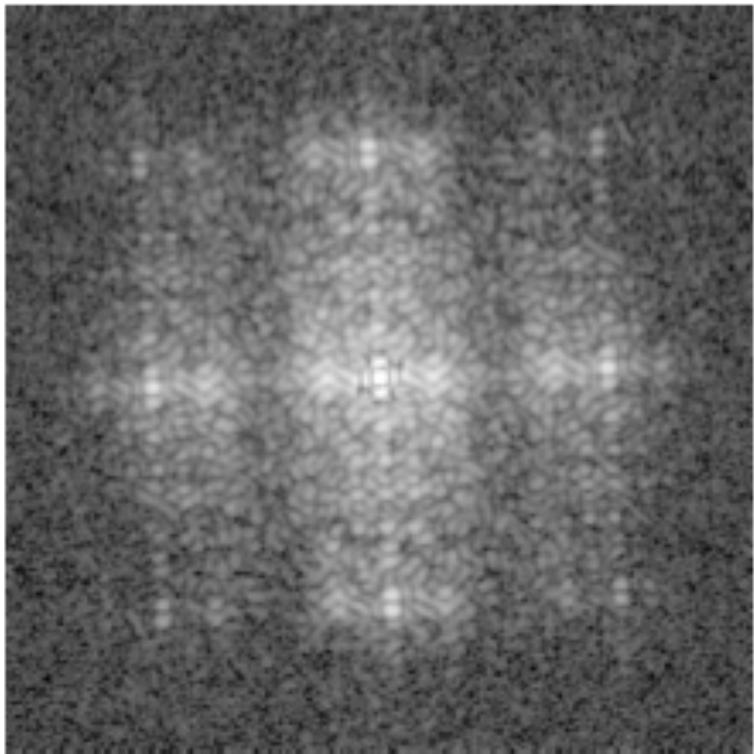
Object Plane

Detector Plane

# Lens-less Imaging:



# FIRST DEMONSTRATION OF CDI WITH X-RAYS



diffraction pattern



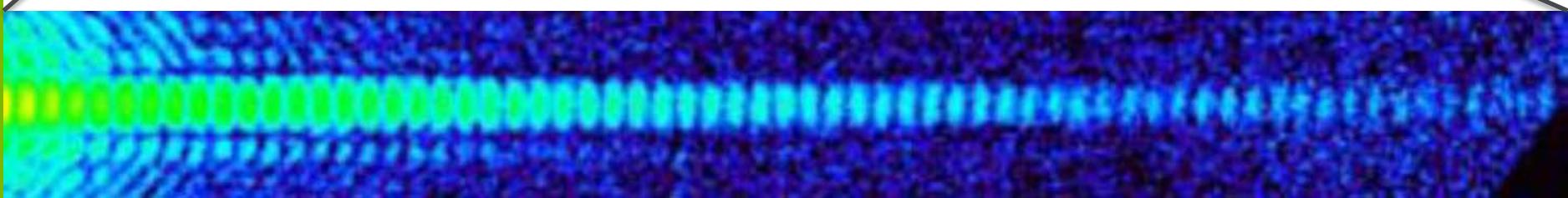
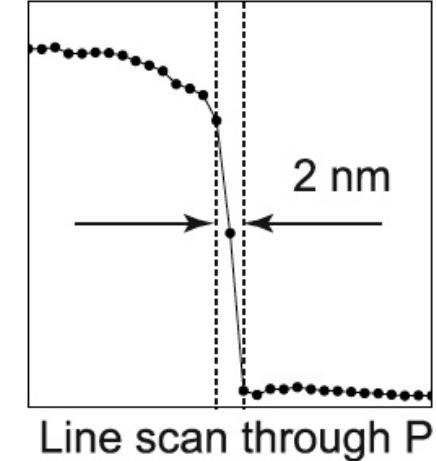
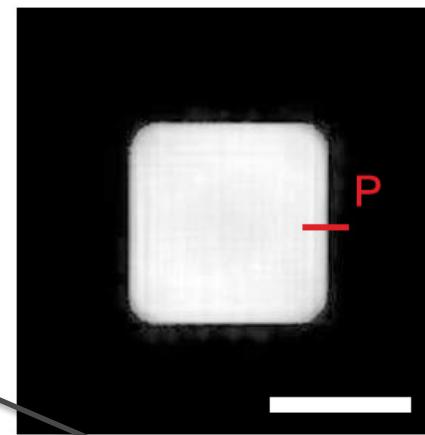
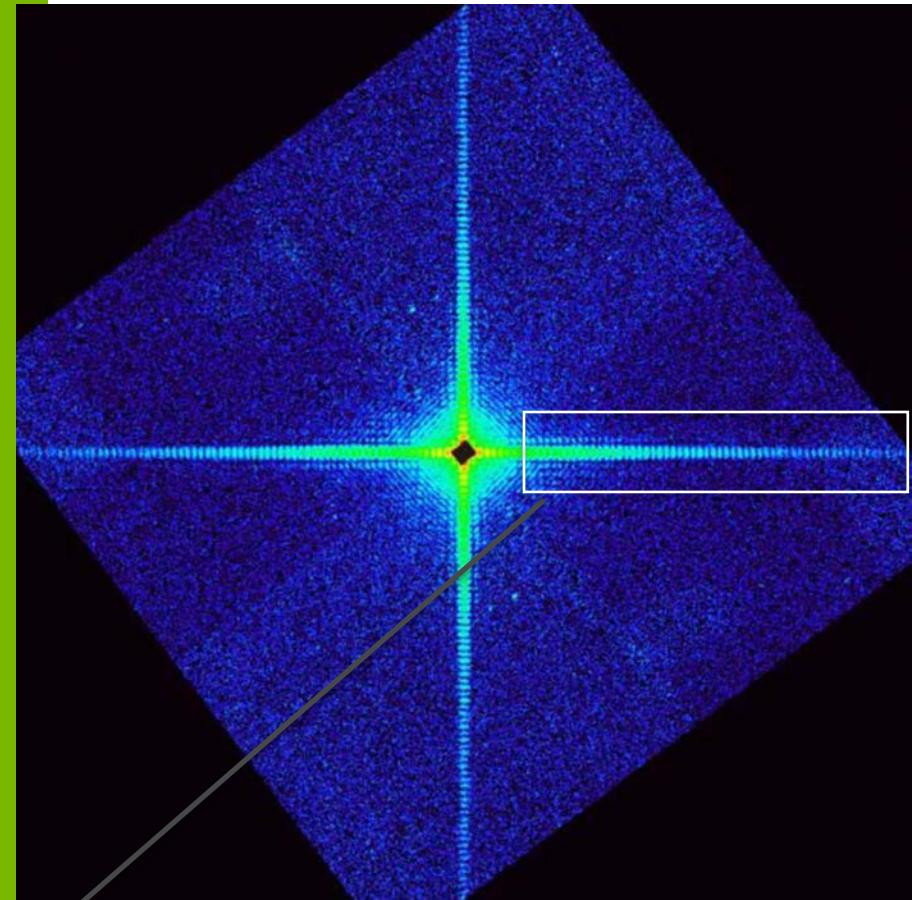
reconstruction

J. Miao, Nature 400, 342  
(1999)

Argonne  
NATIONAL LABORATORY

# COHERENT DIFFRACTIVE IMAGING:

Y. Takahashi et al.,  
Phys. Rev. B 82, 214102 (2010)



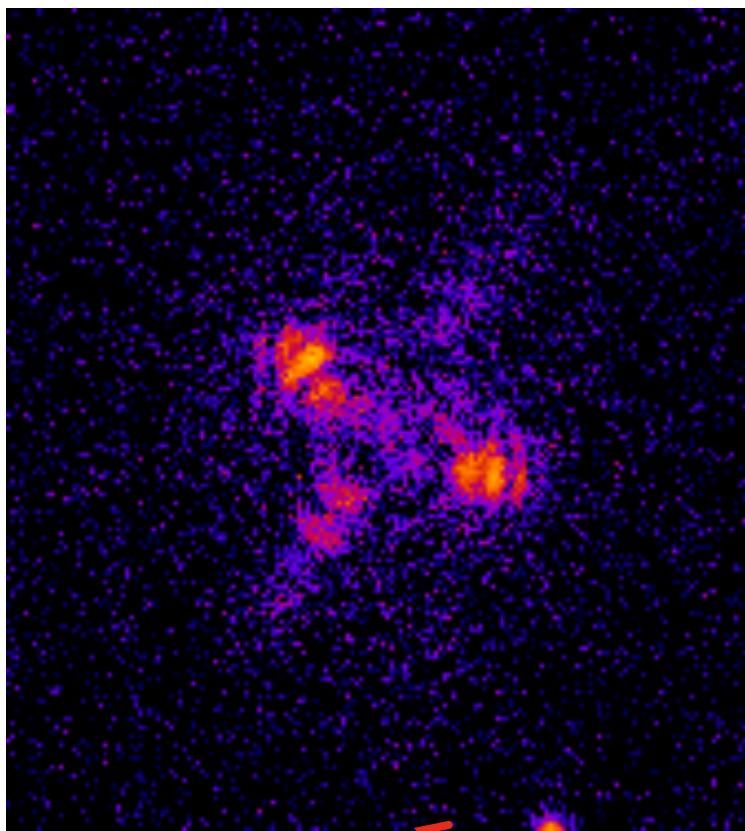
# LARGE-FORMAT, SINGLE-PHOTON SENSITIVE X-RAY CCD CAMERAS OPENED THE DOOR TO COHERENT X-RAY IMAGING

## Fairchild Peregrine 486 CCD Camera

- 4K x 4K pixel array (61.4 mm square area)
- 15  $\mu\text{m}$  pixels, 100% fill factor
- Back-illuminated for up to 80% QE
- Readout noise < 5 e- at 50 Kpixels/s
- Dynamic range > 86 dB in MPP
- 6 s readout with four on-chip amplifiers
- Pixel binning for more rapid readout
- Peltier-cooled to -50 C for low dark current



# Hi Resolution Imaging (CCD)?

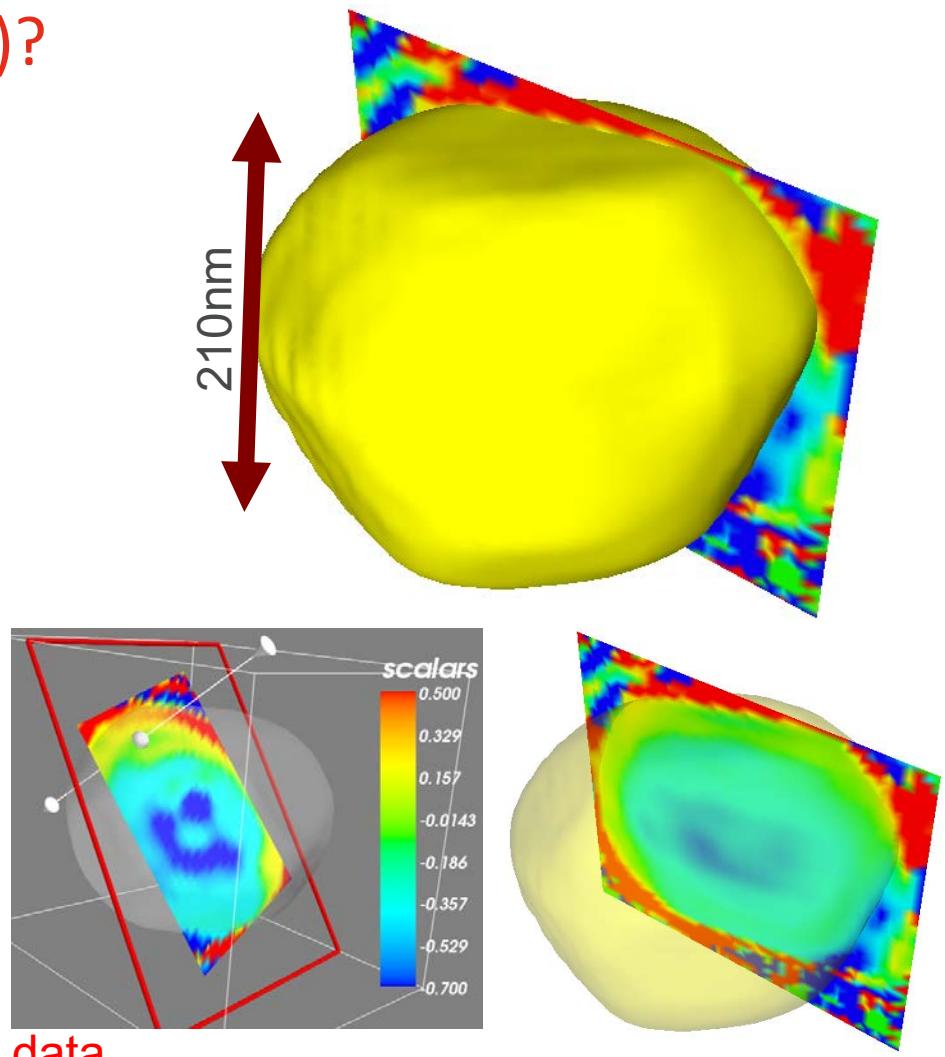


At APS 34-ID-C:

**9.25 hours of scanning**

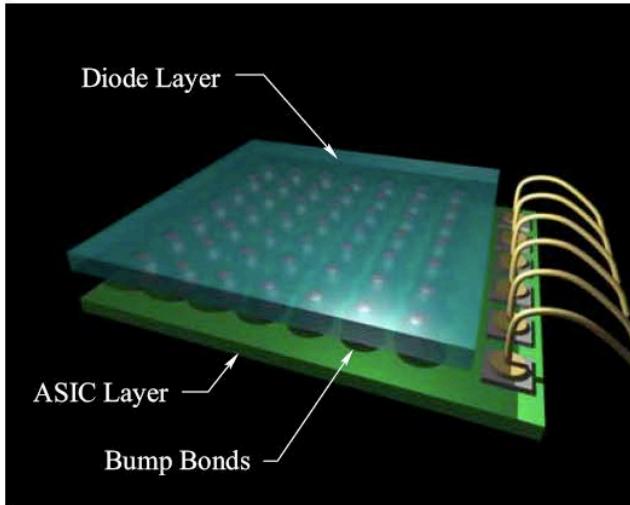
**38 minutes of x-ray exposure**

~7nm data



Rainbow color map (still) considered harmful  
<http://ieeexplore.ieee.org/document/11418486/>

# PIXEL ARRAY DETECTORS: REVOLUTIONIZING COHERENT IMAGING



D. Schuette, S. Gruner (Cornell)

Pilatus 6M detector  
(PSI/Dectris)



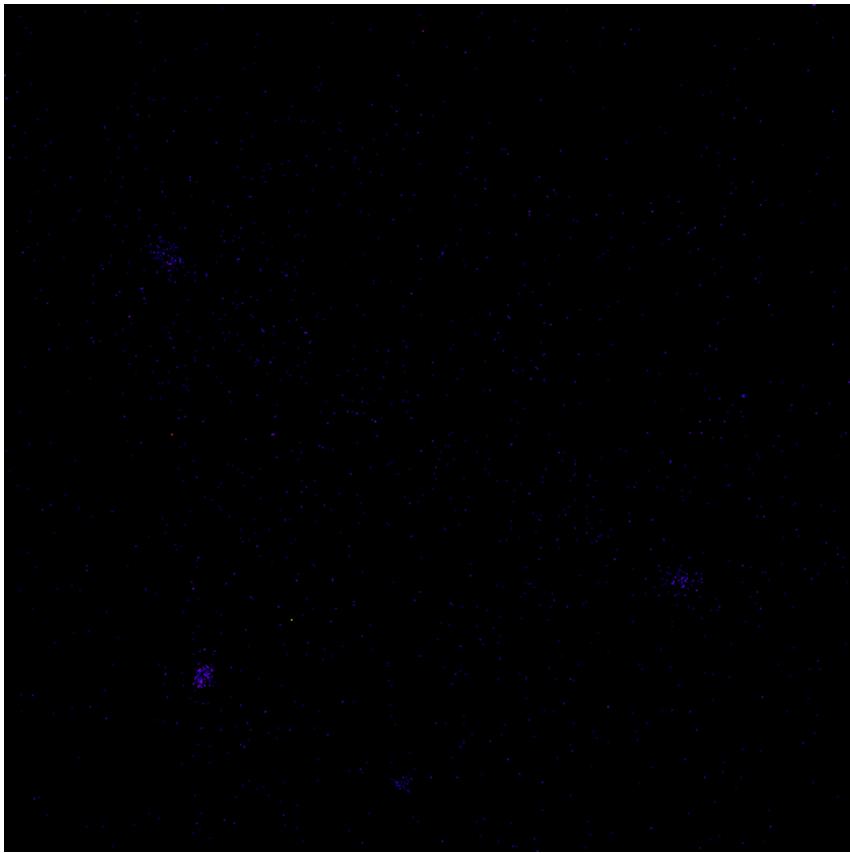
## A Three Layer Hybrid Device

- Diode layer → converts x-rays to photocurrent.
- ASIC layer → custom signal processing electronics.
- A layer of metallic interconnects (bump bonds) between corresponding pixels on the diode and ASIC layers.

PADs can be read out in ~1 ms  
(CCDs take seconds!)

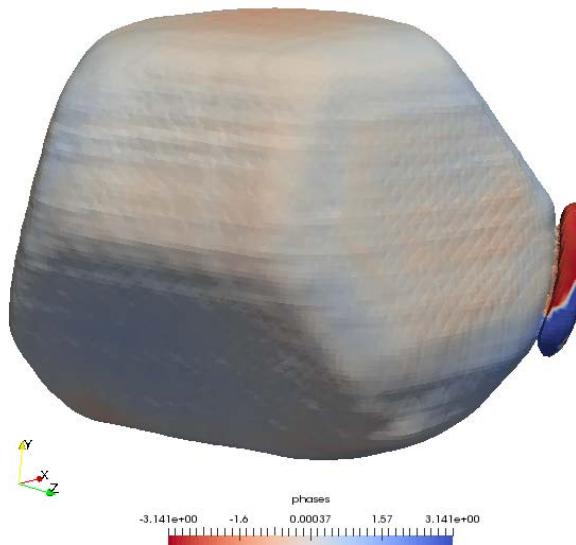
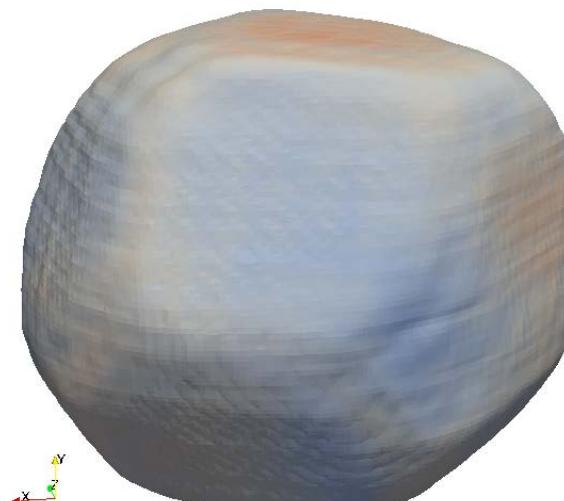
PAD pixels are 55-150  $\mu\text{m}$ .  
(CCDs are 12-24  $\mu\text{m}$ )

# Hi Resolution Imaging (PAD)?

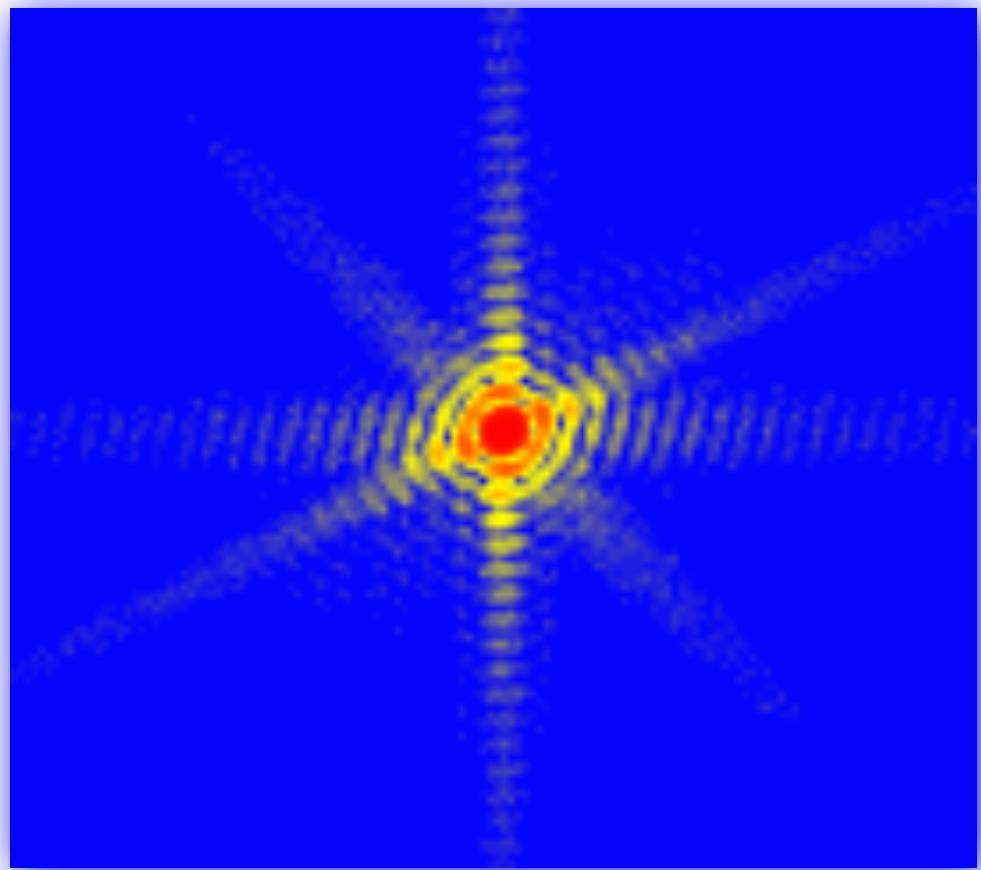
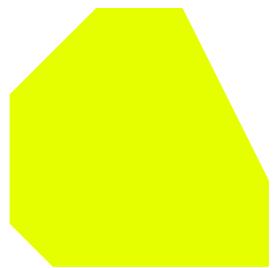


Quad Timepix GaAs sensor

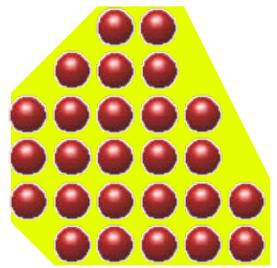
700nm gold crystal  
3 degree rocking curve  
25 minute measurement  
15 sec movie (1X APS-U measurement)



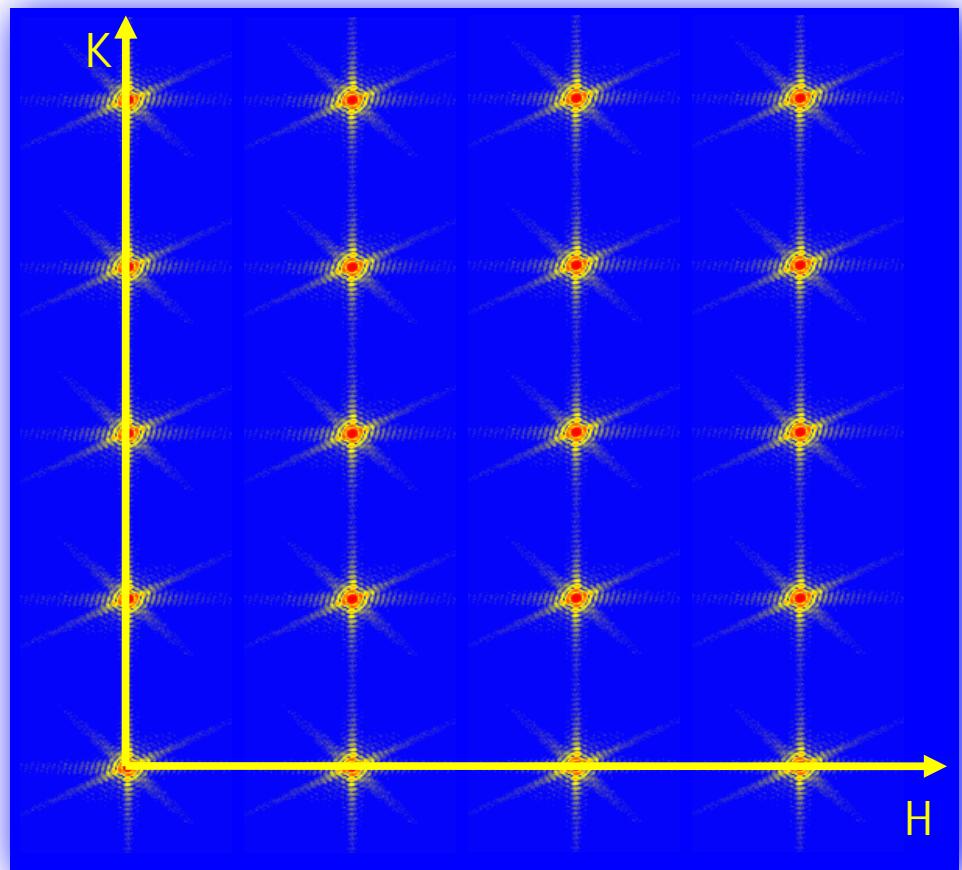
# Coherent Diffraction from Crystals



# Coherent Diffraction from Crystals

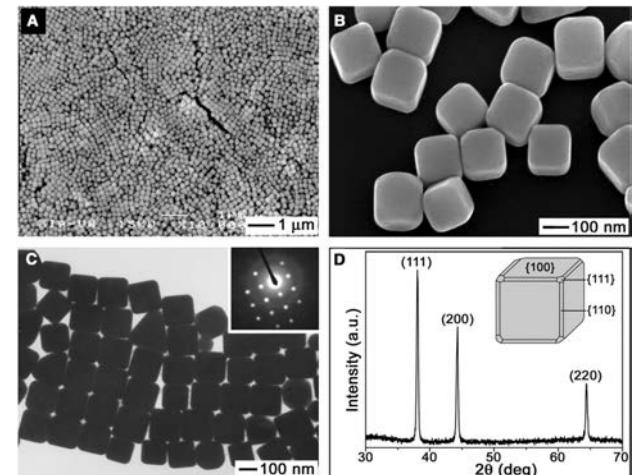
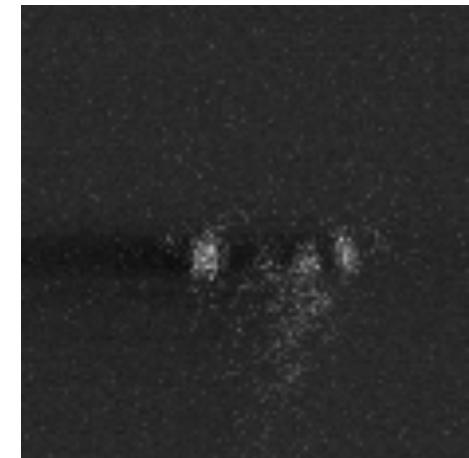
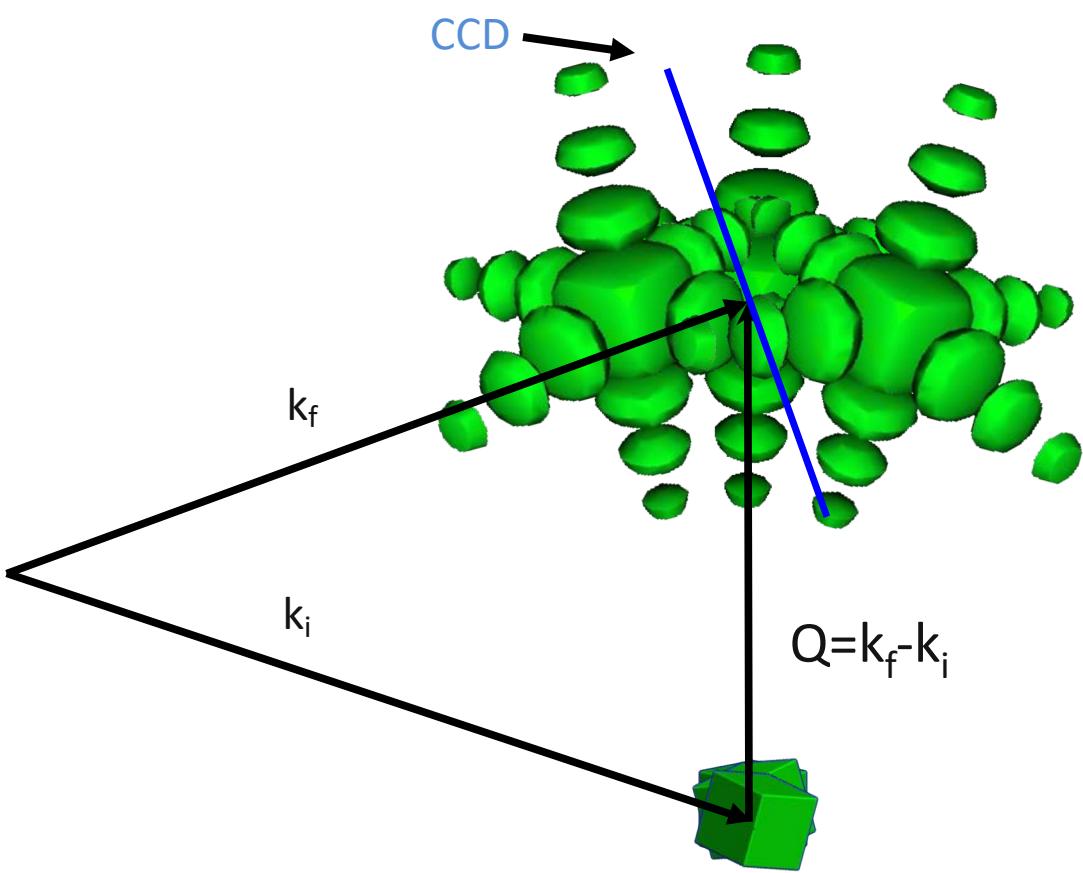


$| \text{Fourier Transform} |^2$



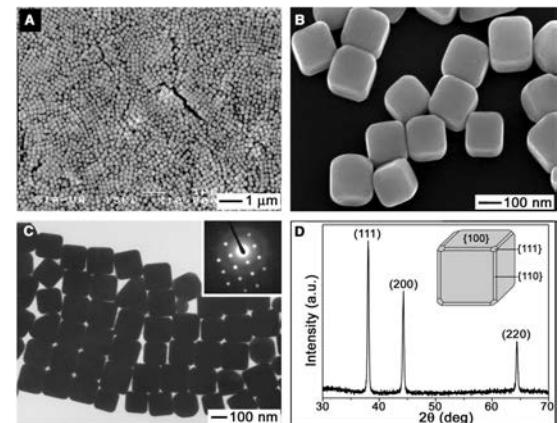
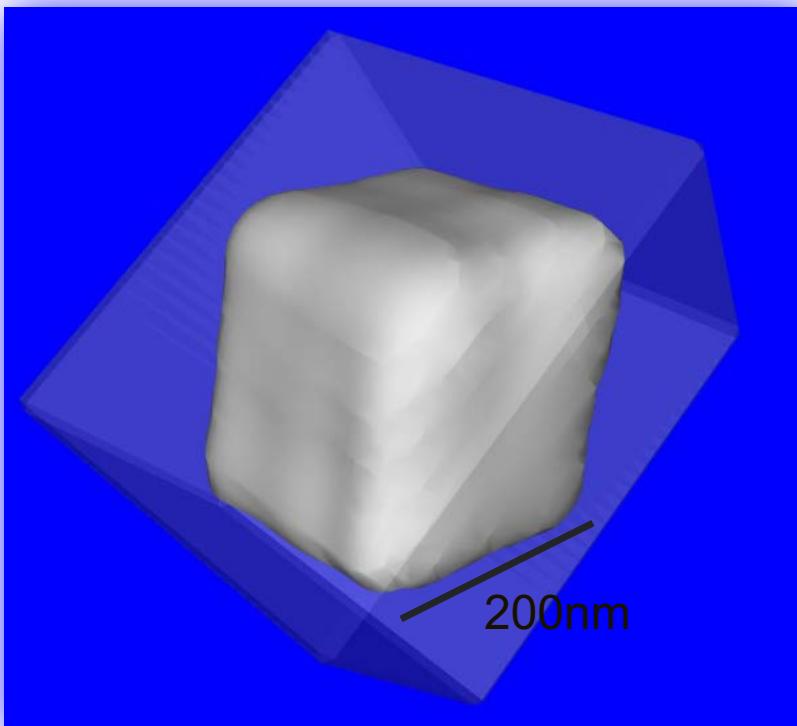
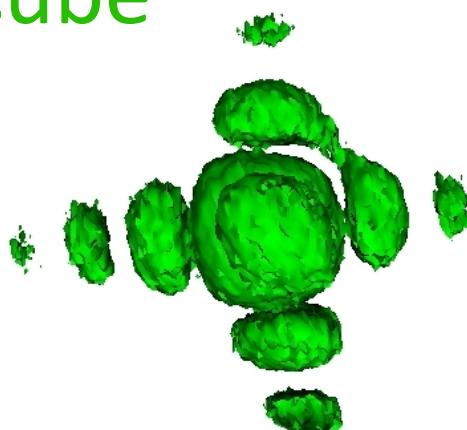
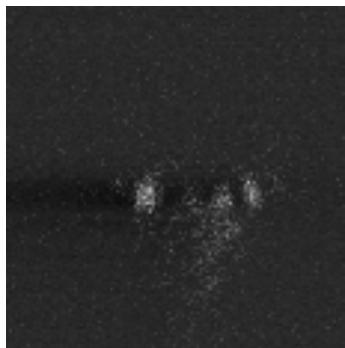
# Measuring 3D CXD

Silver Nano Cube (111)

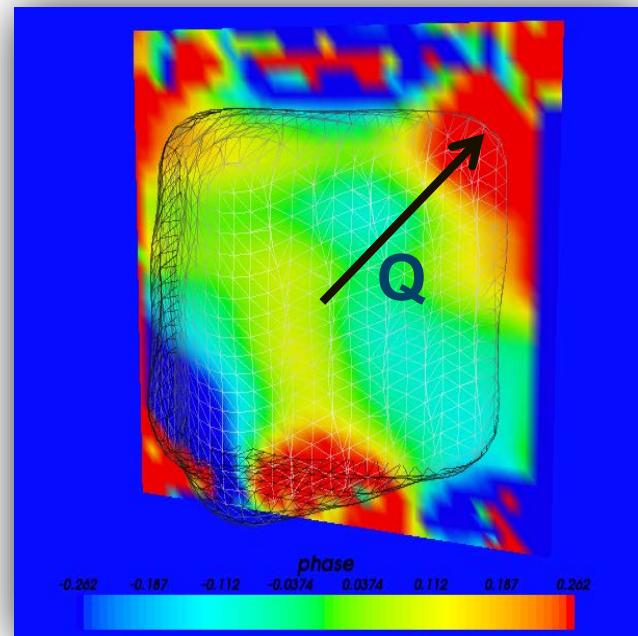


Yugang Sun and Younan Xia,  
Science 298 2177 (2003)

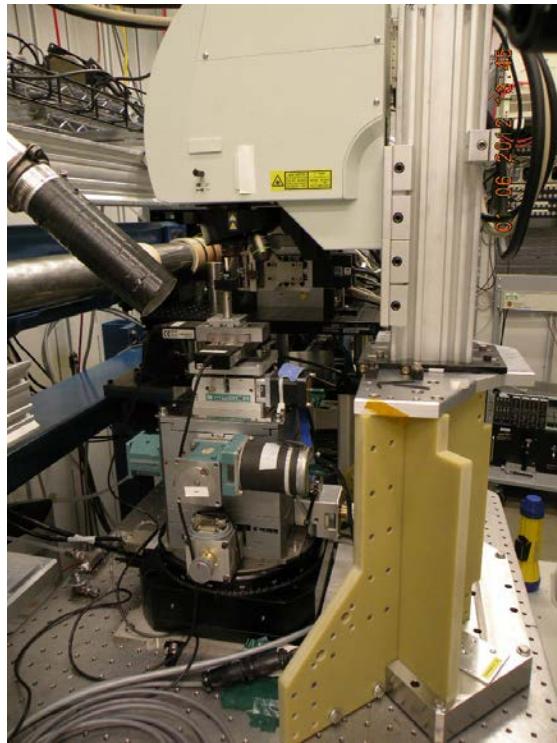
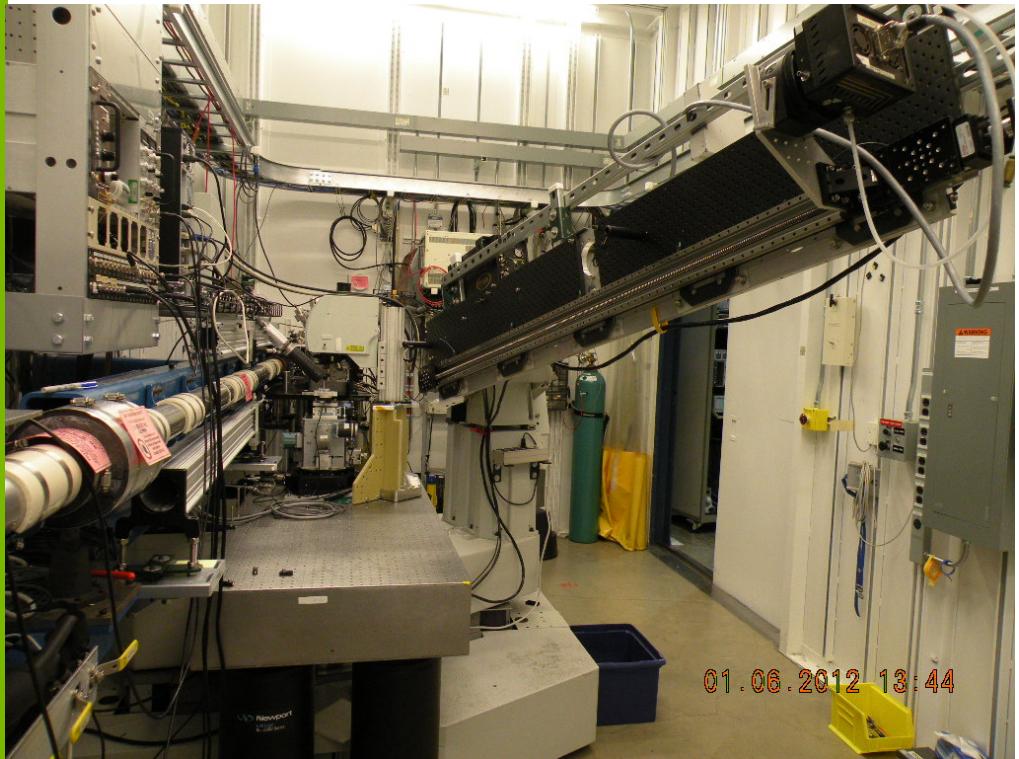
# 3D Ag Nano Cube



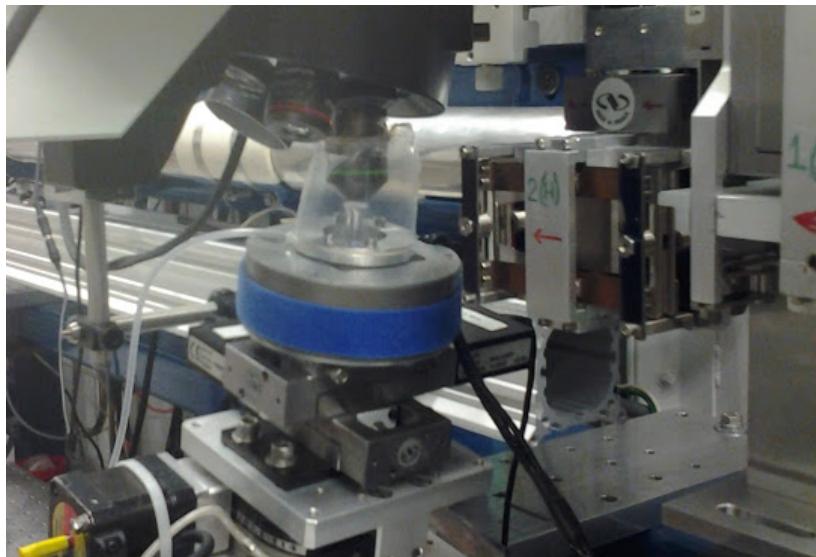
Yugang Sun and Younan Xia,  
Science [298 2177 \(2003\)](#)



# APS 34-ID-C



Precision scanning stage



# ORIGINAL PHASE RETRIEVAL PAPER (BY D. SAYRE):

*Acta Cryst.* (1952). 5, 843

NOT  $\rho = \rho^2$  *Acta Cryst.* (1952). 5, 60

**Some implications of a theorem due to Shannon.** By D. SAYRE, *Johnson Foundation for Medical Physics, University of Pennsylvania, Philadelphia 4, Pennsylvania, U. S. A.*

(Received 3 July 1952)

Shannon (1949), in the field of communication theory, has given the following theorem: If a function  $d(x)$  is known to vanish outside the points  $x = \pm a/2$ , then its Fourier transform  $F(X)$  is completely specified by the values which it assumes at the points  $X = 0, \pm 1/a, \pm 2/a, \dots$ . In fact, the continuous  $F(X)$  may be filled in merely by laying down the function  $\sin \pi aX/\pi aX$  at each of the above points, with weight equal to the value of  $F(X)$  at that point, and adding.

Now the electron-density function  $d(x)$  describing a single unit cell of a crystal vanishes outside the points  $x = \pm a/2$ , where  $a$  is the length of the cell. The reciprocal-lattice points are at  $X = 0, \pm 1/a, \pm 2/a, \dots$ , and hence the experimentally observable values of  $F(X)$  would suffice, by the theorem, to determine  $F(X)$  everywhere, if the phases were known. (In principle, the necessary points extend indefinitely in reciprocal space, but by using, say, Gaussian atoms both  $d(x)$  and  $F(X)$  can be effectively confined to the unit cell and the observable region, respectively.)

For centrosymmetrical structures, to be able to fill in the  $|F|^2$  function would suffice to yield the structure, for sign changes could occur only at the points where  $|F|^2$  vanishes. The structure corresponding to the  $|F|^2$  function is the Patterson of a single unit cell. This has

twice the width of the unit cell, and hence to fill in the  $|F|^2$  function would require knowledge of  $|F|^2$  at the half-integral, as well as the integral  $h$ 's. This is equivalent to a statement made by Gay (1951).

I think the conclusions which may be stated at this point are:

1. Direct structure determination, for centrosymmetric structures, could be accomplished as well by finding the sizes of the  $|F|^2$  at half-integral  $h$  as by the usual procedure of finding the signs of the  $F$ 's at integral  $h$ .

2. In work like that of Boyes-Watson, Davidson & Perutz (1947) on haemoglobin, where  $|F|^2$  was observed at non-integral  $h$ , it would suffice to have only the values at half-integral  $h$ .

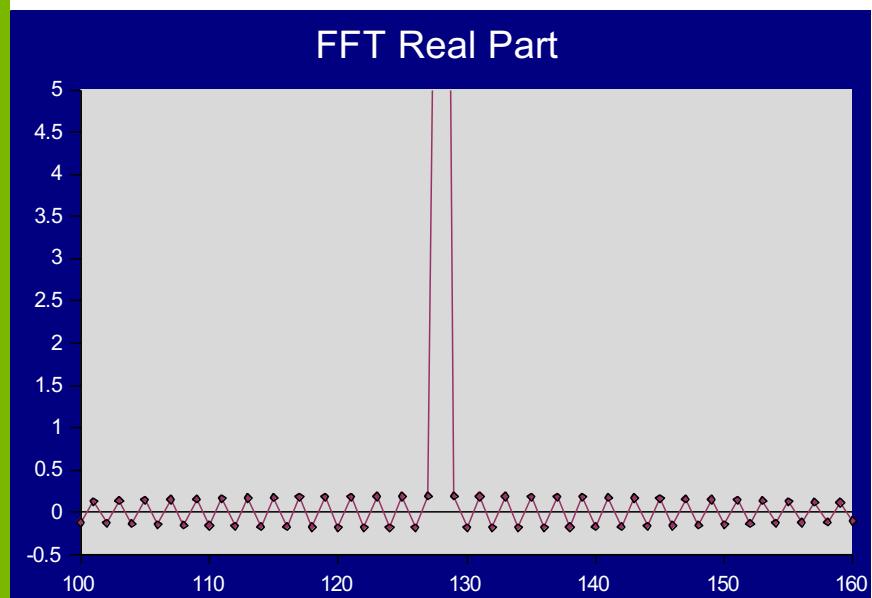
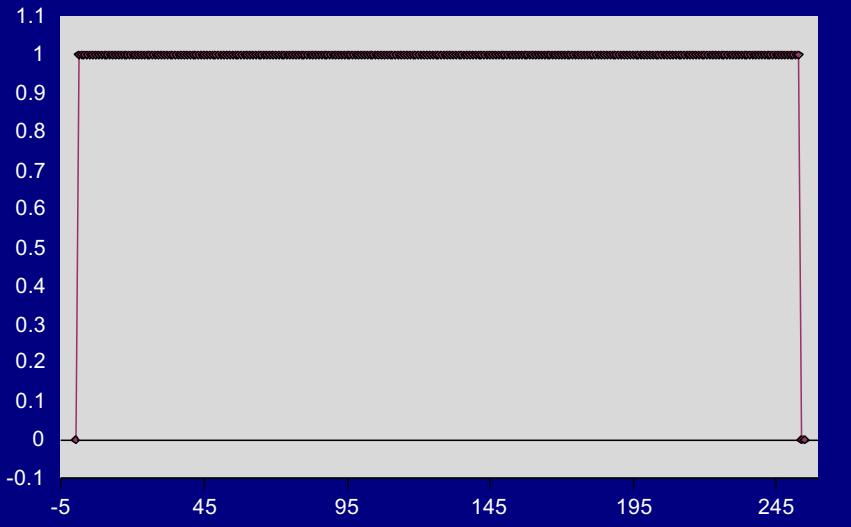
The extension to three dimensions is obvious.

## References

- BOYES-WATSON, J., DAVIDSON, E. & PERUTZ, M. F. (1947). *Proc. Roy. Soc. A*, **191**, 83.  
GAY, R. (1951). Paper presented at the Second International Congress of Crystallography, Stockholm.  
SHANNON, C. E. (1949). *Proc. Inst. Radio Engrs., N.Y.* **37**, 10.

# Critical sampling

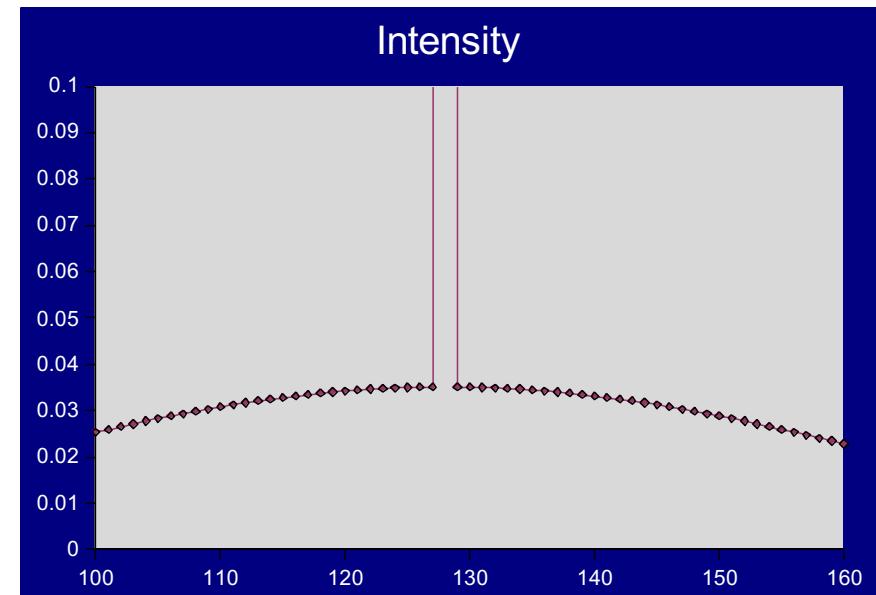
Object



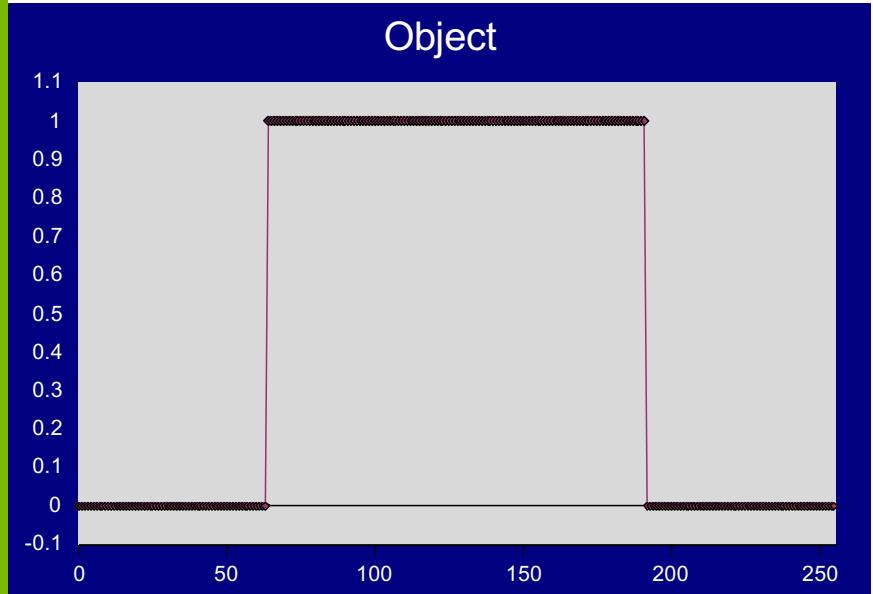
N unknown densities  
N/2 equations

$$|A_q| = \left| \sum_0^N \rho_n e^{-iqr_n} \right|$$

Nyquist Freq = 1/(2\*bandwidth)  
Intensity is under sampled

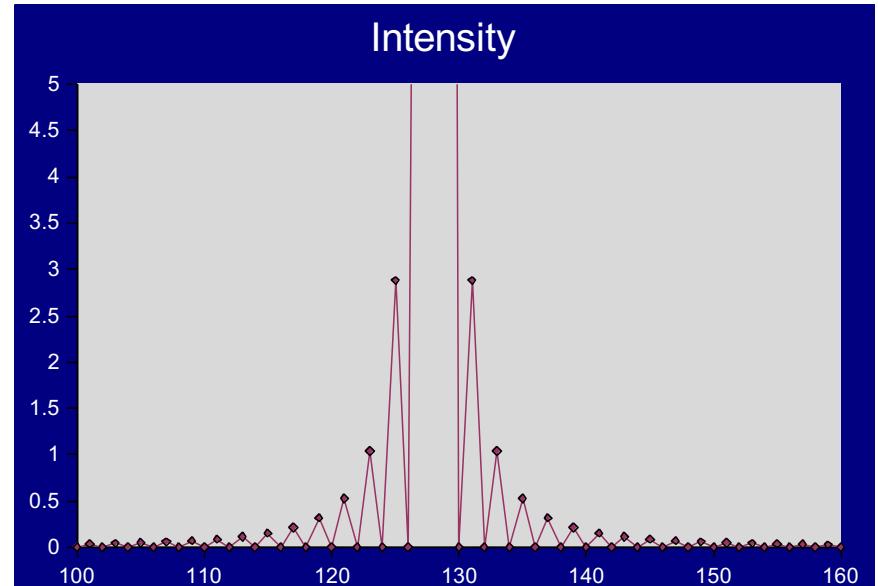
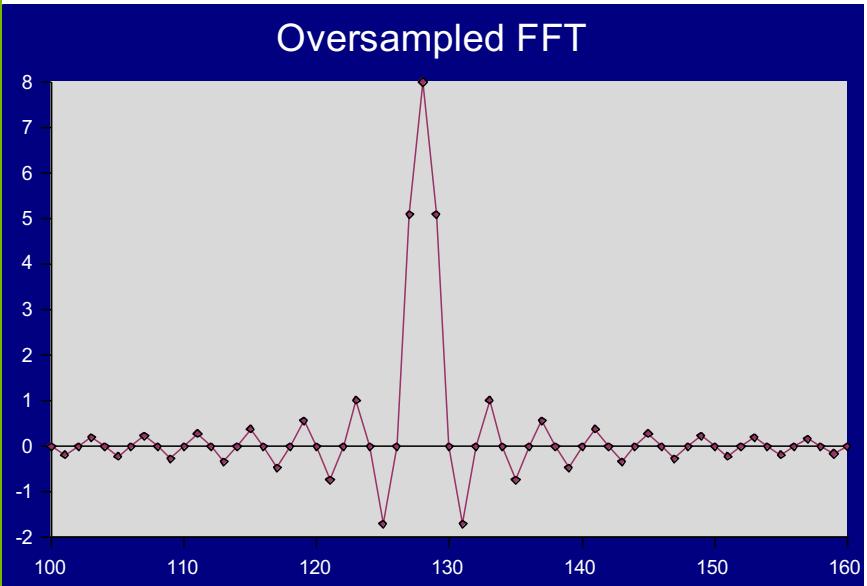


# Oversampling 2x

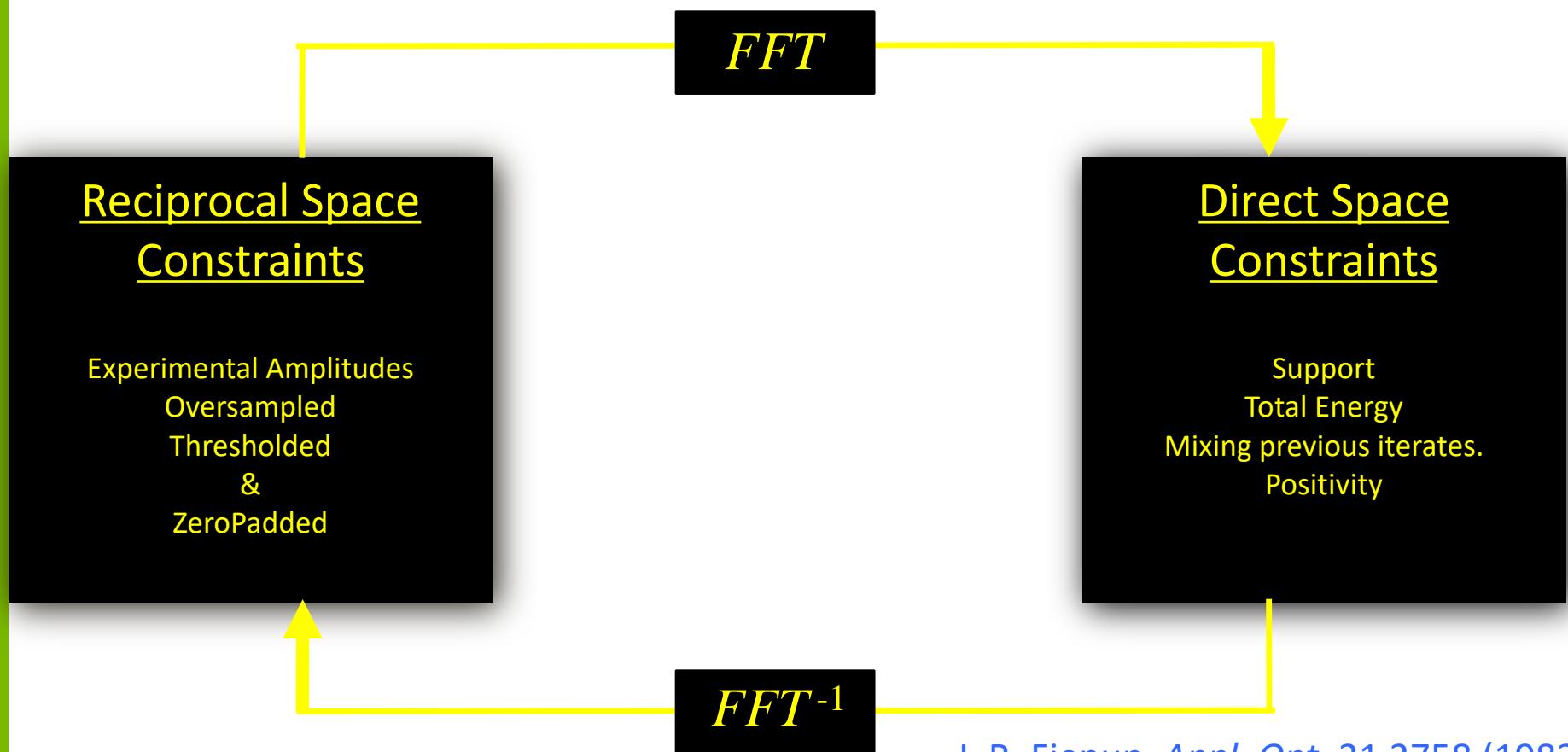


N/2 equations  
N/2 Unknown densities  
N/2 Known Densities(zero)

$$|A_q| = \left| \sum_0^N \rho_n e^{-iqr_n} \right|$$



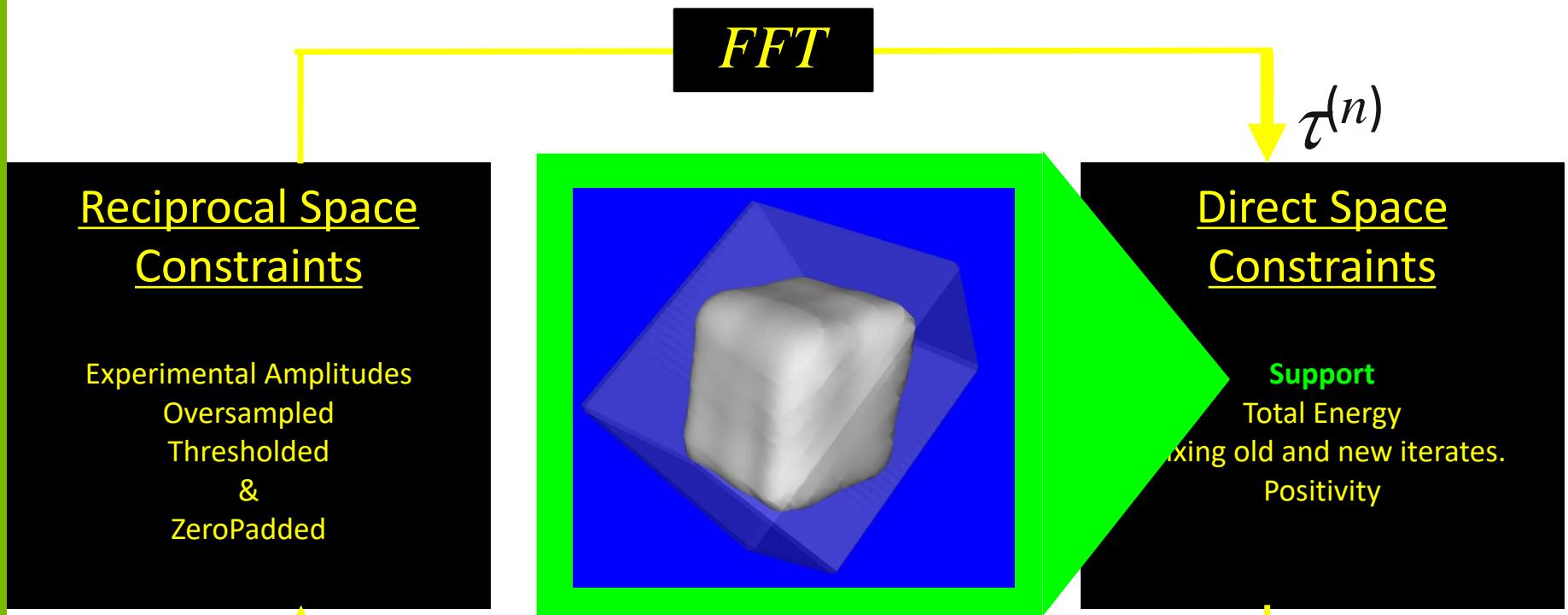
# Input Output Algorithms



J. R. Fienup *Appl. Opt.* 21 2758 (1982)  
Collins *Nature* 298, 49 (1982)

R. W. Gerchberg and W. O. Saxton *Optik* 35 237 (1972)  
Fienup, James R. 2013. "Phase Retrieval Algorithms: a  
Personal Tour." *Applied Optics* 52 (1): 45–56.

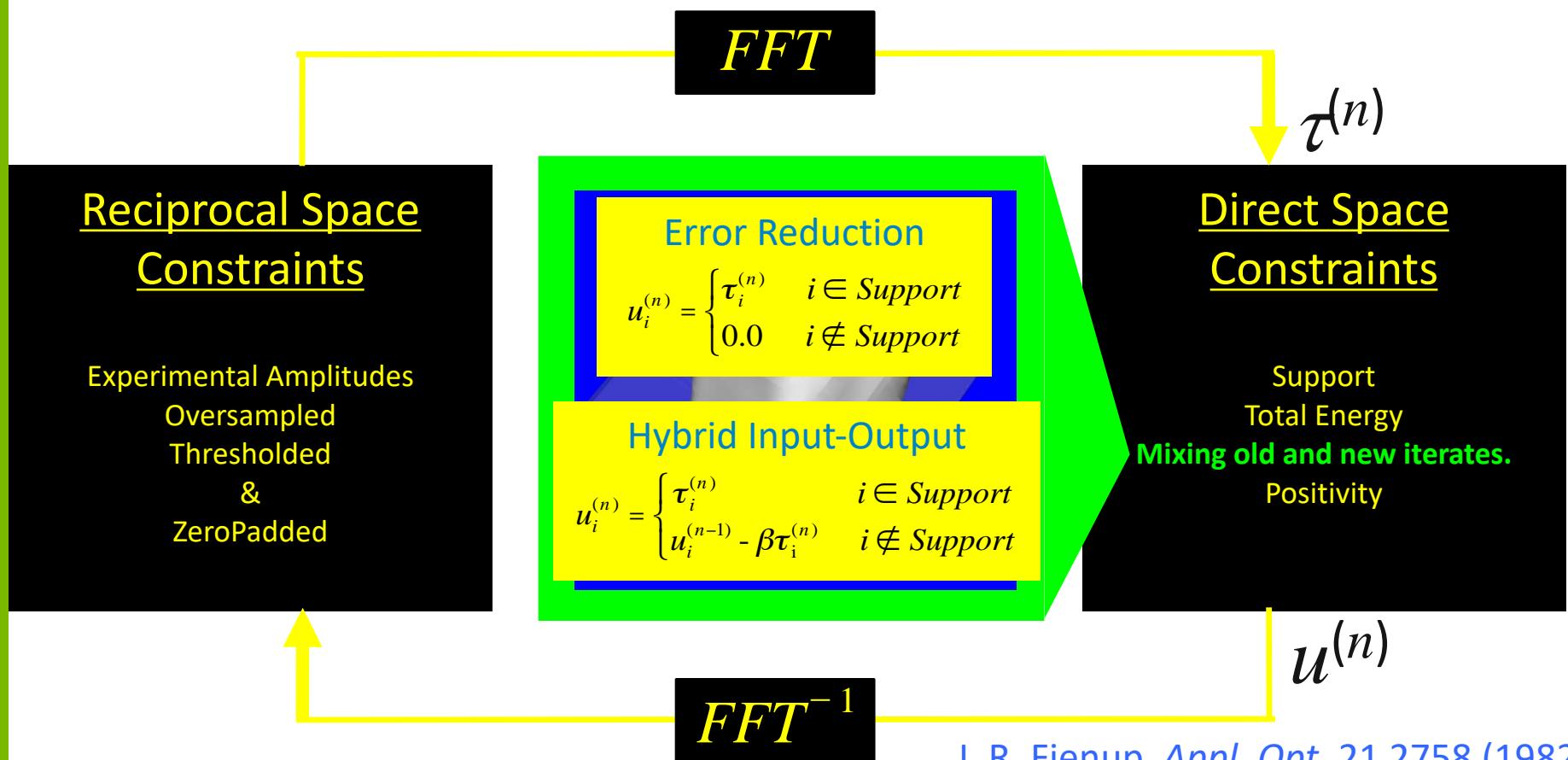
# Input Output Algorithms



J. R. Fienup *Appl. Opt.* **21** 2758 (1982)  
Collins *Nature* **298**, 49 (1982)

R. W. Gerchberg and W. O. Saxton *Optik* **35** 237 (1972)  
Fienup, James R. 2013. "Phase Retrieval Algorithms: a  
Personal Tour." *Applied Optics* **52** (1): 45–56.

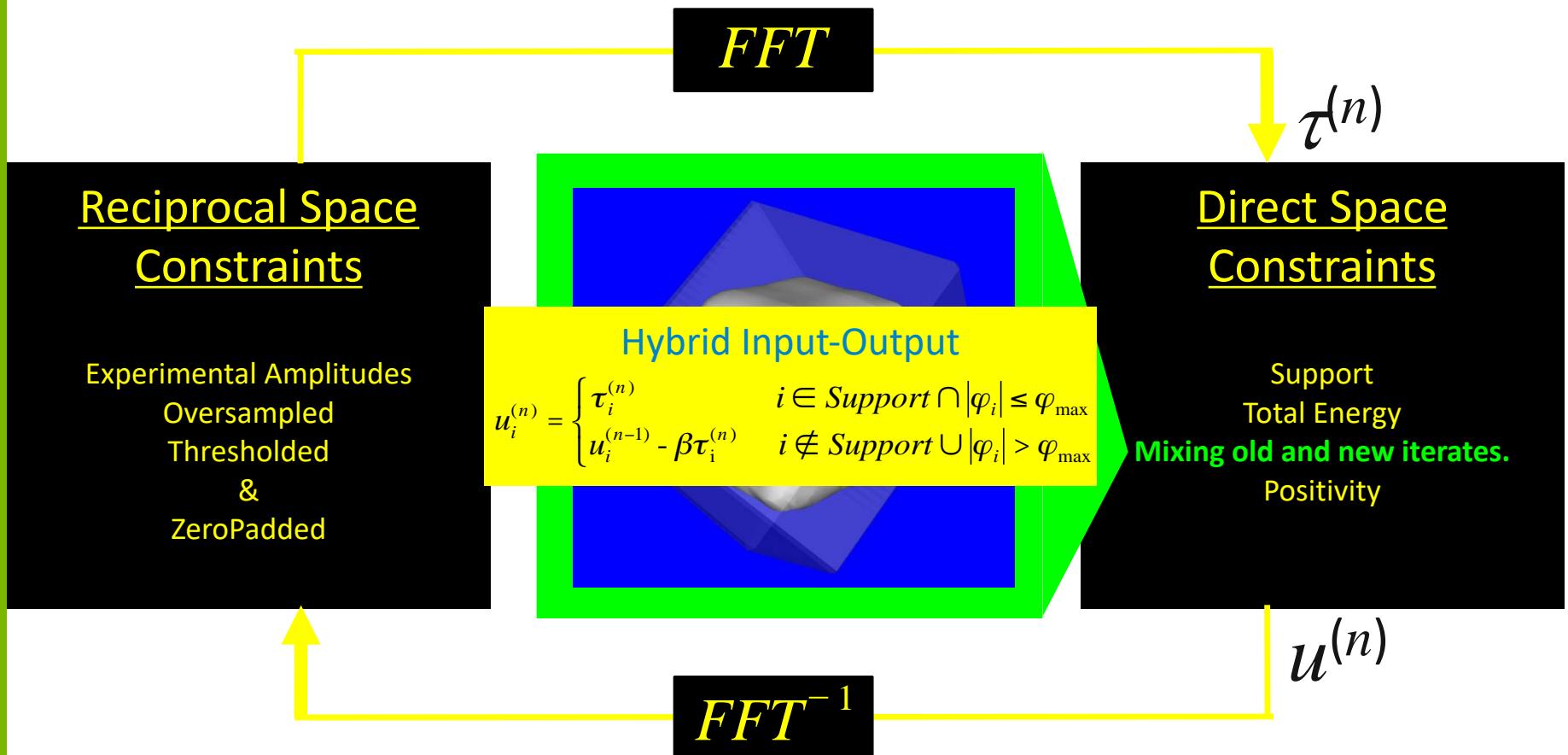
# Input Output Algorithms



J. R. Fienup *Appl. Opt.* **21** 2758 (1982)  
Collins *Nature* **298**, 49 (1982)

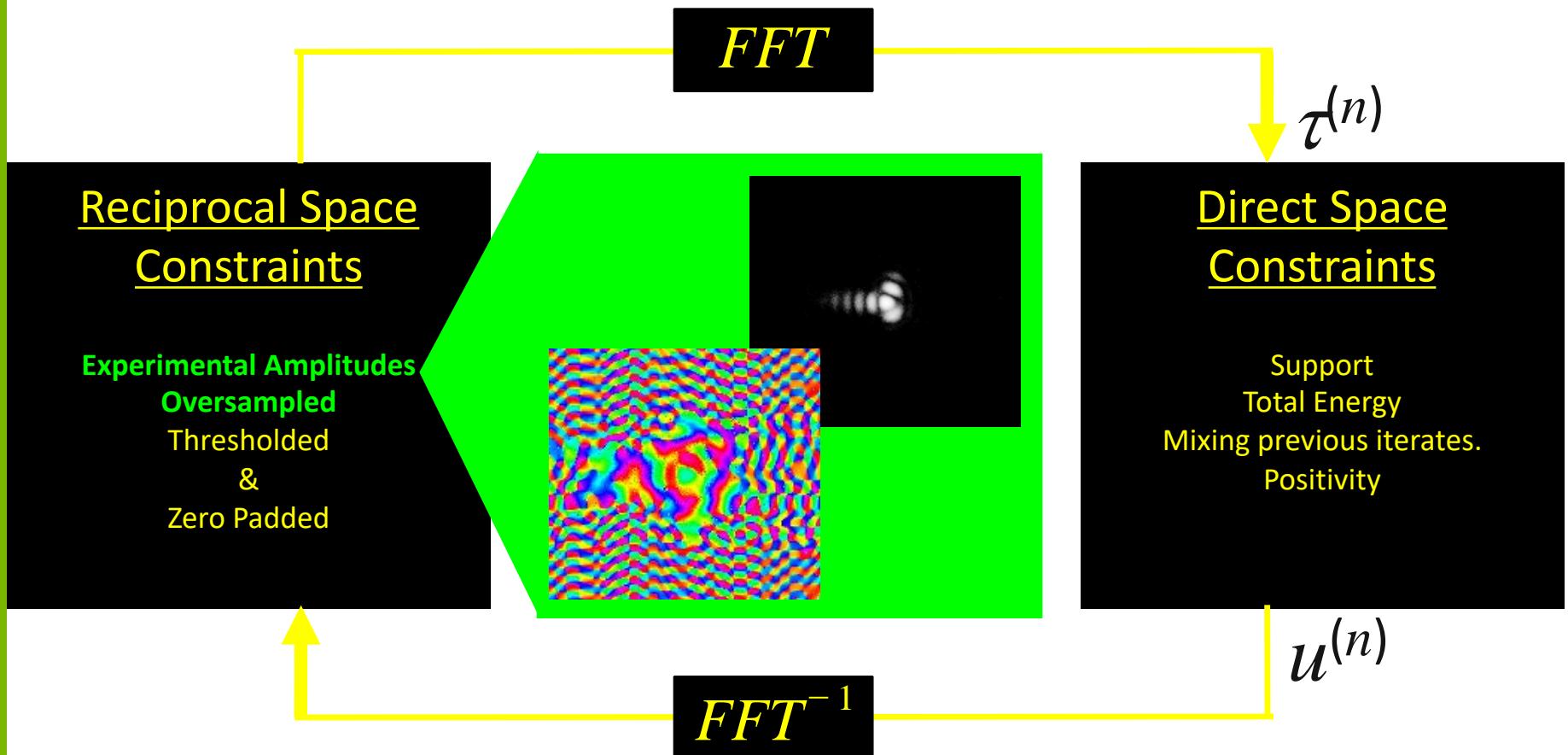
R. W. Gerchberg and W. O. Saxton *Optik* **35** 237 (1972)  
Fienup, James R. 2013. "Phase Retrieval Algorithms: a Personal Tour." *Applied Optics* **52** (1): 45–56.

# Input Output Algorithms



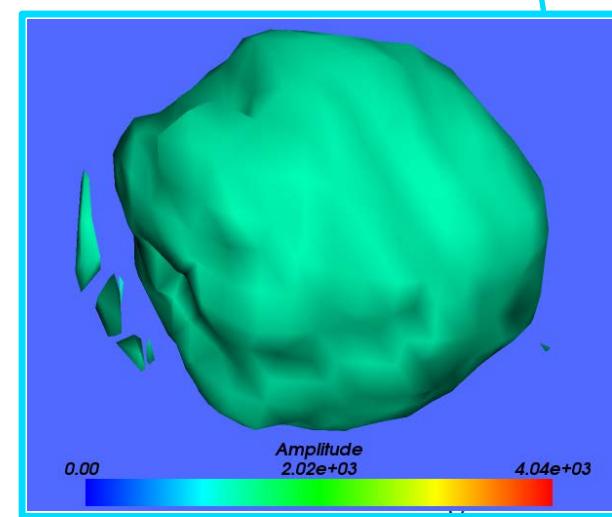
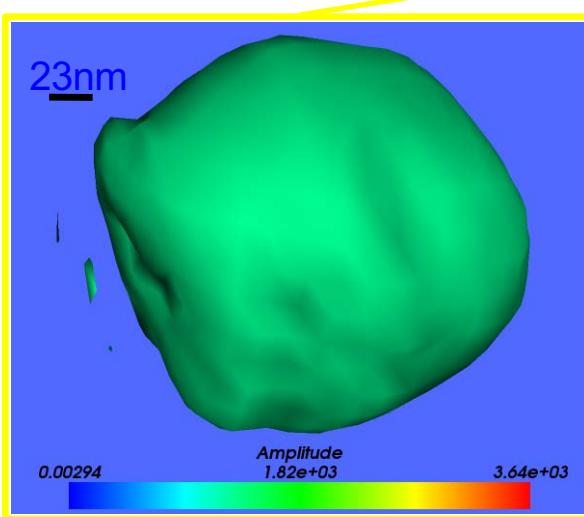
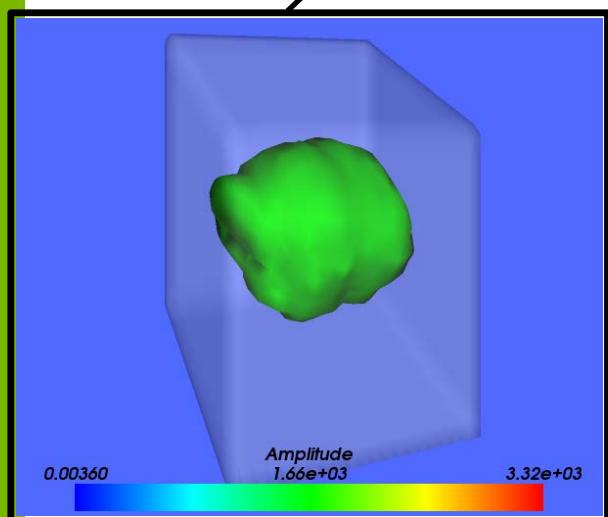
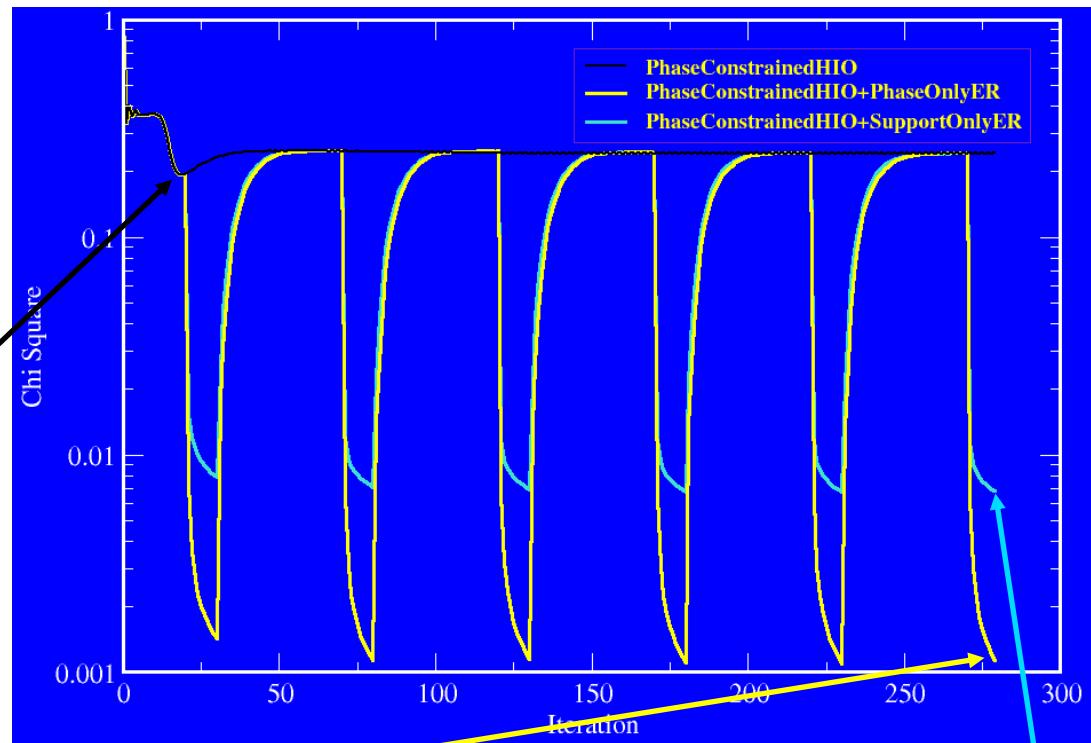
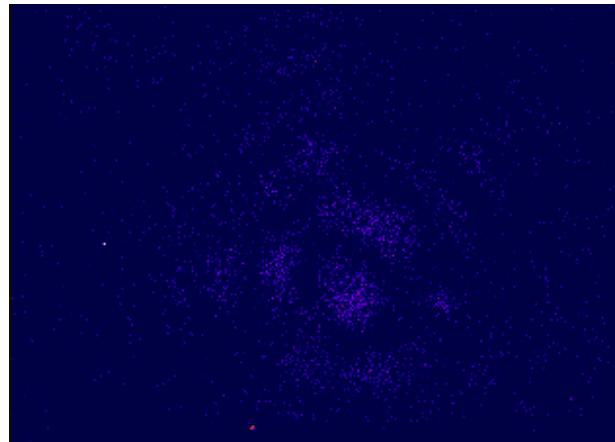
- Harder, R., Liang, M., Sun, Y., Xia, Y., & Robinson, I. K. (2010). Imaging of complex density in silver nanocubes by coherent x-ray diffraction. *New Journal of Physics*, 12(3), 035019.
- Huang, X., Harder, R., Xiong, G., Shi, X., & Robinson, I. (2011). Propagation uniqueness in three-dimensional coherent diffractive imaging. *Physical Review B*, 83(22), 224109.

# Input Output Algorithms

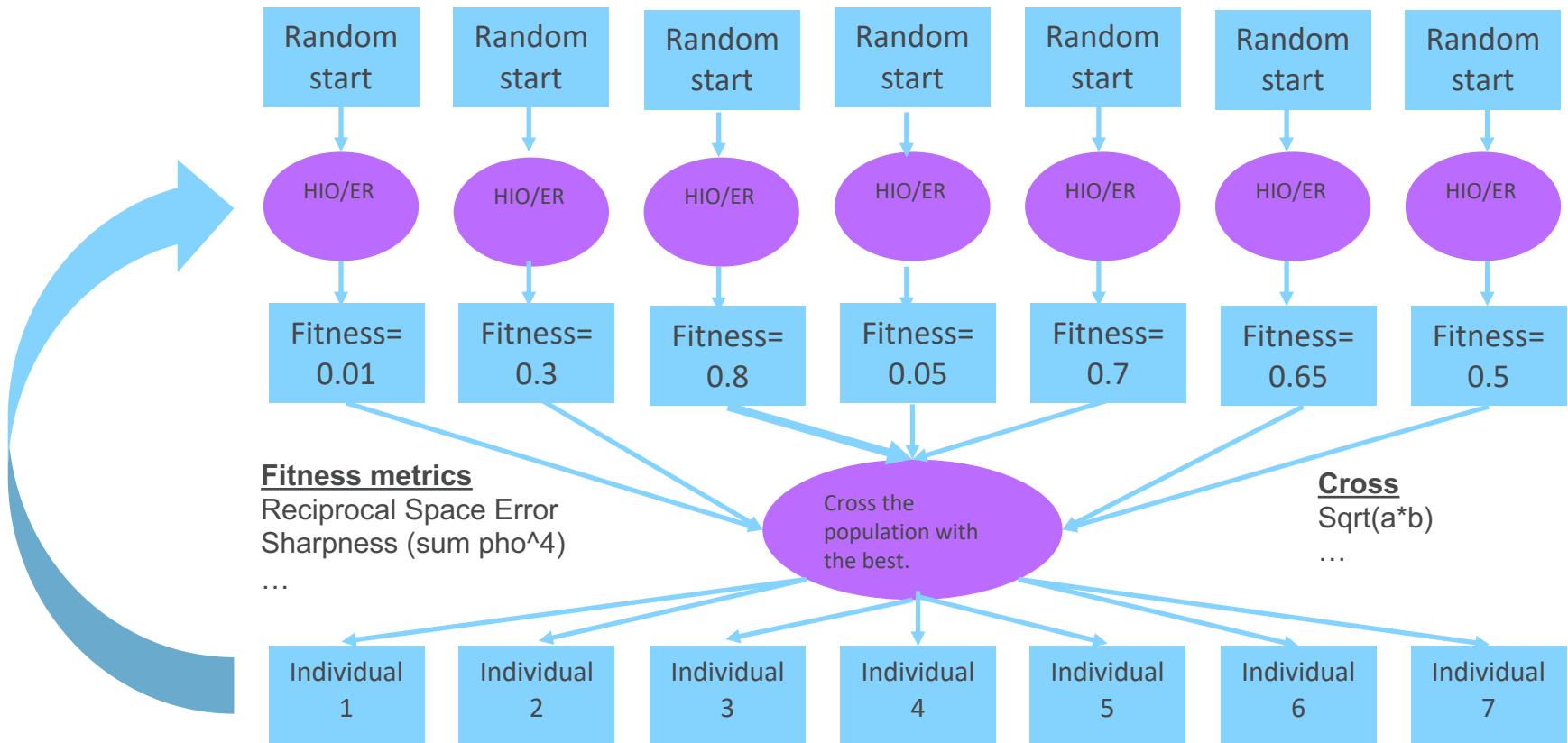


- Harder, R., Liang, M., Sun, Y., Xia, Y., & Robinson, I. K. (2010). Imaging of complex density in silver nanocubes by coherent x-ray diffraction. *New Journal of Physics*, 12(3), 035019.
- Huang, X., Harder, R., Xiong, G., Shi, X., & Robinson, I. (2011). Propagation uniqueness in three-dimensional coherent diffractive imaging. *Physical Review B*, 83(22), 224109.

# Monitor Reciprocal Space Error



# GENETIC/GUIDED ALGORITHM



Clark, J. N., Ihli, J., Schenk, A. S., Kim, Y.-Y., Kulak, A. N., Campbell, J. M., et al. (2015). Three-dimensional imaging of dislocation propagation during crystal growth and dissolution. *Nature Materials*, 14(8), 780–784. <http://doi.org/10.1038/nmat4320>

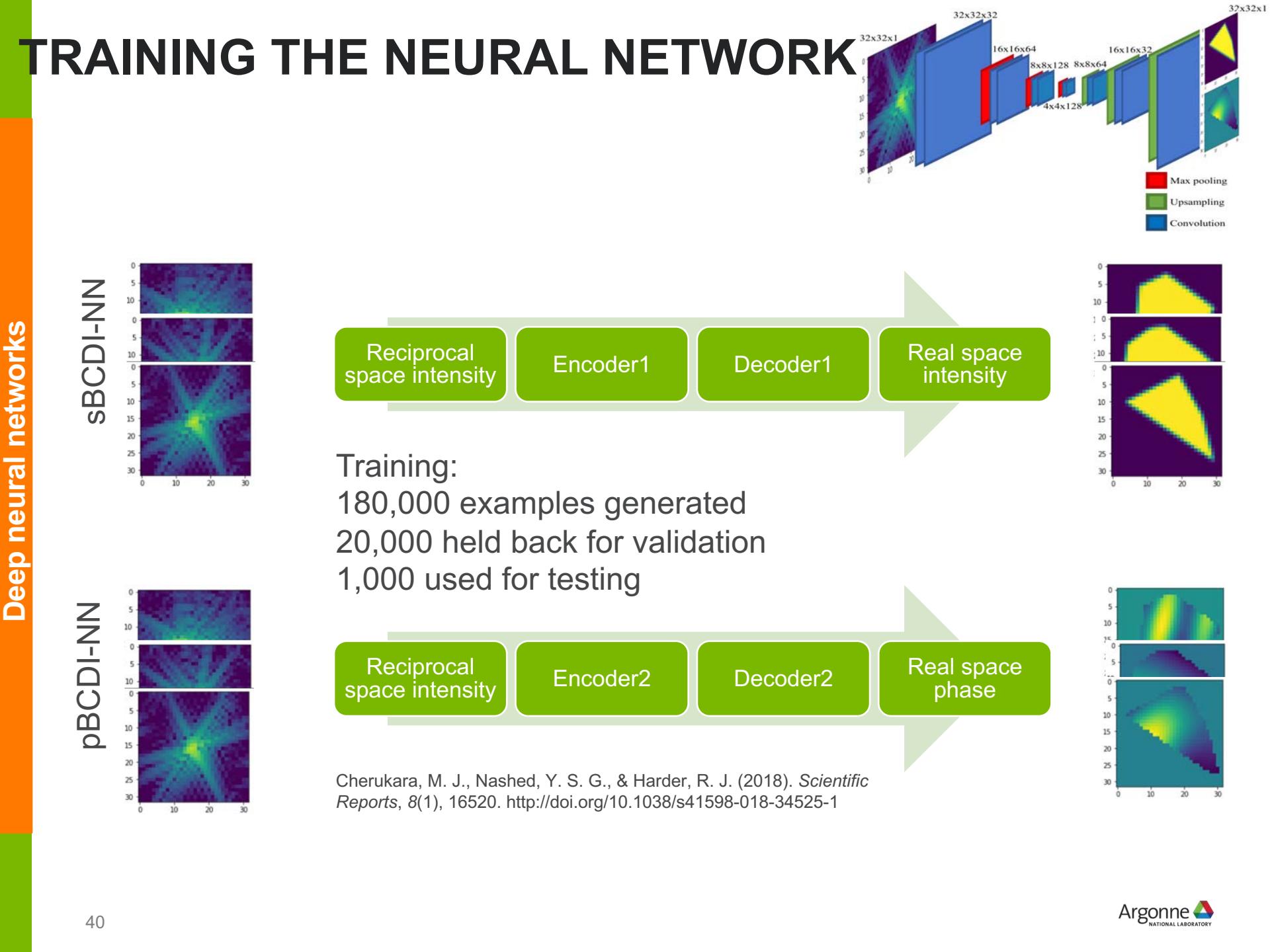
Clark, J. N., Huang, X., Harder, R., & Robinson, I. K. (2012). High-resolution three-dimensional partially coherent diffraction imaging. *Nature Communications*, 3, 993–. <http://doi.org/10.1038/ncomms1994>



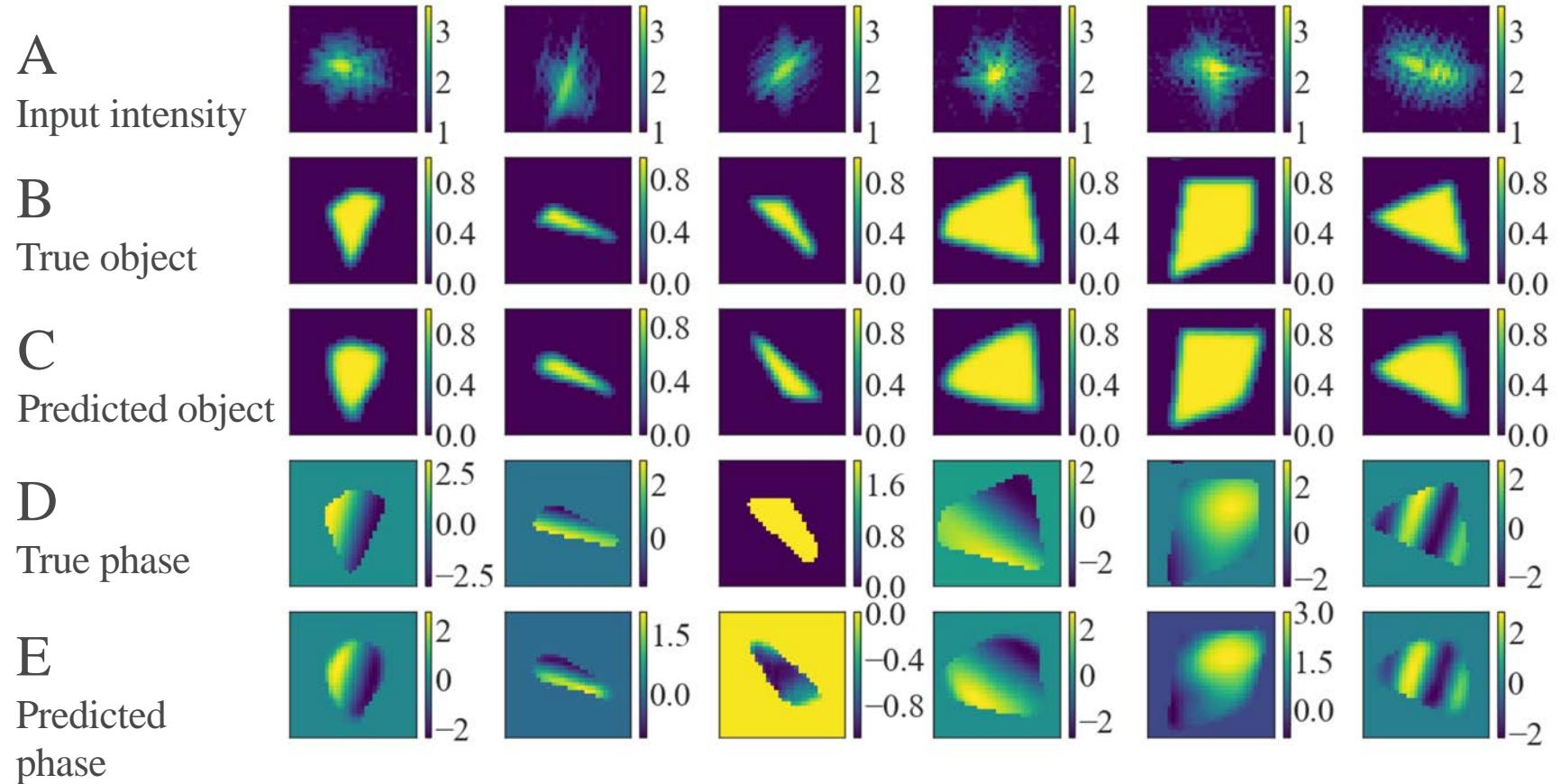
# A.I. CDI

Atomistically Informed Coherent Diffraction Imaging

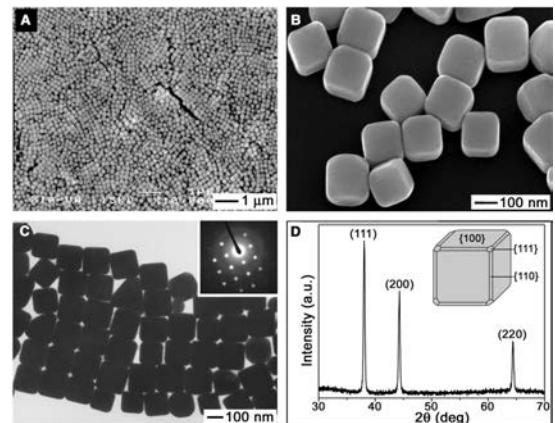
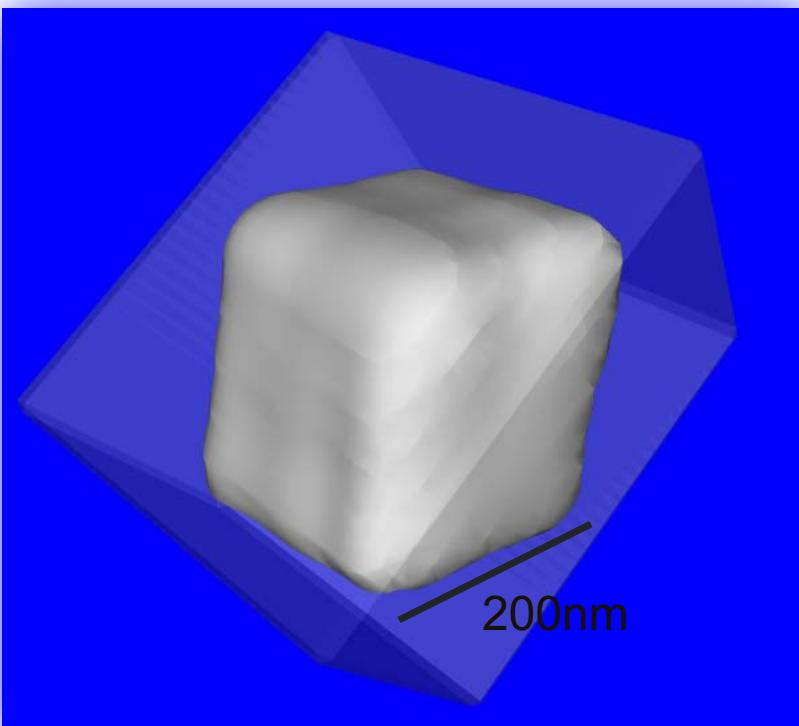
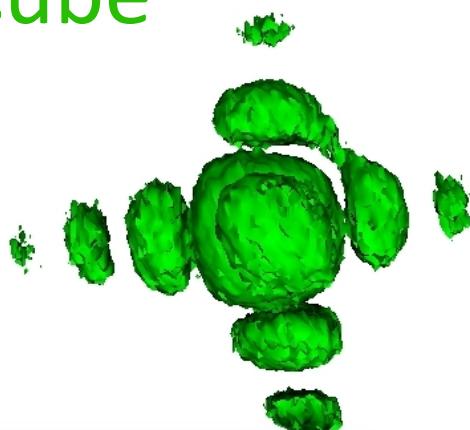
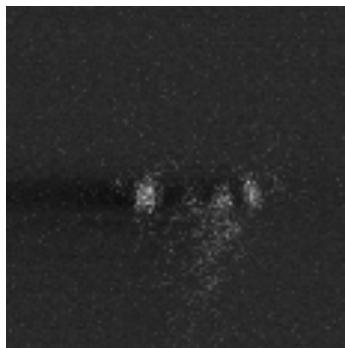
ROSS J. HARDER (XSD)  
MATHEW J. CHERUKARA (XSD)  
YOUSSEF NASHED (MCS)  
TOM PETERKA (MCS)  
PRASANNA BALAPRAKASH (MCS)  
S. SANKARANARAYANAN (CNM)  
BADRI NARAYANAN (MSD)



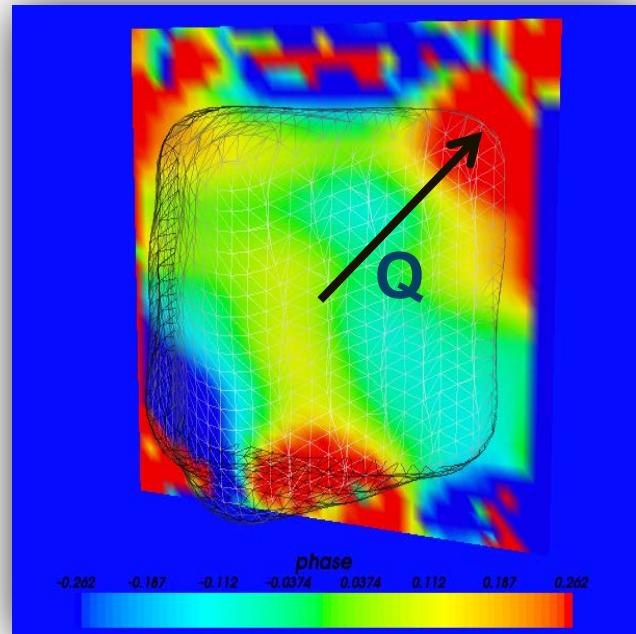
# NEURAL NETWORK THAT **LEARNS** IMAGE RECONSTRUCTION



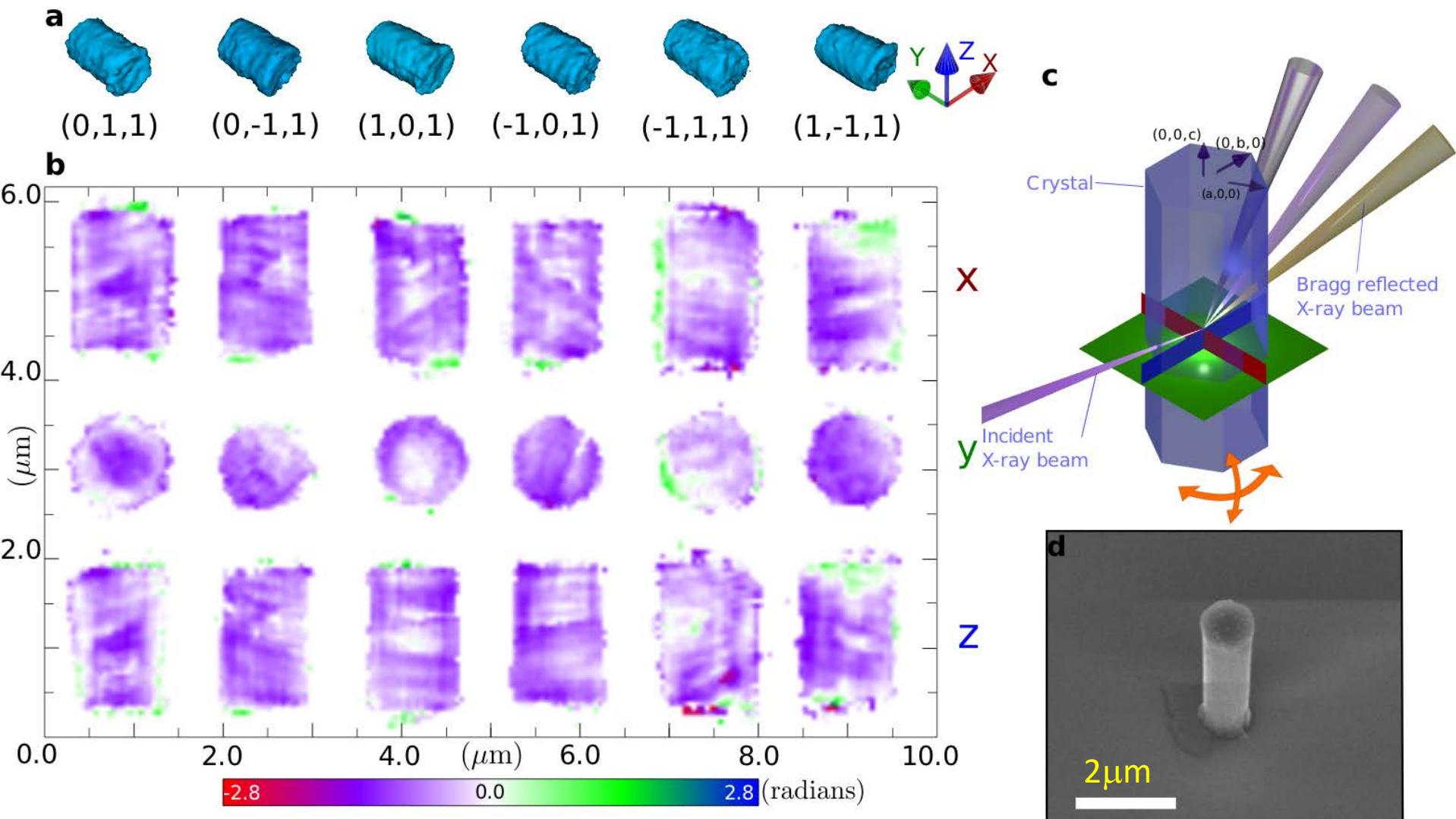
# 3D Ag Nano Cube



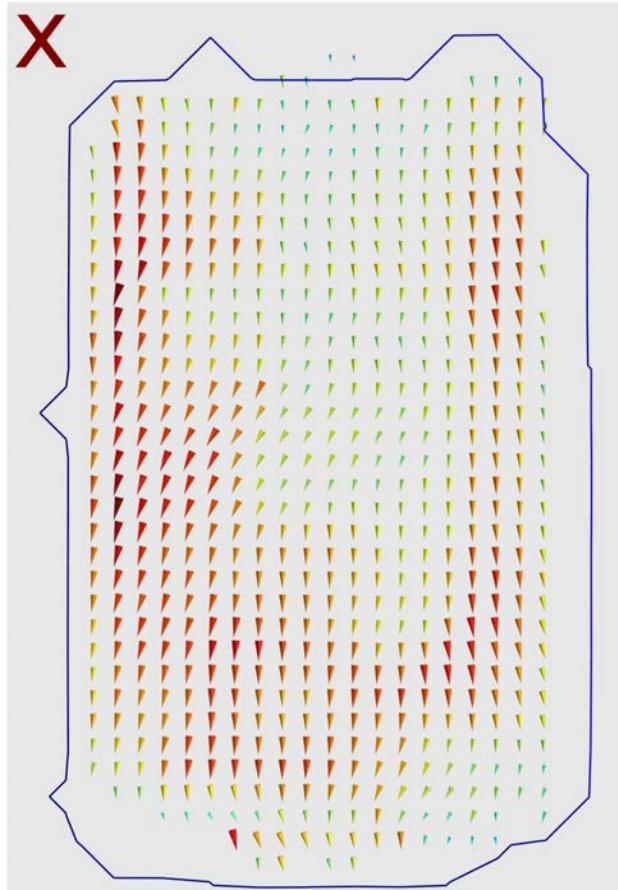
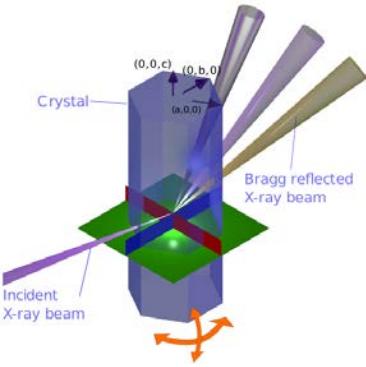
Yugang Sun and Younan Xia,  
Science [298](#) 2177 (2003)



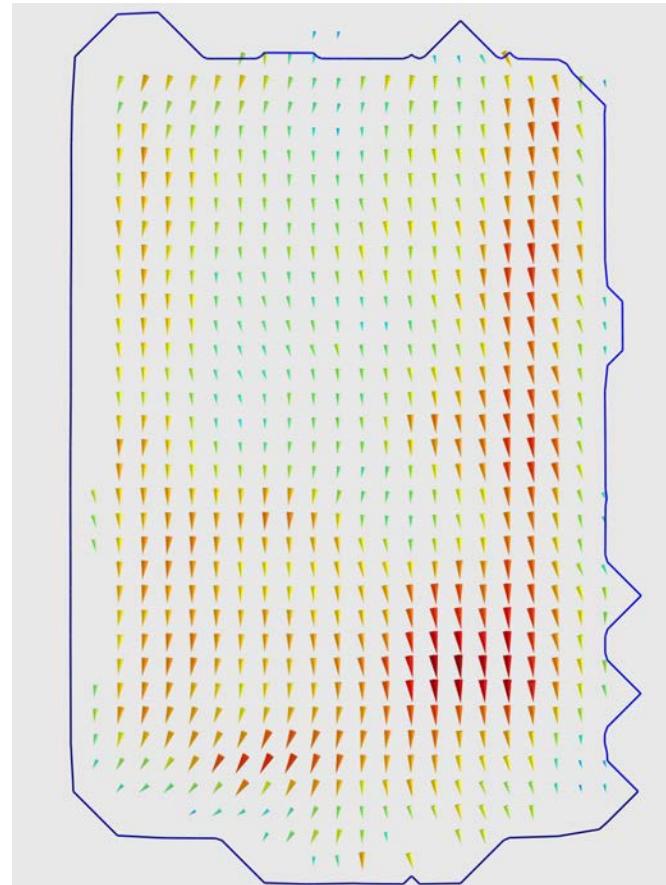
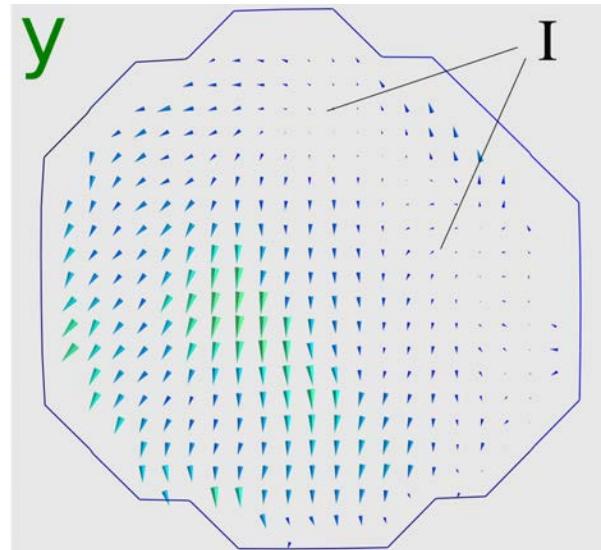
# 3D Strain Map in ZnO



# 3D Strain Map in ZnO

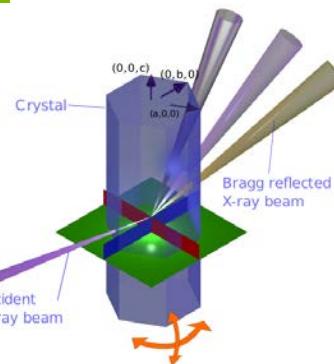


$$u_j = \xi_{ji} q_{ki} \phi_k; \quad \xi_{ji} = (q_{kj} q_{ki})^{-1}$$

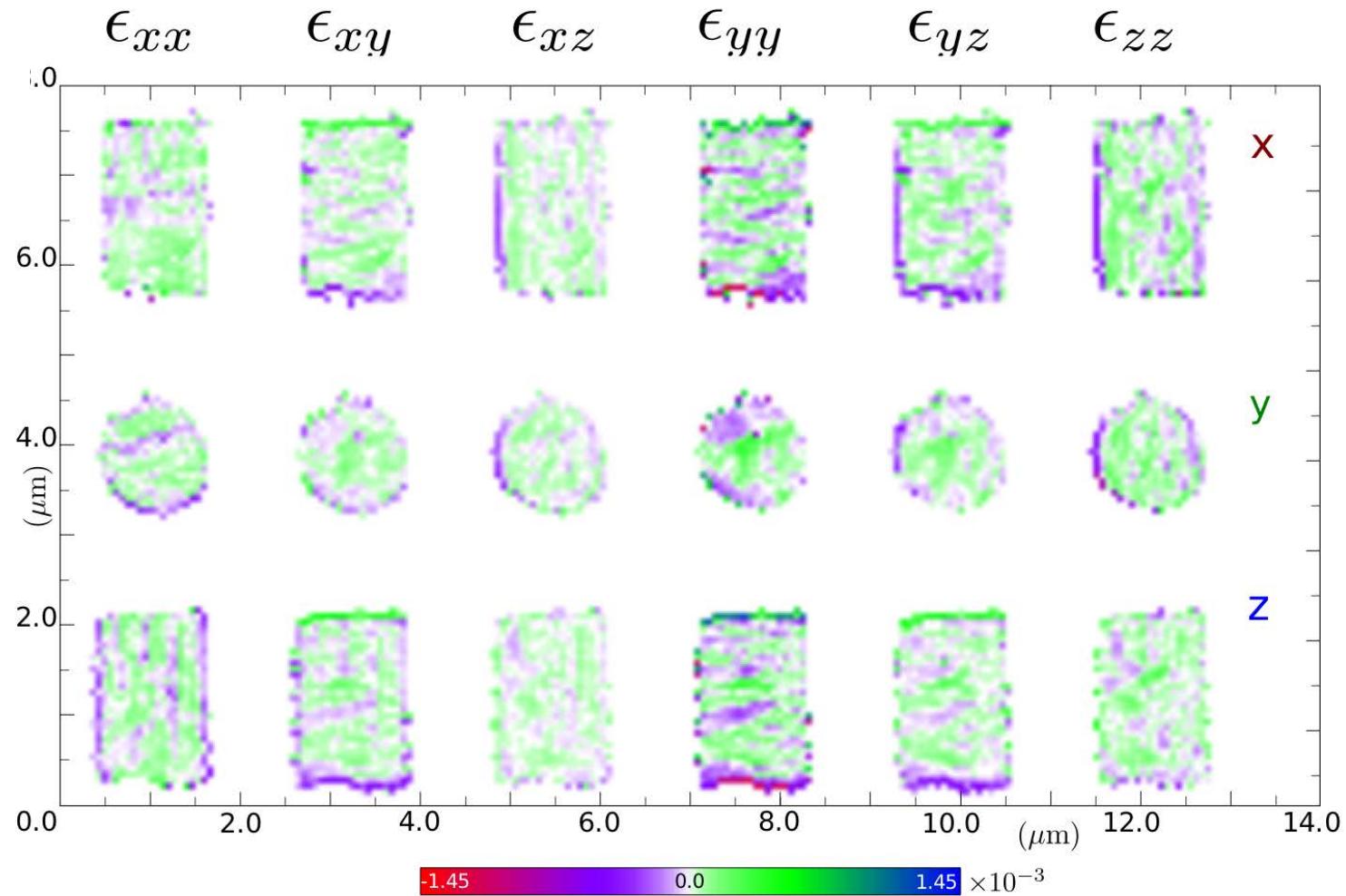


0.0 0.09 nm

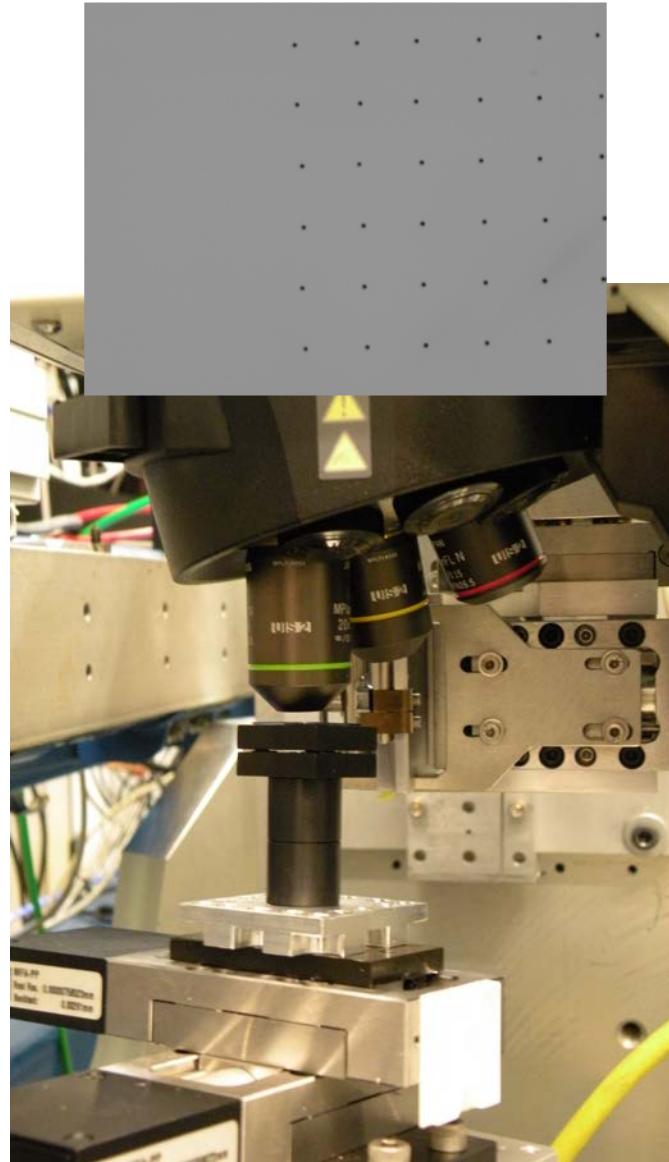
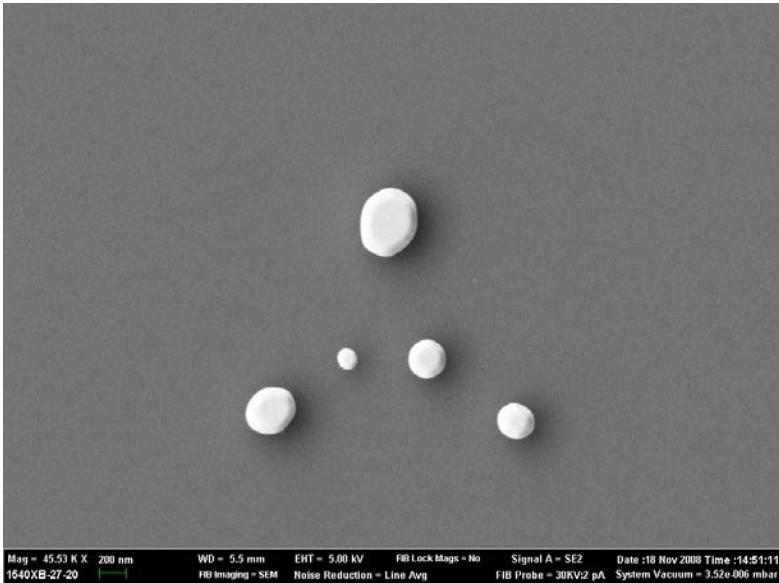
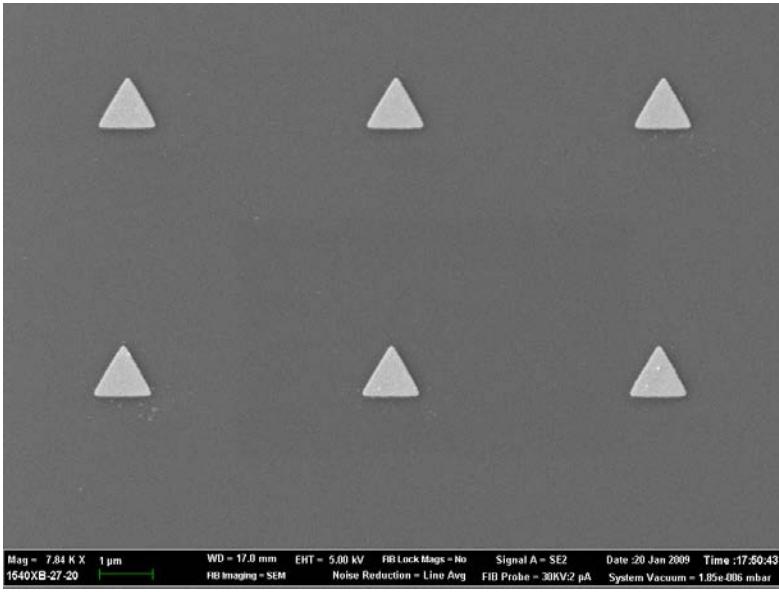
# 3D Strain Map in ZnO



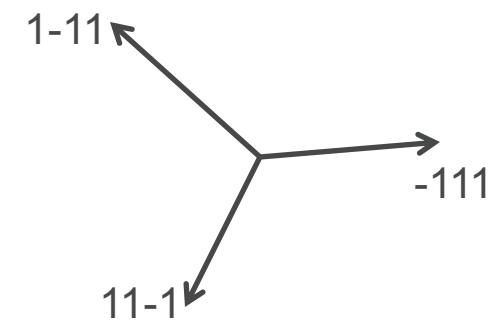
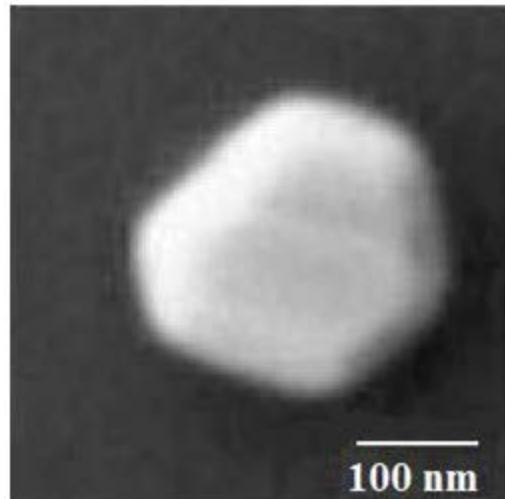
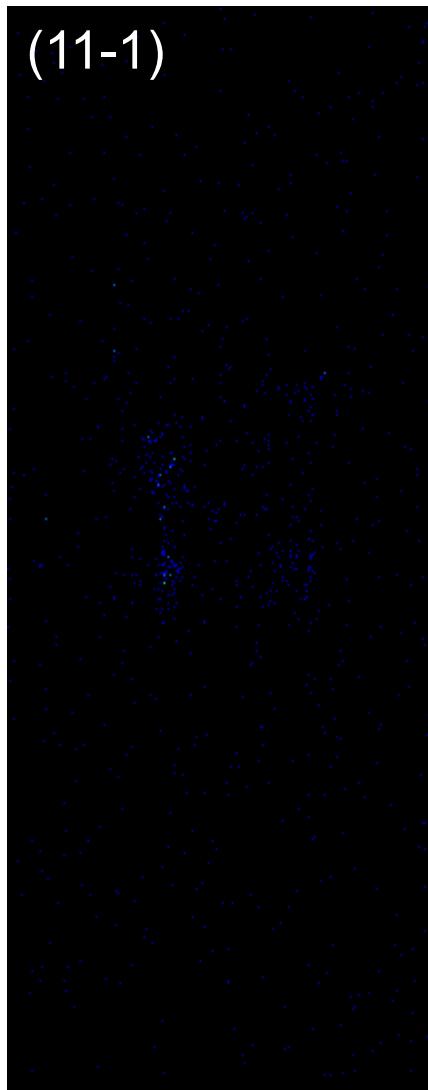
$$\epsilon_{ij} = \frac{1}{2} \left( \frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right), \quad \tau_{ij} = \left( \frac{\partial u_j}{\partial x_i} - \frac{\partial u_i}{\partial x_j} \right)$$



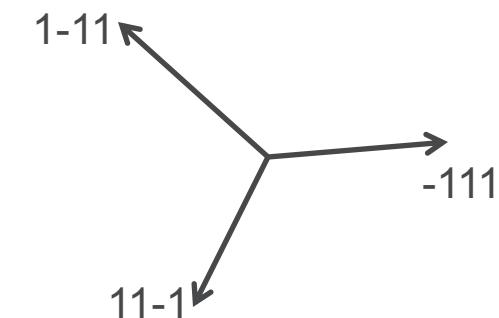
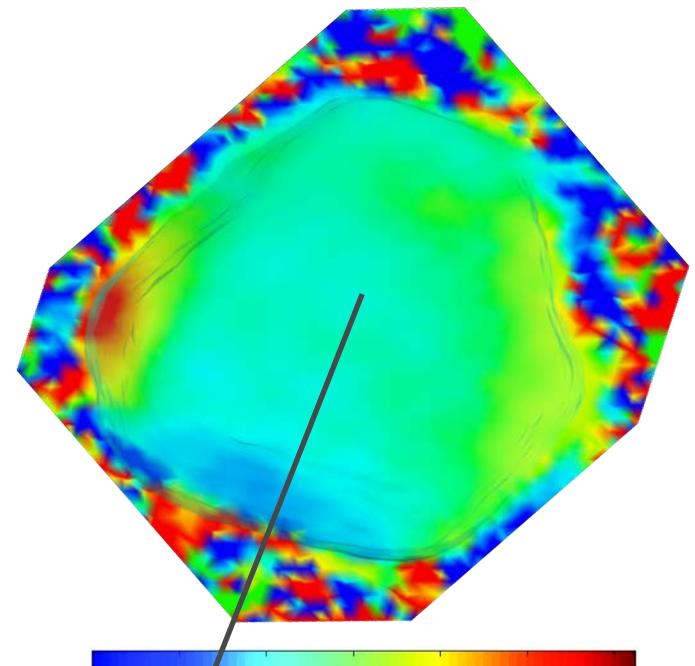
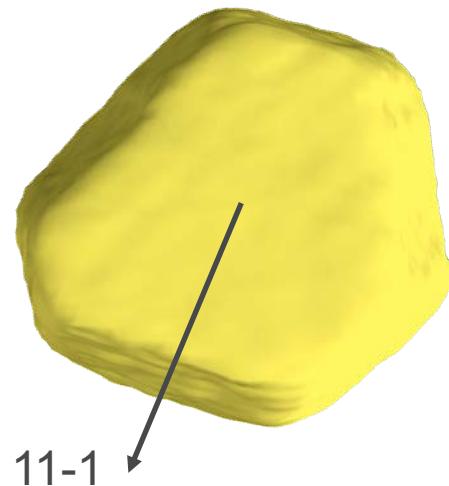
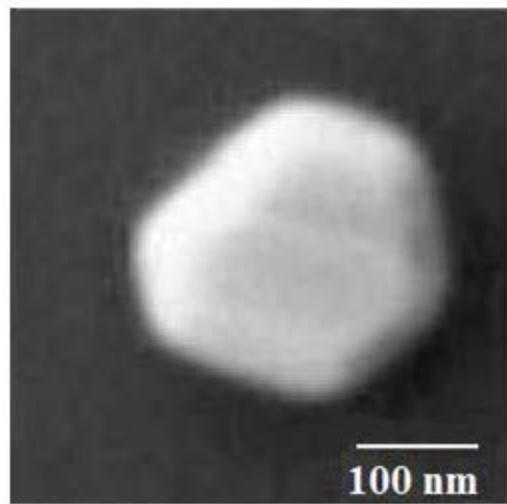
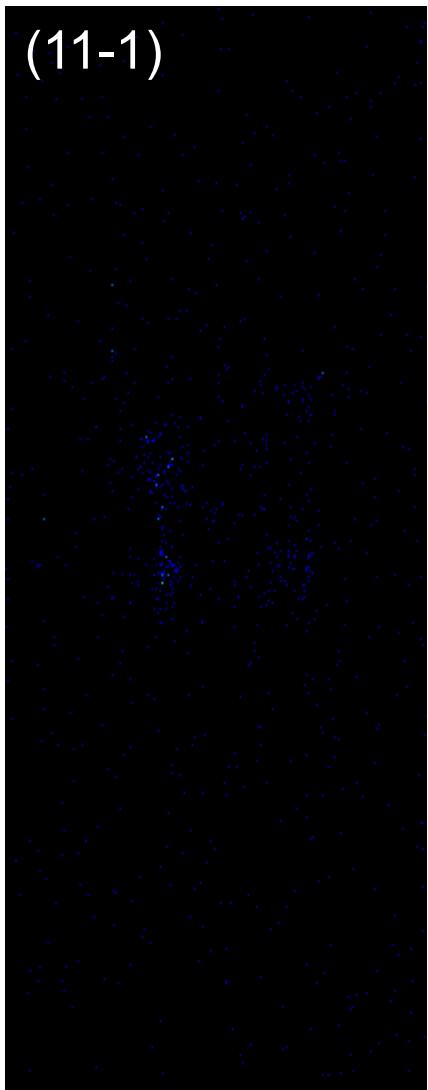
# Patterned Gold Nanocrystal Samples



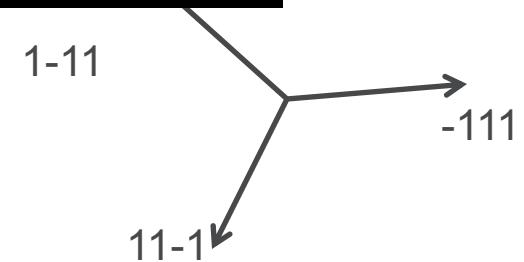
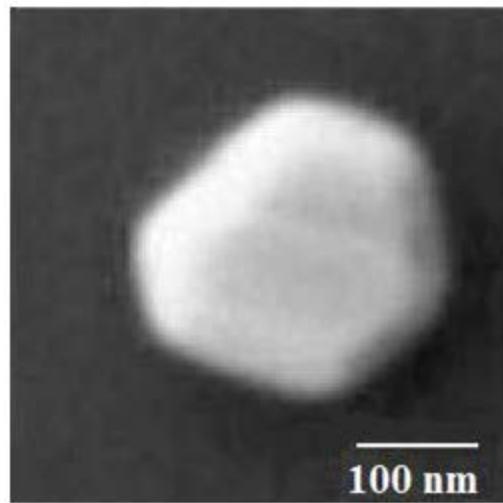
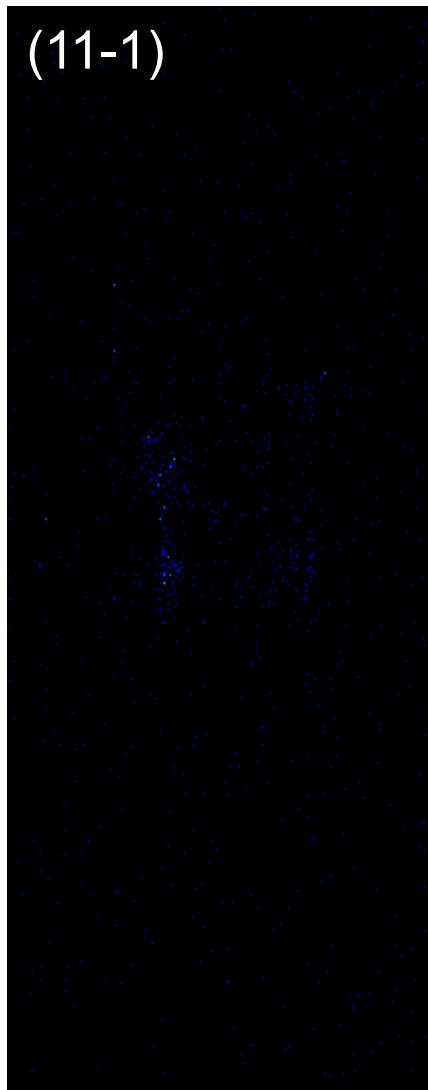
# Multiple reflection reconstructions



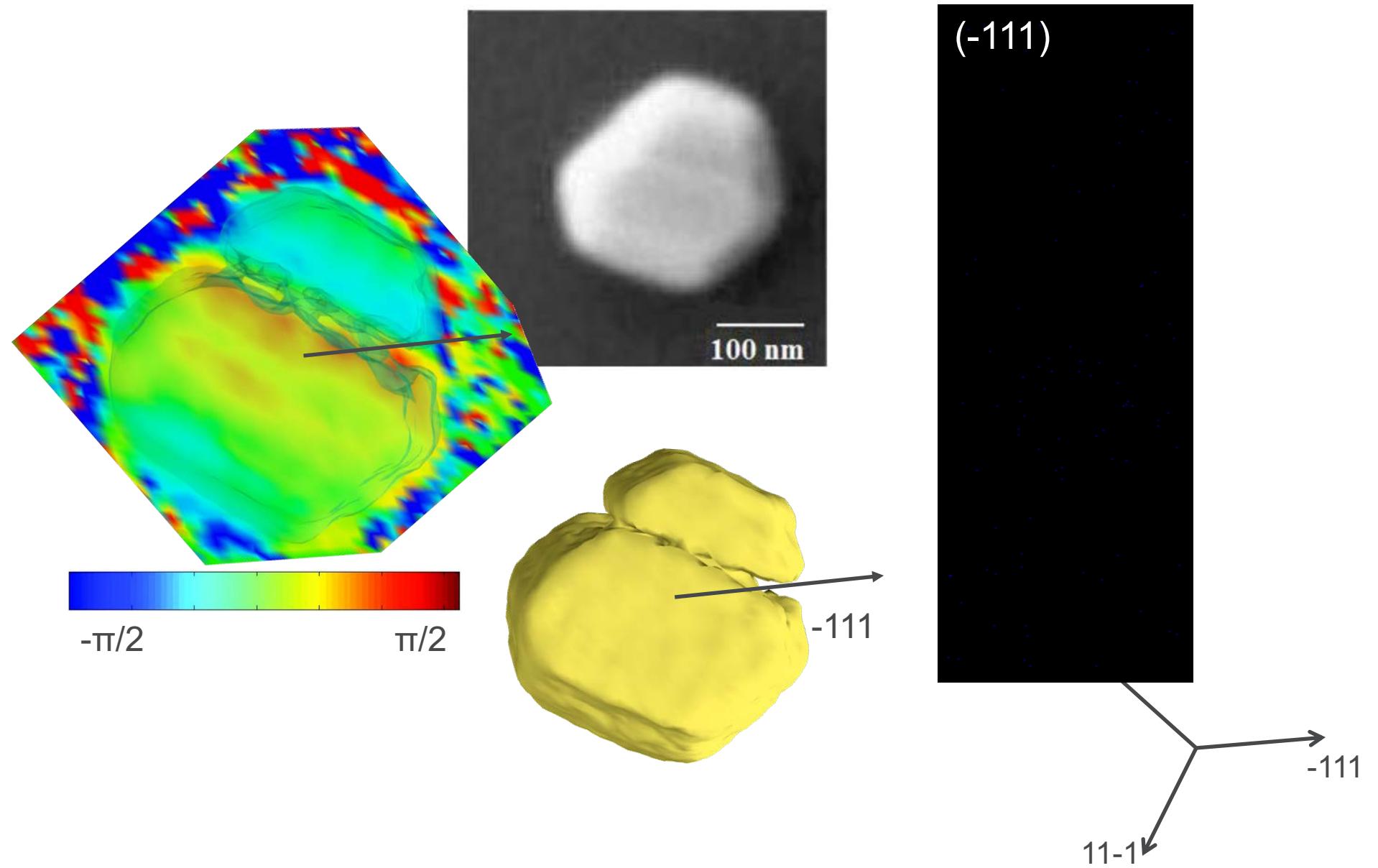
# Multiple reflection reconstructions



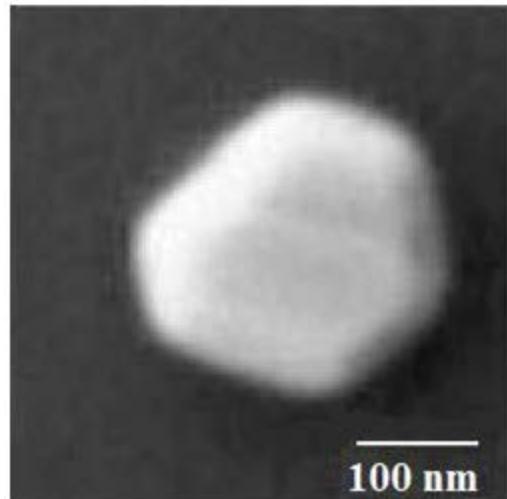
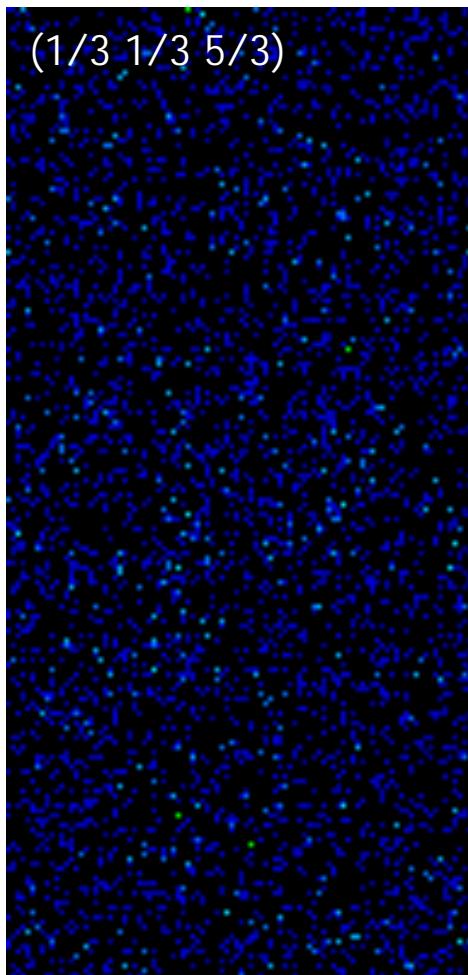
# Multiple reflection reconstructions



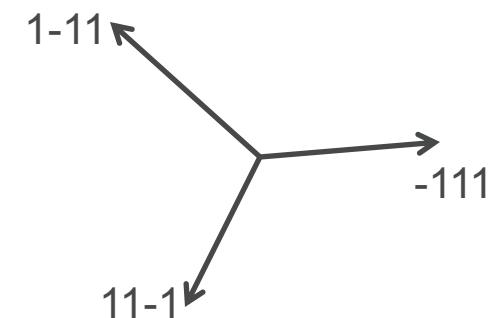
# Multiple reflection reconstructions



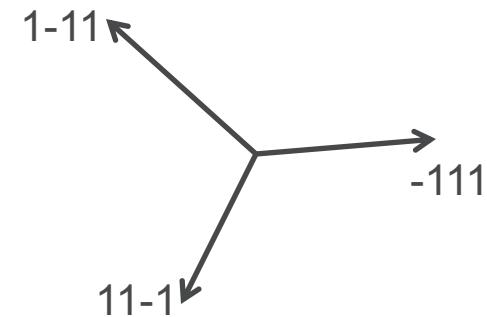
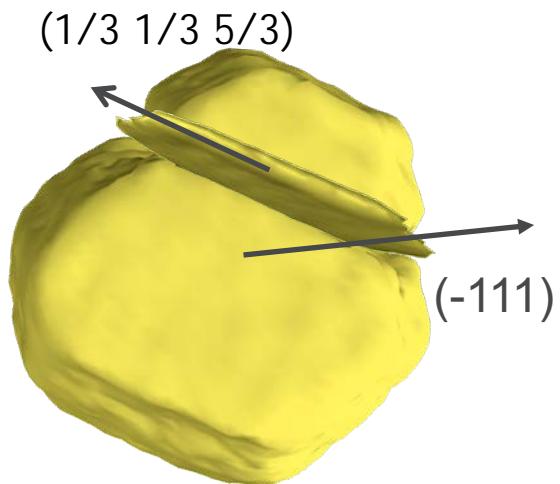
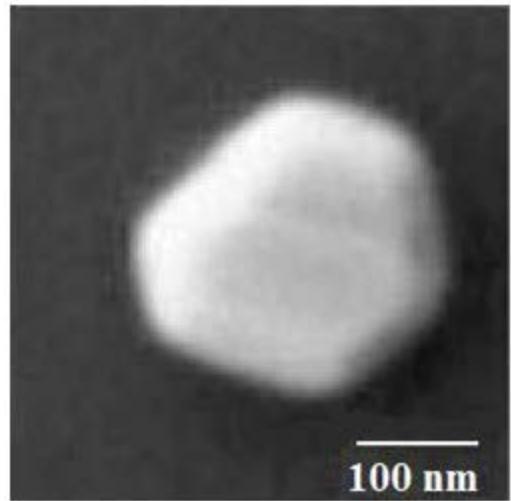
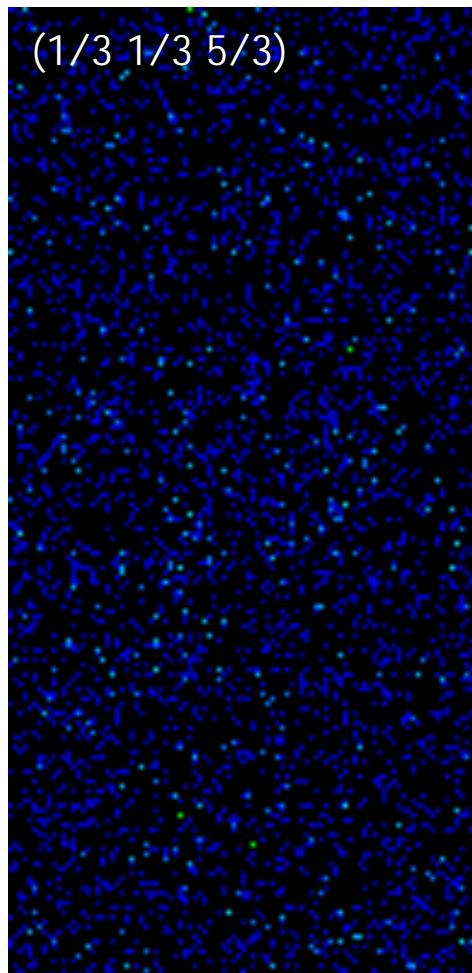
# Multiple reflection reconstructions



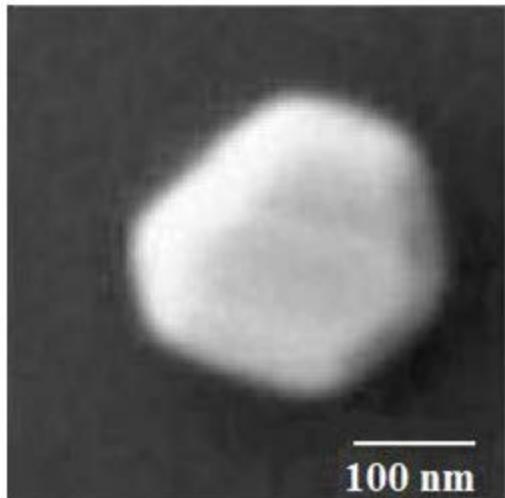
(1/3 1/3 5/3)



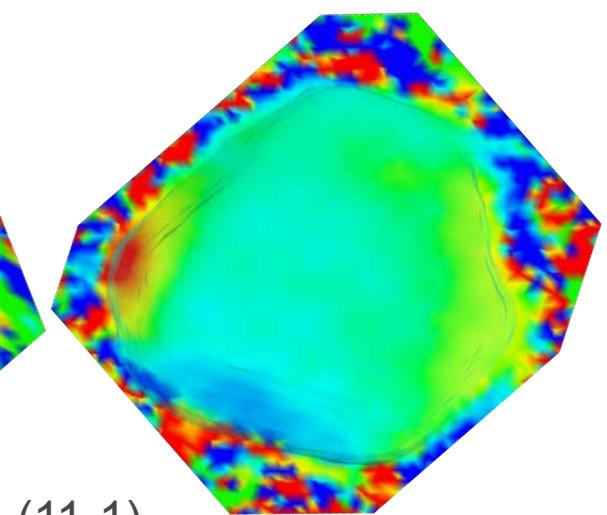
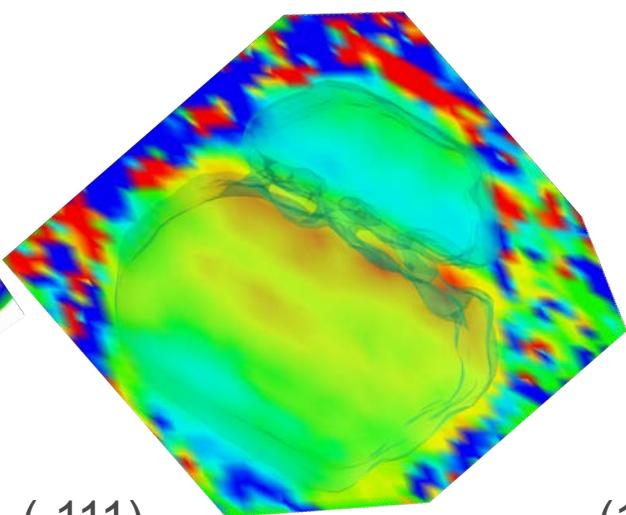
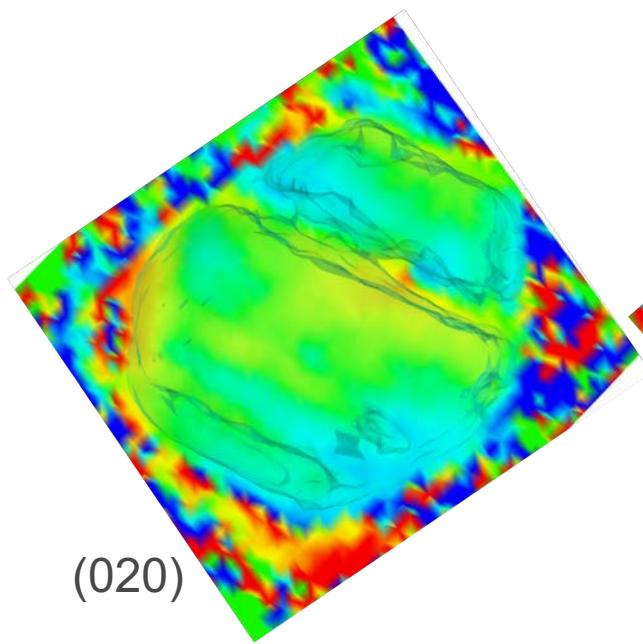
# Multiple reflection reconstructions



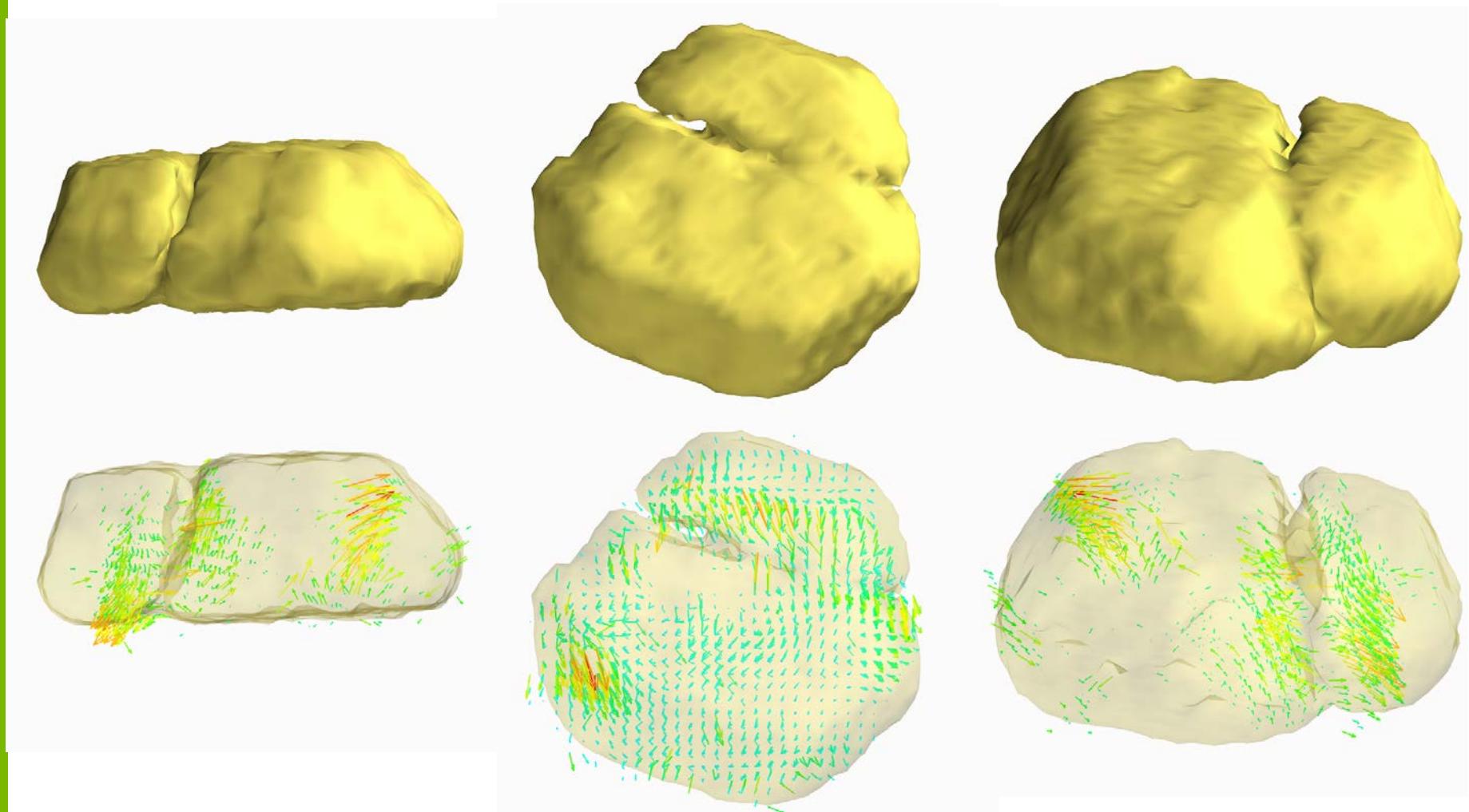
# Multiple reflection reconstructions



$$\varphi = \mathbf{q} \cdot \mathbf{u}(r)$$



# Vector Displacement Field of Gold lattice

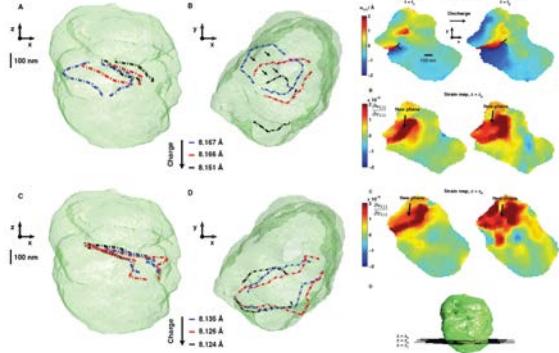


Produced by combining reconstructions from (11-1) (020) (-111)

# BCDI TODAY

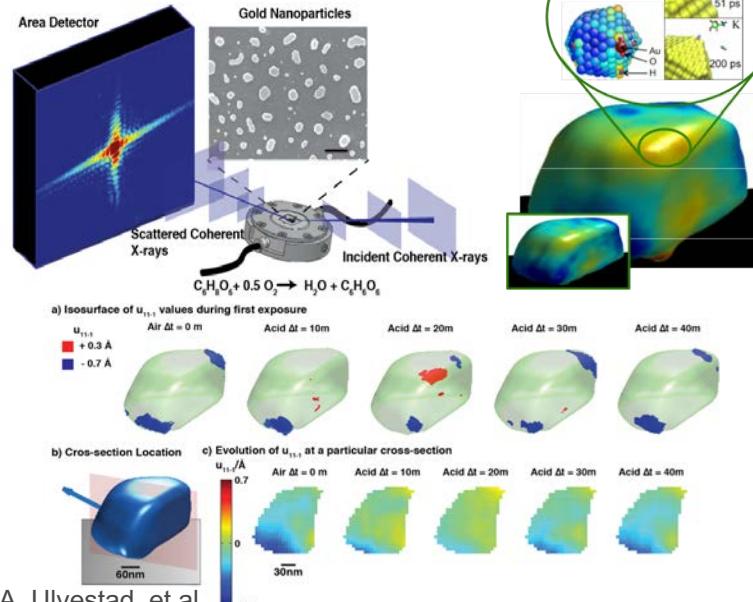
## Operando Nanoscale Imaging

### Dislocation dynamics in Li-ion battery



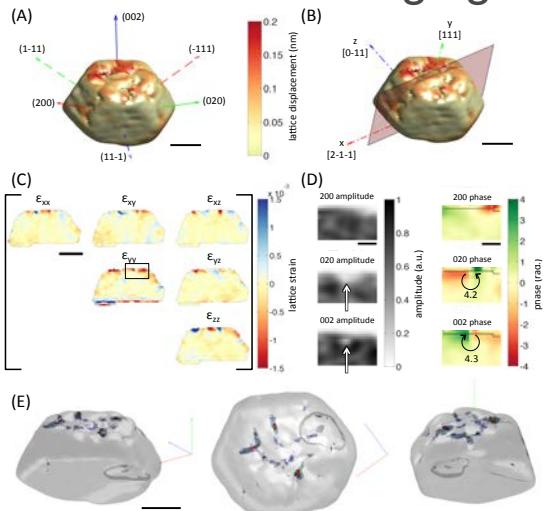
Ulvestad, A., et al. (2015).  
*Science*, 348(6241), 1344–1347

### Liquid Catalysis



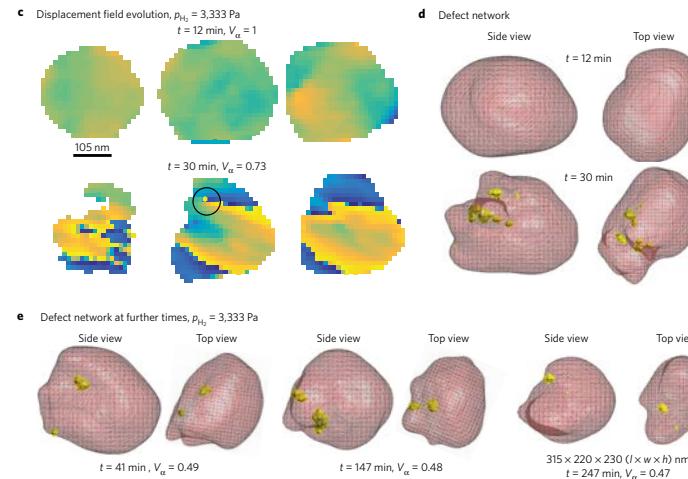
A. Ulvestad, et al.  
*J. Phys. Chem. Lett.*, vol. 7, no. 15, pp. 3008, Aug. 2016.

### Strain Tensor Imaging



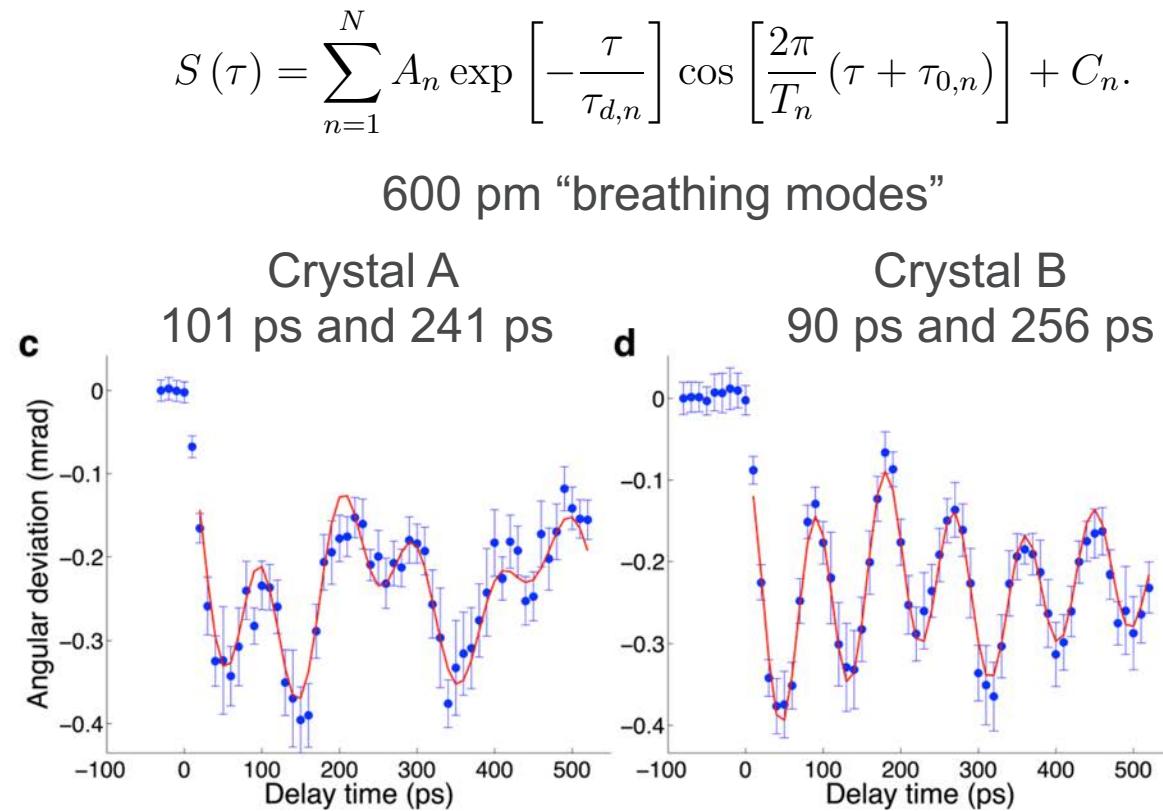
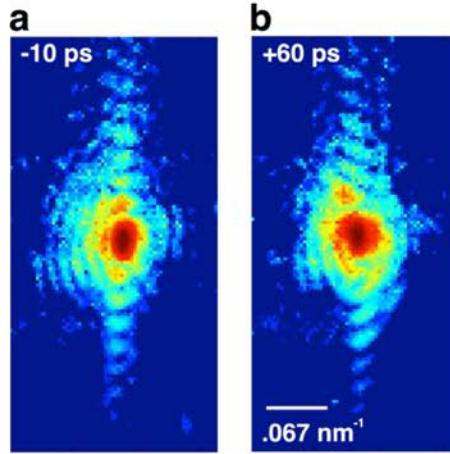
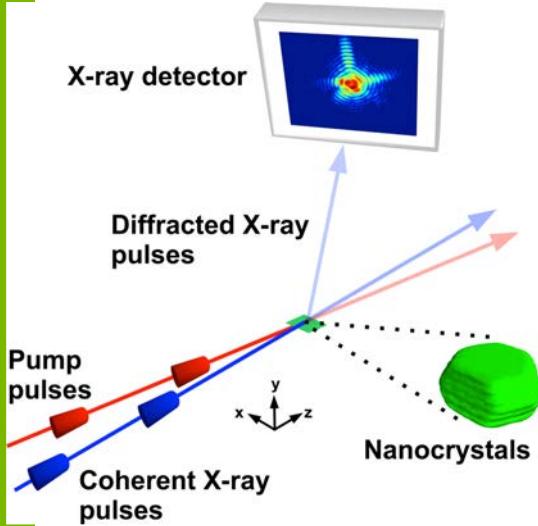
F. Hofmann, et al.  
*Sci Rep*, vol. 7, p. 45993, Apr. 2017.

### Dislocation dynamics in the hydriding phase transformations of Pd



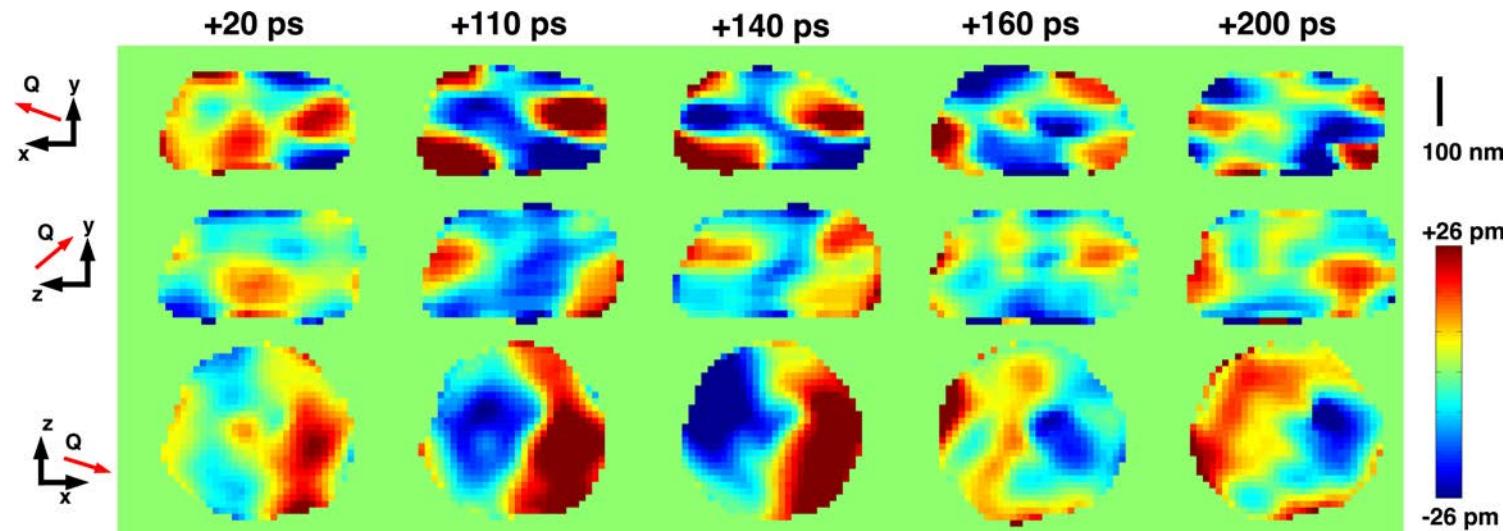
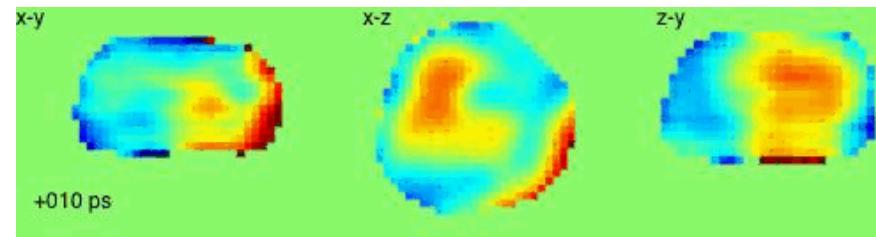
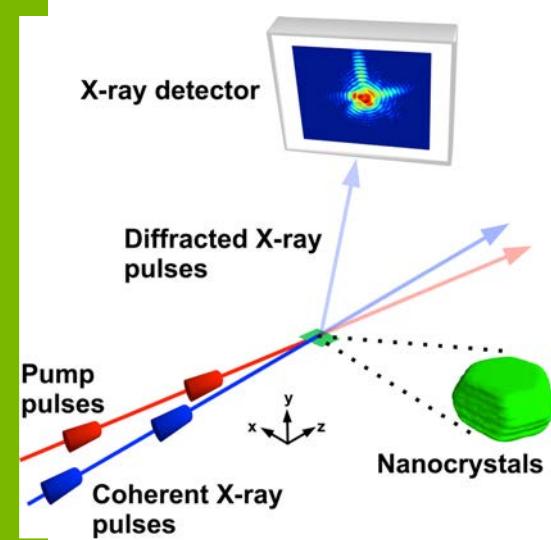
Ulvestad, et al.  
*Nature Materials*, vol. 16, no. 5, pp. 565–571, Jan. 2017.

# Imaging Lattice Dynamics Laser Pump - CXD Probe@LCLS



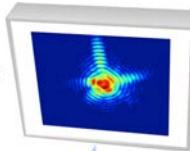
Ultrafast three dimensional imaging of lattice dynamics in individual gold nanocrystals  
 J. N. Clark, L. Beitra, G. Xiong, A. Higginbotham, D. M. Fritz, H. T. Lemke, D. Zhu,  
 M. Chollet, G. J. Williams, M. Messerschmidt, B. Abbey, R. J. Harder,  
 A. M. Korsunsky, J. S. Wark & I. K. Robinson. (2013). *Science*, 341(6141), 56–59

# Imaging Lattice Dynamics Laser Pump - CXD Probe@LCLS



Ultrafast three dimensional imaging of lattice dynamics in individual gold nanocrystals  
J. N. Clark, L. Beitra, G. Xiong, A. Higginbotham, D. M. Fritz, H. T. Lemke, D. Zhu,  
M. Chollet, G. J. Williams, M. Messerschmidt, B. Abbey, R. J. Harder,  
A. M. Korsunsky, J. S. Wark & I. K. Robinson. (2013). *Science*, 341(6141), 56–59

X-ray detector



Diffracted X-ray pulses

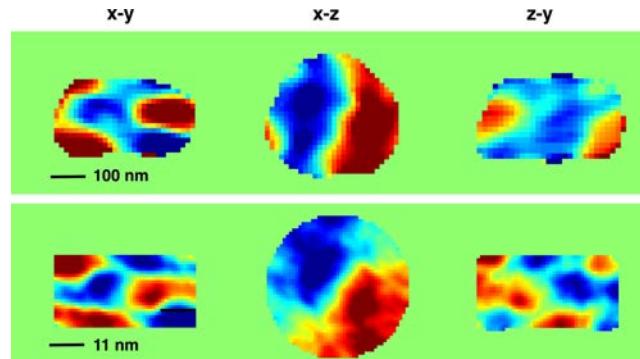
Pump pulses

Coherent X-ray pulses



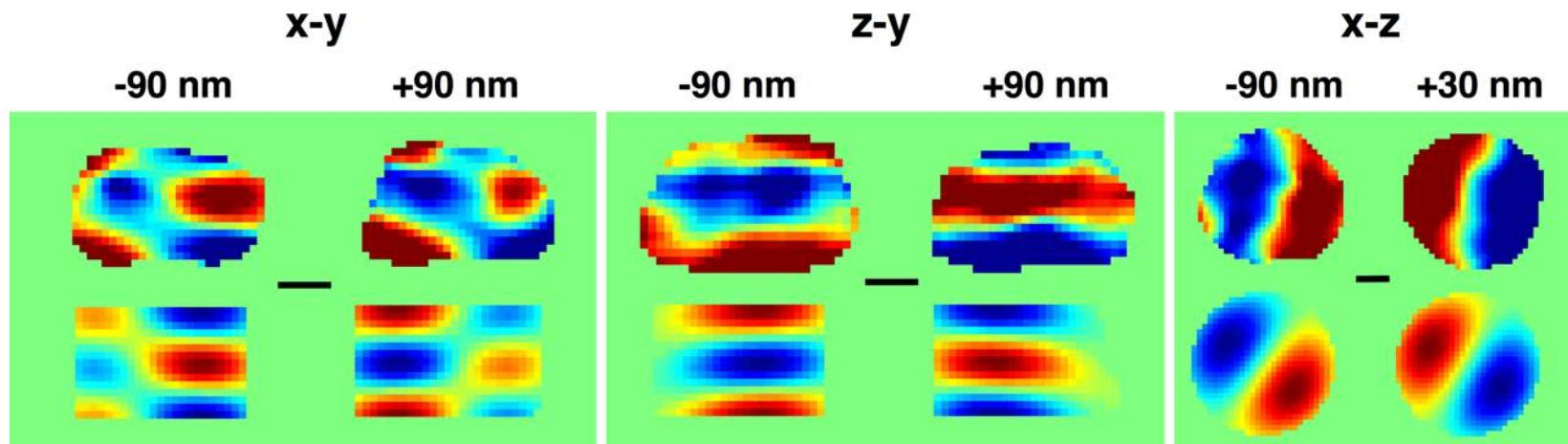
Nanocrystals

# Imaging Lattice Dynamics Laser Pump - CXD Probe@LCLS



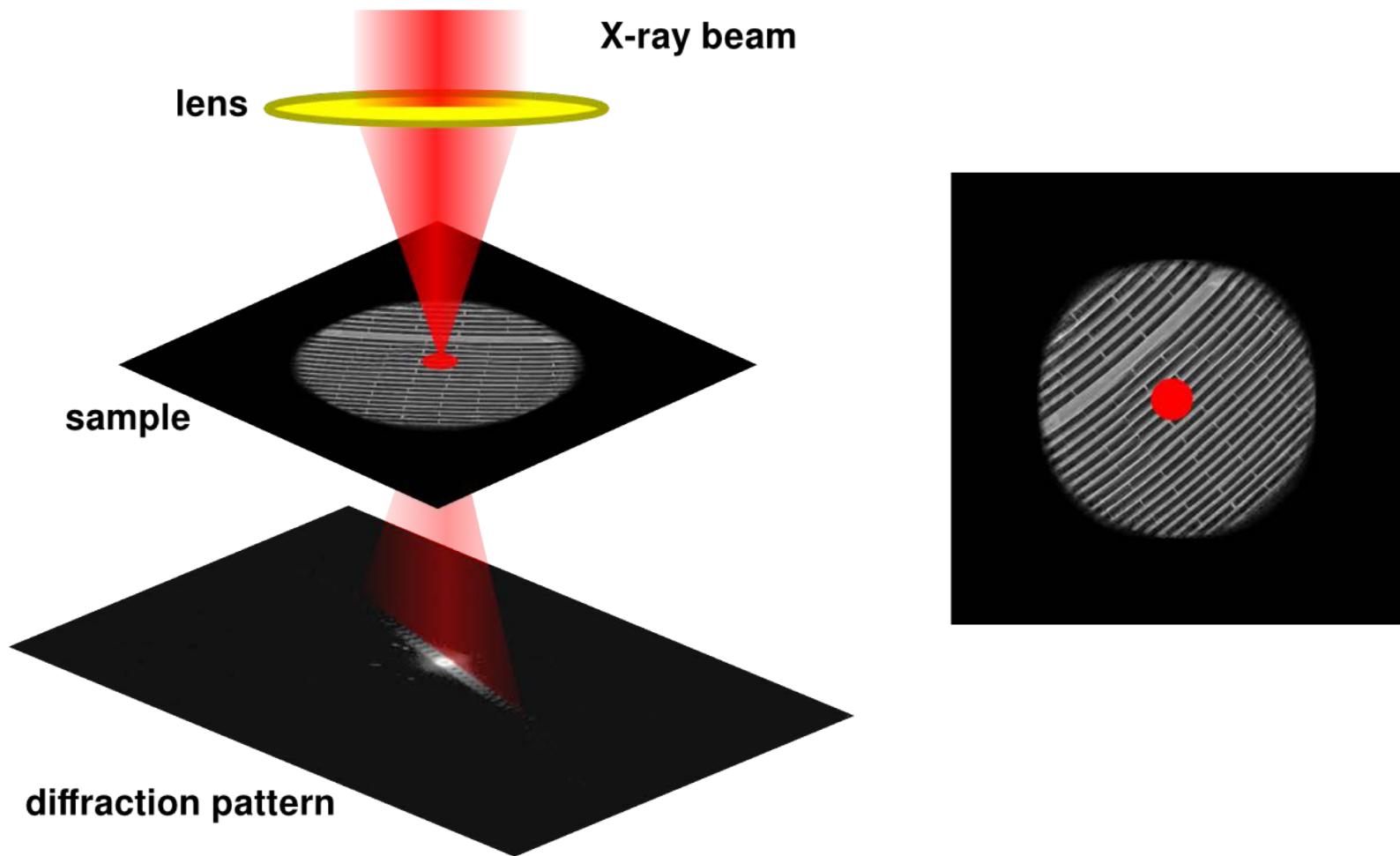
Orthogonal slices  
Through crystal density

MD simulation  
at +110ps

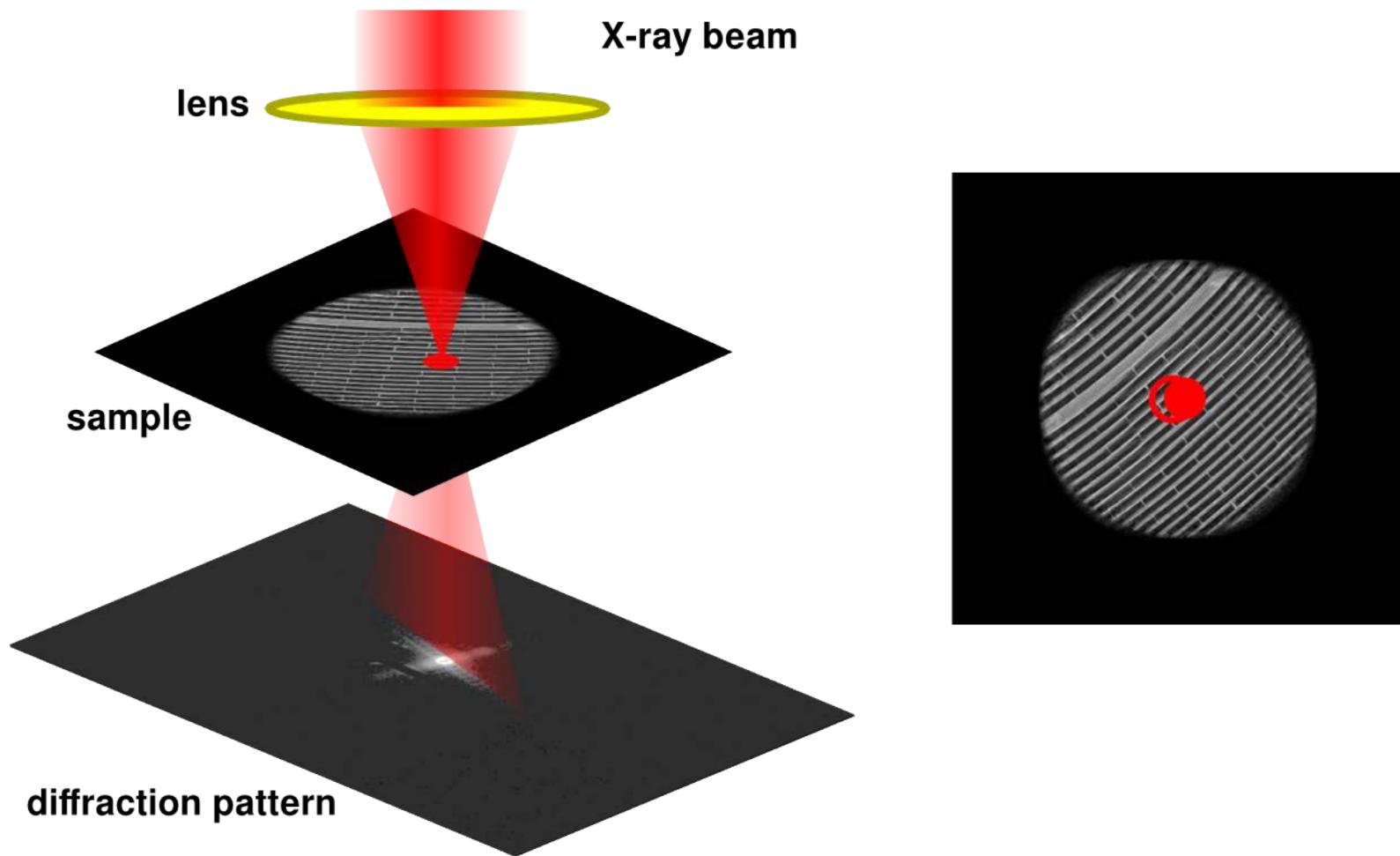


Ultrafast three dimensional imaging of lattice dynamics in individual gold nanocrystals  
J. N. Clark, L. Beitra, G. Xiong, A. Higginbotham, D. M. Fritz, H. T. Lemke, D. Zhu,  
M. Chollet, G. J. Williams, M. Messerschmidt, B. Abbey, R. J. Harder,  
A. M. Korsunsky, J. S. Wark & I. K. Robinson. (2013). *Science*, 341(6141), 56–59

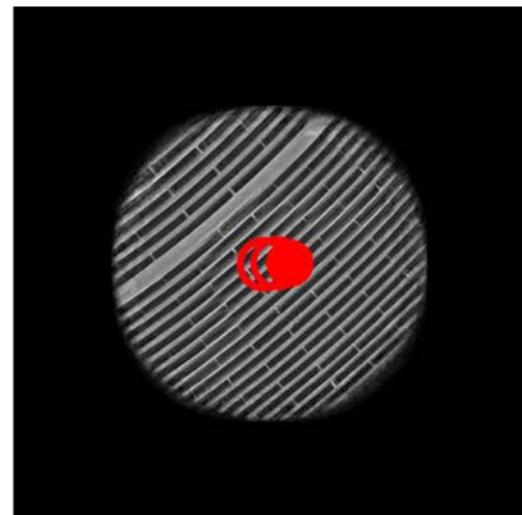
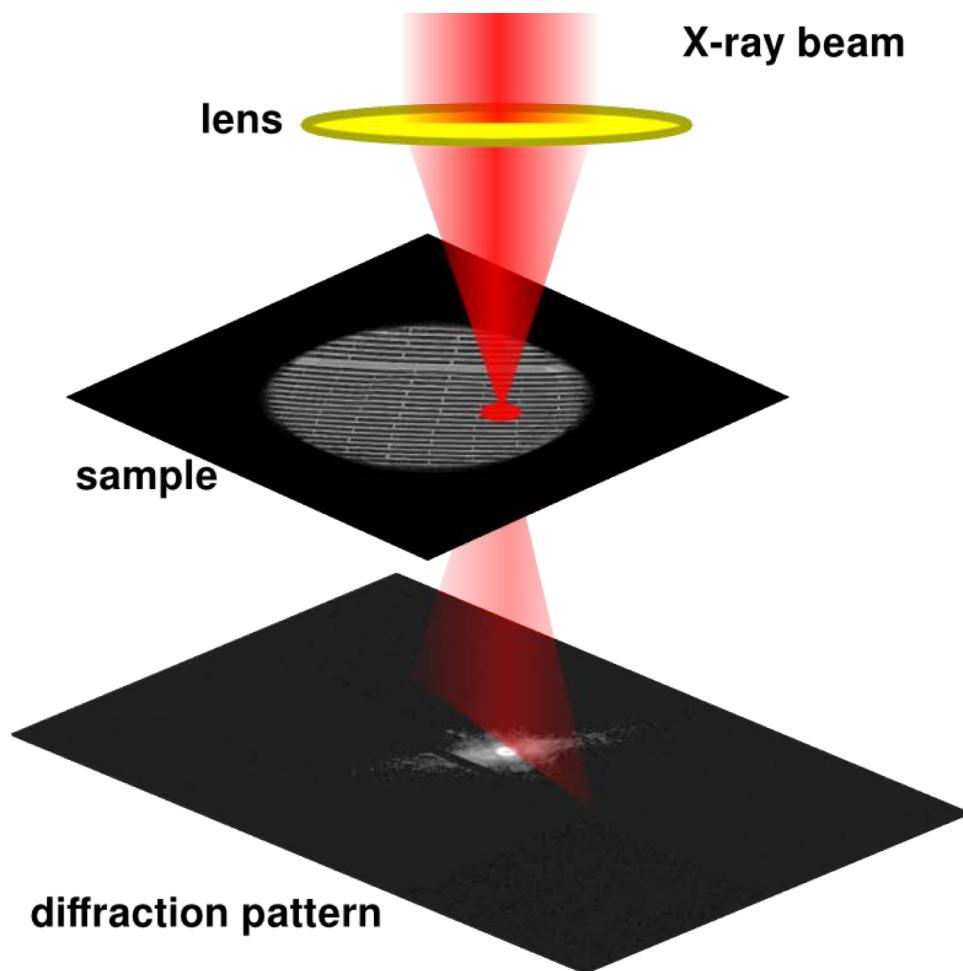
# Ptychography (to fold) - Scanning CDI for extended object



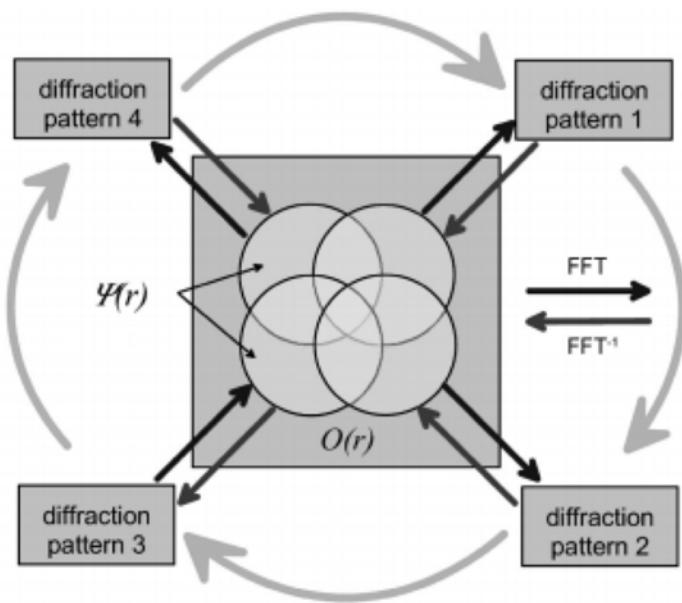
# Ptychography (to fold) - Scanning CDI for extended object



# Ptychography (to fold) - Scanning CDI for extended object



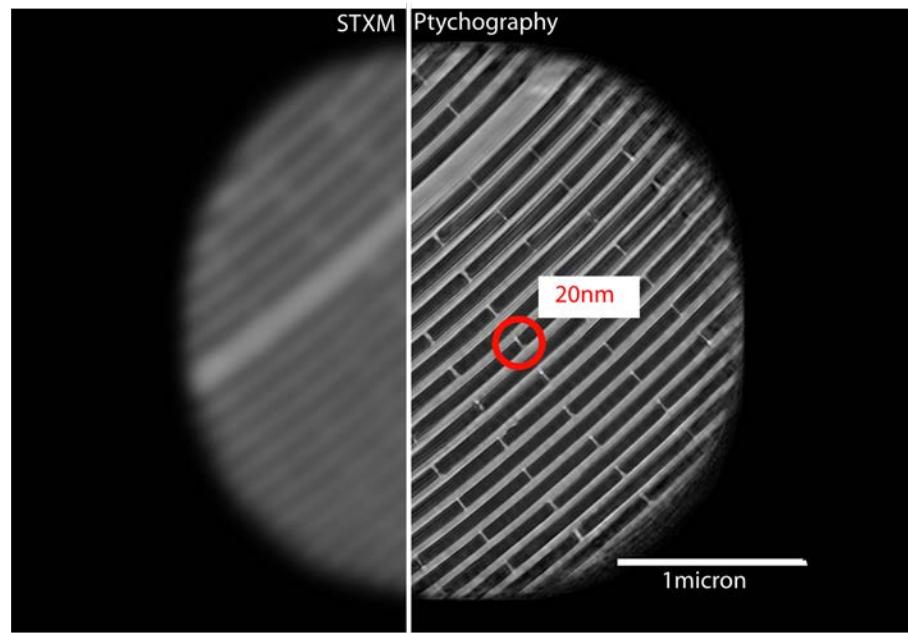
# Ptychography



Ptychographic iterative engine (PIE)

J. Rodenburg *et al.*, *PRL* **98**, 034801 (2007)

Platinum nanostructure

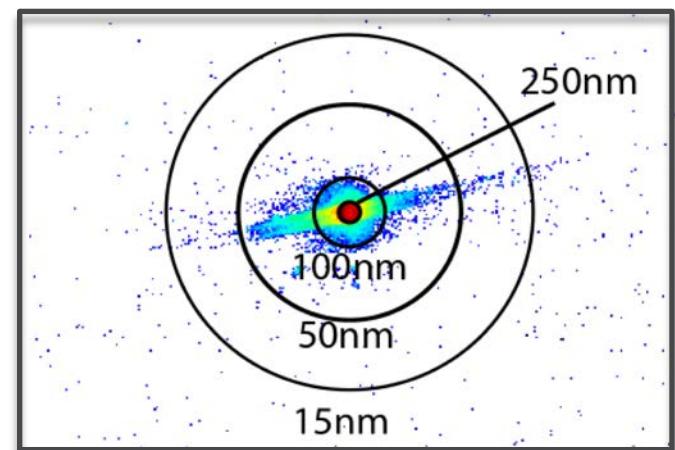


Spatial resolution:  $\delta = \frac{\lambda}{\theta} = \frac{\lambda z}{N\Delta}$

Exit surface wave field:  $\psi(r) = P(r)O(r)$

$$O(\mathbf{r}) = \frac{\sum_j P^*(\mathbf{r} - \mathbf{r}_j)\psi_j(\mathbf{r})}{\sum_j |P(\mathbf{r} - \mathbf{r}_j)|^2} \quad P(\mathbf{r}) = \frac{\sum_j O^*(\mathbf{r} + \mathbf{r}_j)\psi_j(\mathbf{r} + \mathbf{r}_j)}{\sum_j |O(\mathbf{r} + \mathbf{r}_j)|^2}$$

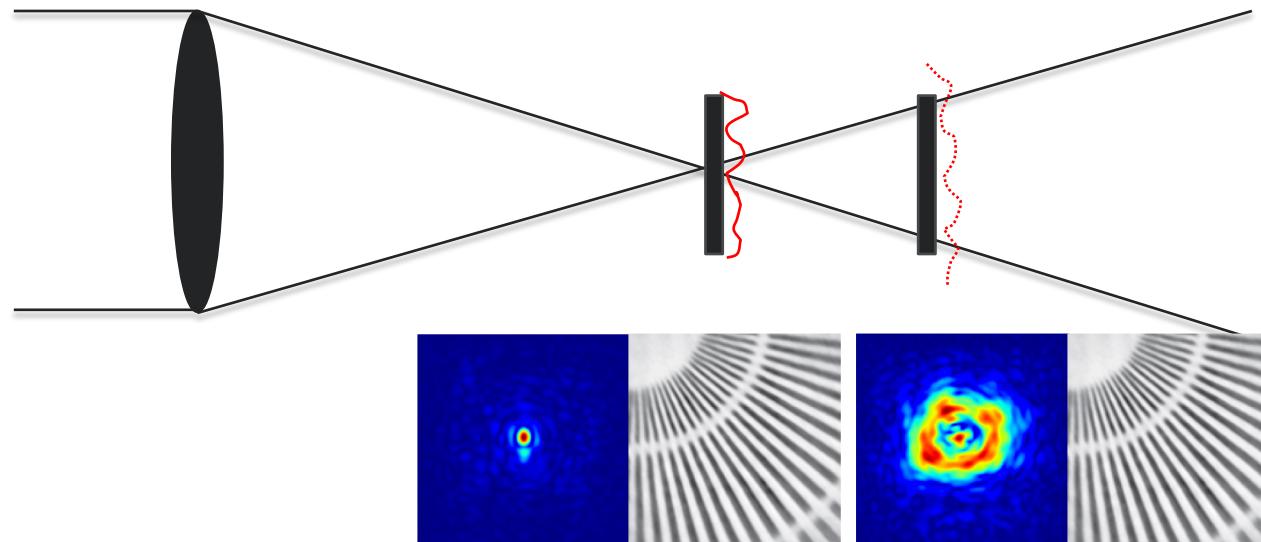
P. Thibault *et al.*, *Science* **321**, 379 (2008)



# At which plane ptychographic images are reconstructed

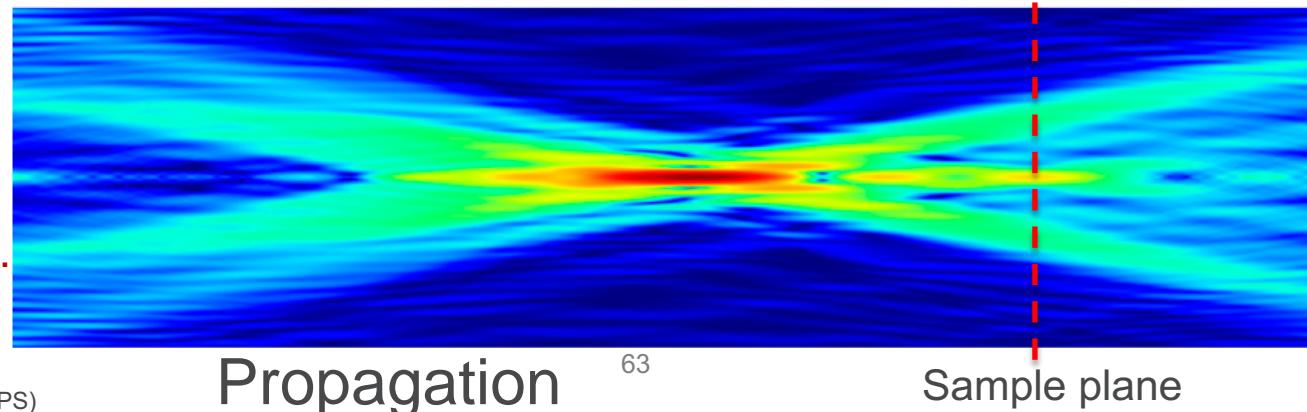
$$\psi(r) = P(r)O(r)$$

Ptychography always produces images at the sample plane.

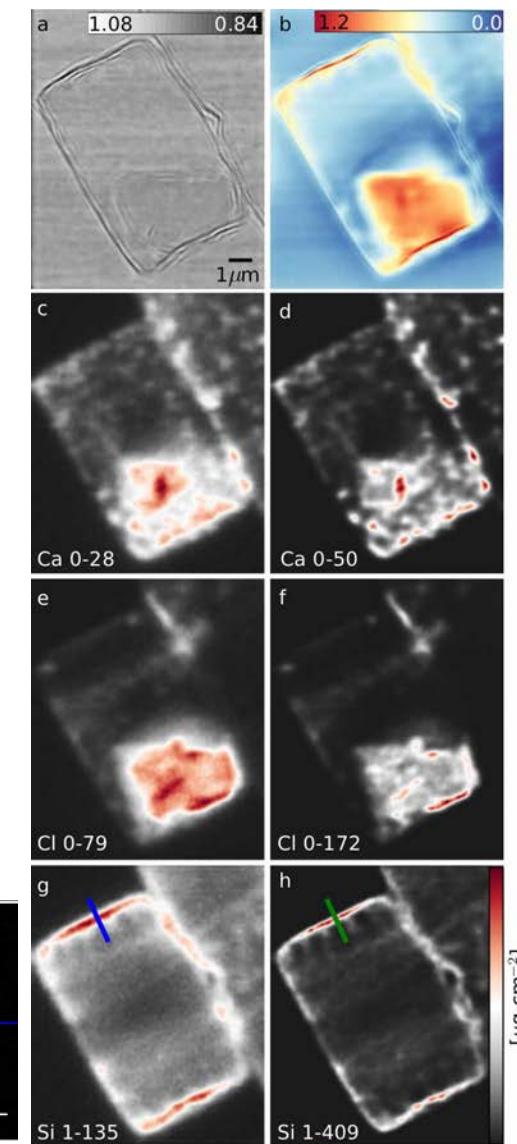
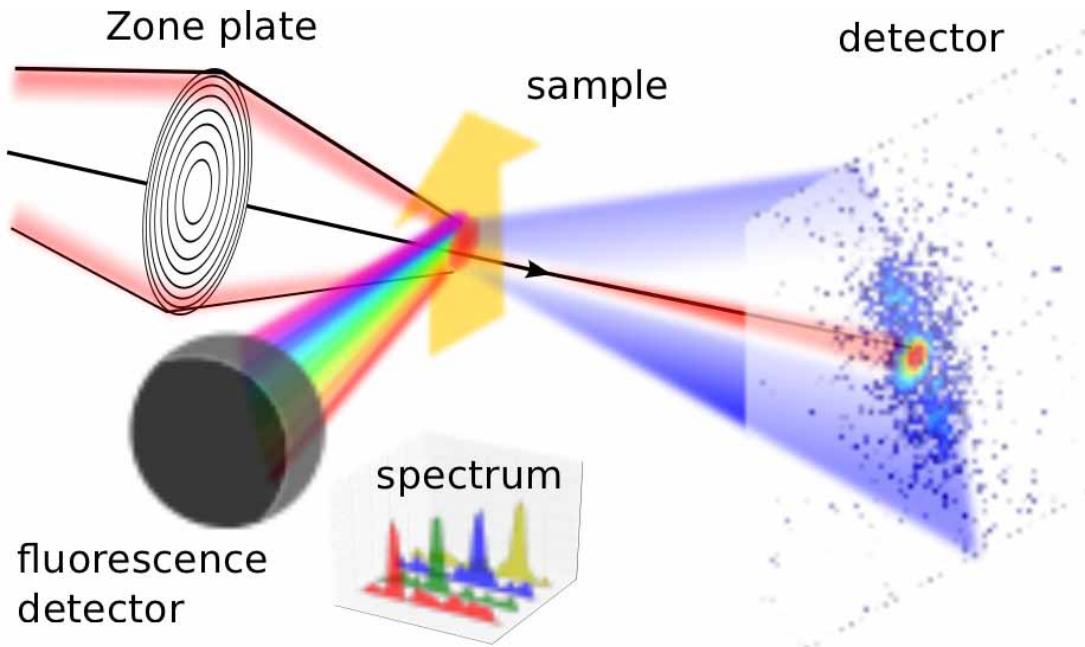


The resolution  
is not limited  
by the beam  
size.

Characterization  
of focusing optics.



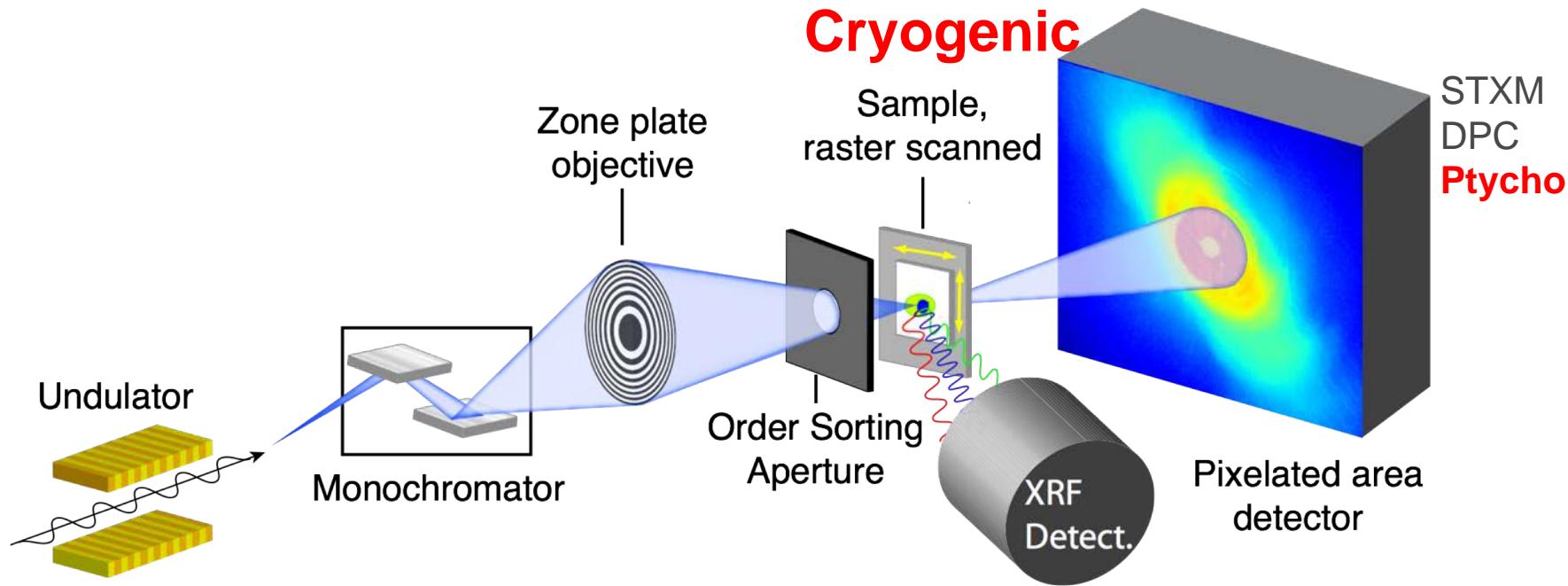
# PTYCHOGRAPHY MICROPROBES -> COHERENT IMAGING INSTRUMENT



Vine, et al. (2012). *Opt. Express*, 20(16), 18287–18296.

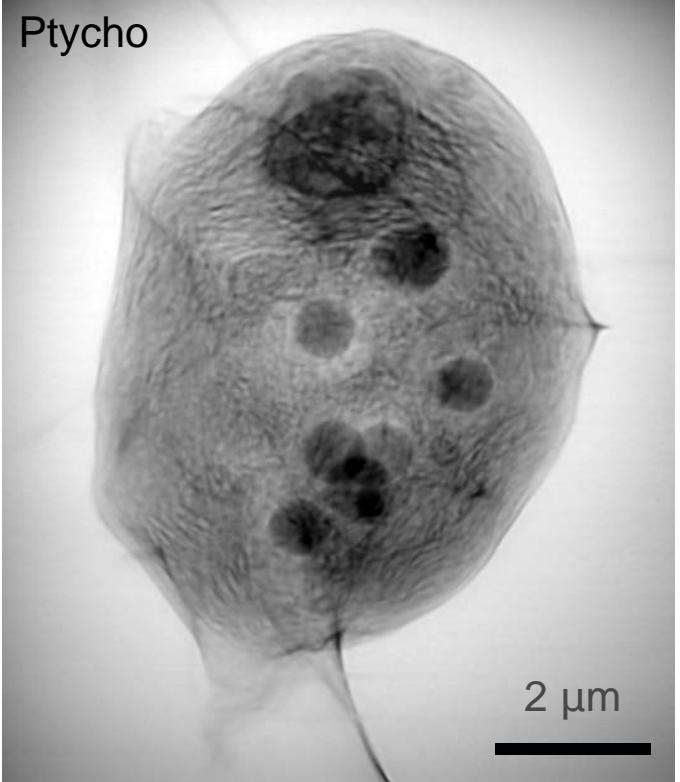
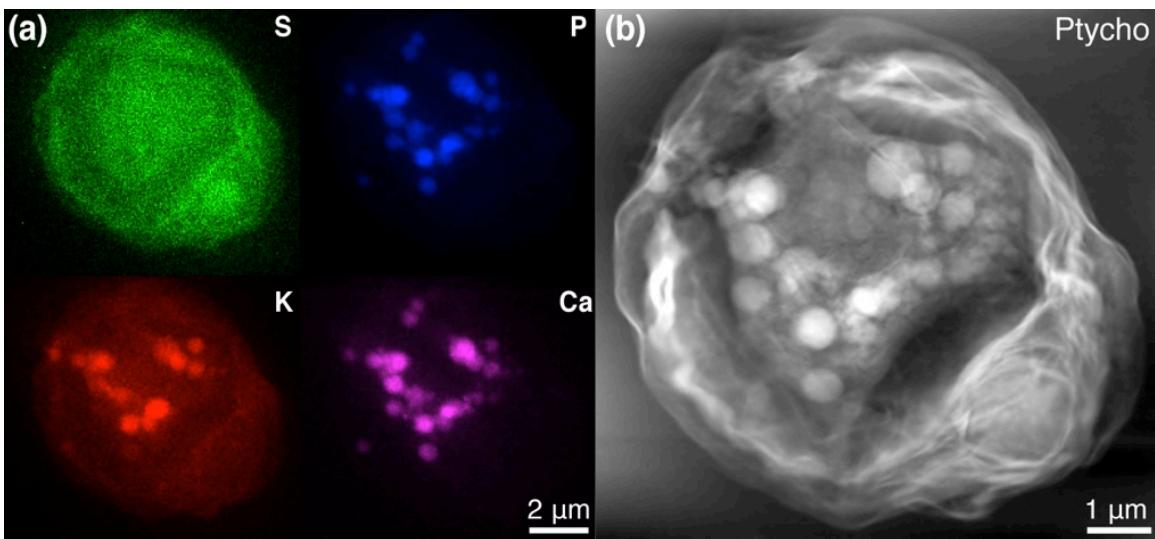
# Making ptychography colorful

## ❖ Combination of Ptychography & Fluorescence



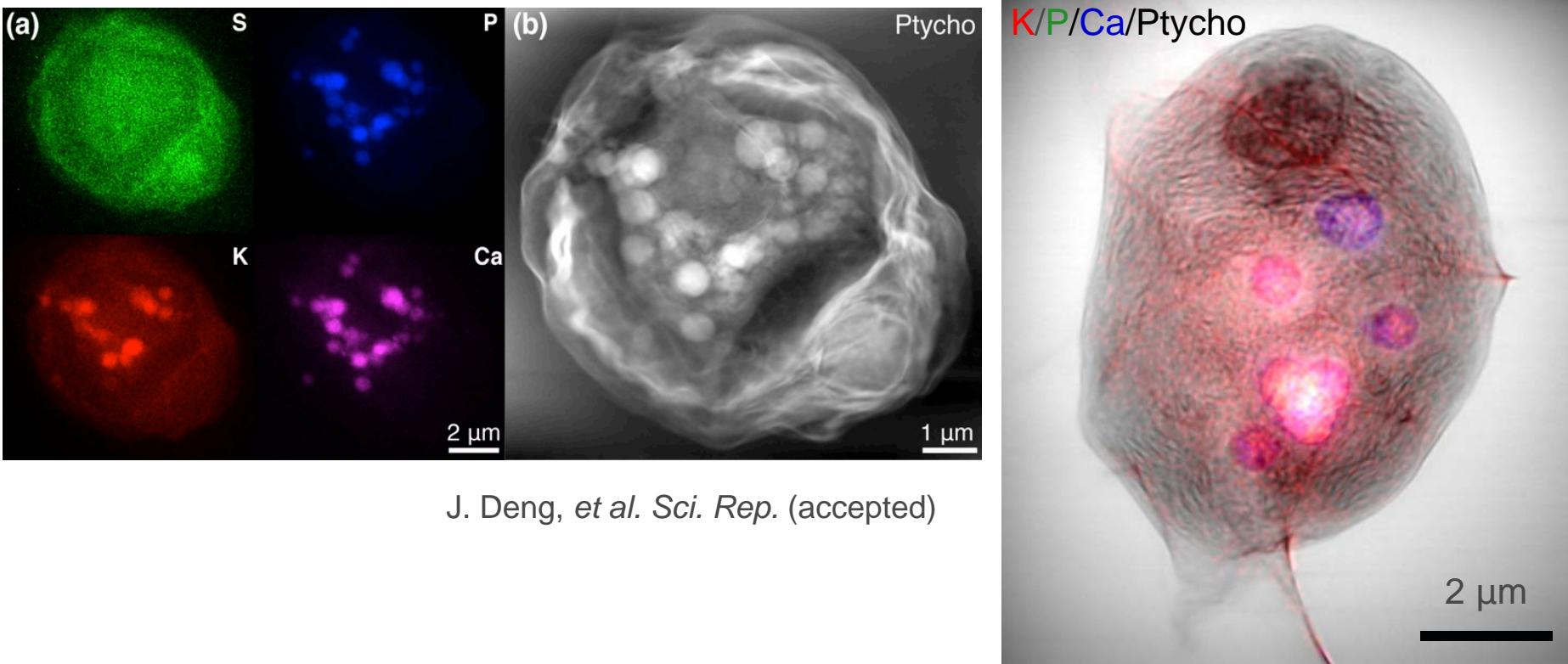
J. Deng, et al. PNAS 112, 2314-2319 (2015)

- **Frozen-hydrated samples:** closer to natural state, reduce radiation damage
- **Fluorescence:** quantitative elemental composition
- **Ptychography:** structure information with high resolution



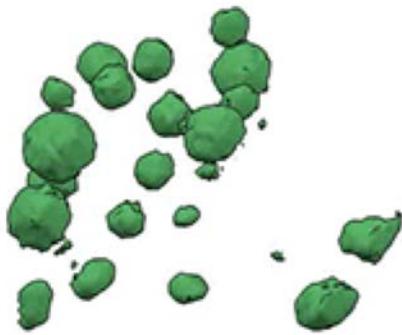
J. Deng, et al. *Sci. Rep.* (accepted)

- Frozen-hydrated *Chlamy.* Alga
- Ptychographic image resolution: ~18 nm
- Fluorescence image resolution: ~100 nm
- Complementary information helps with sample analysis



- Frozen-hydrated *Chlamy. Alga*
- Ptychographic image resolution: ~18 nm
- Fluorescence image resolution: ~100 nm
- Complementary information helps with sample analysis

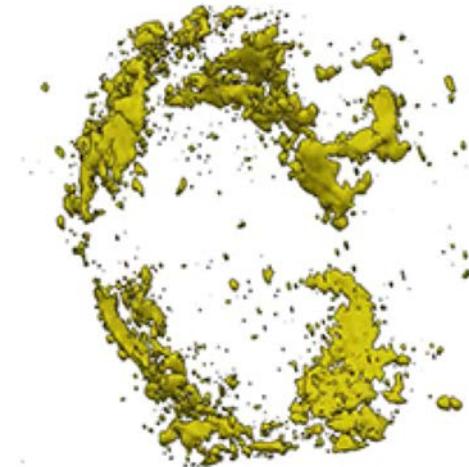
# Extended to 3D



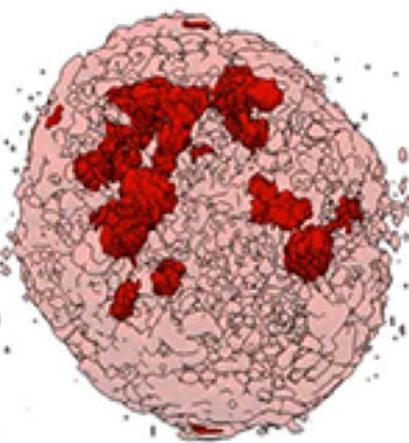
P



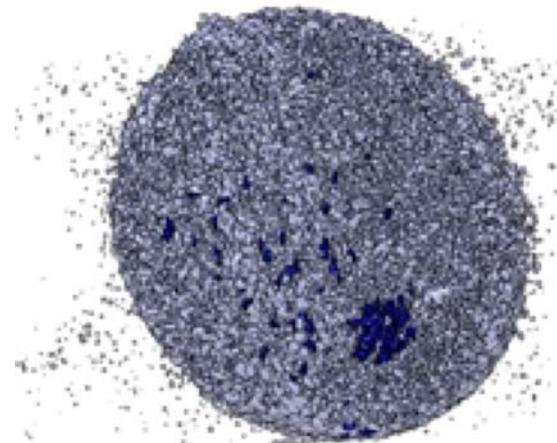
Ca



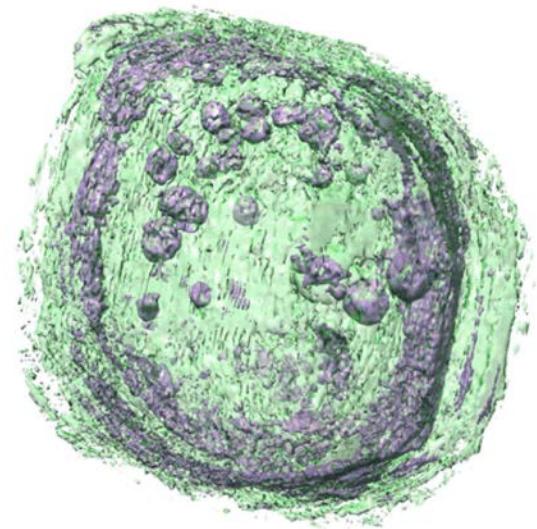
Cl



K

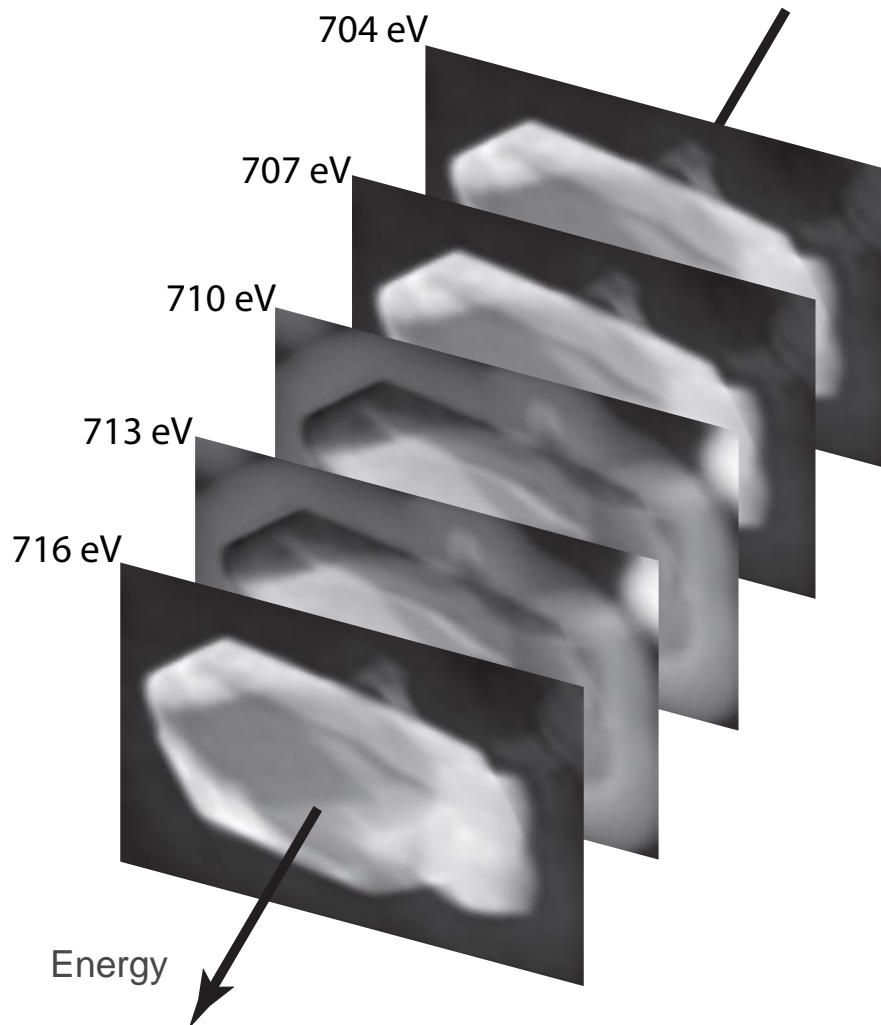


S

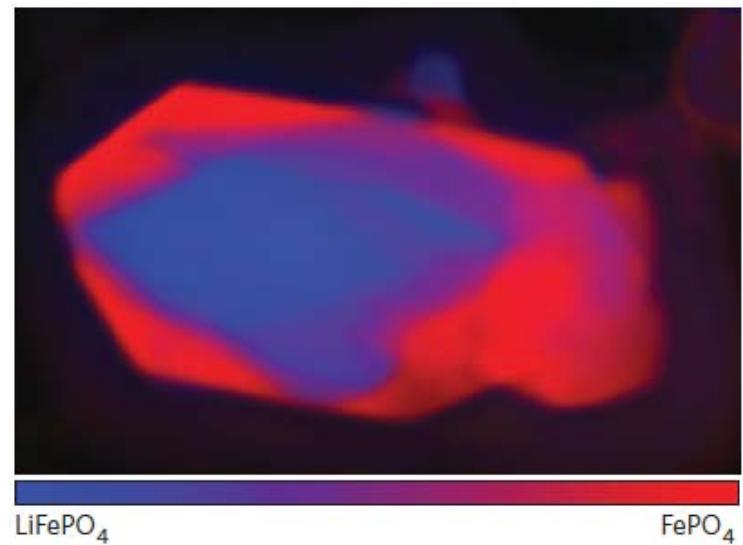
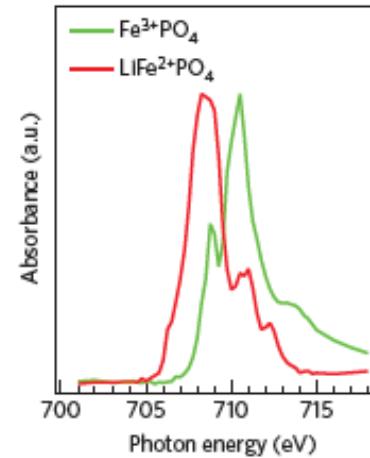


Ptycho  
(In preparation)

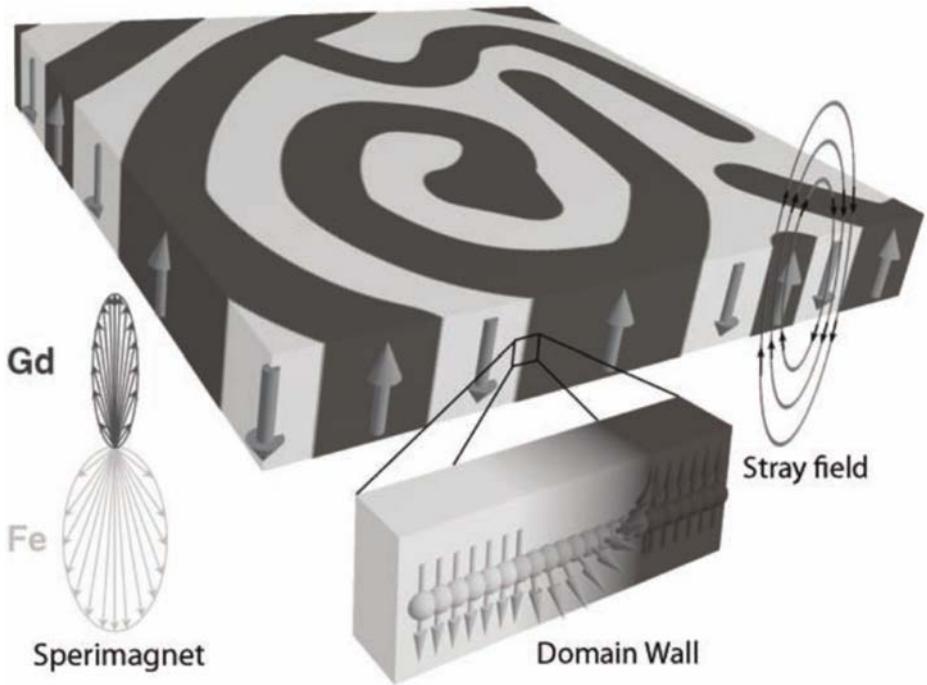
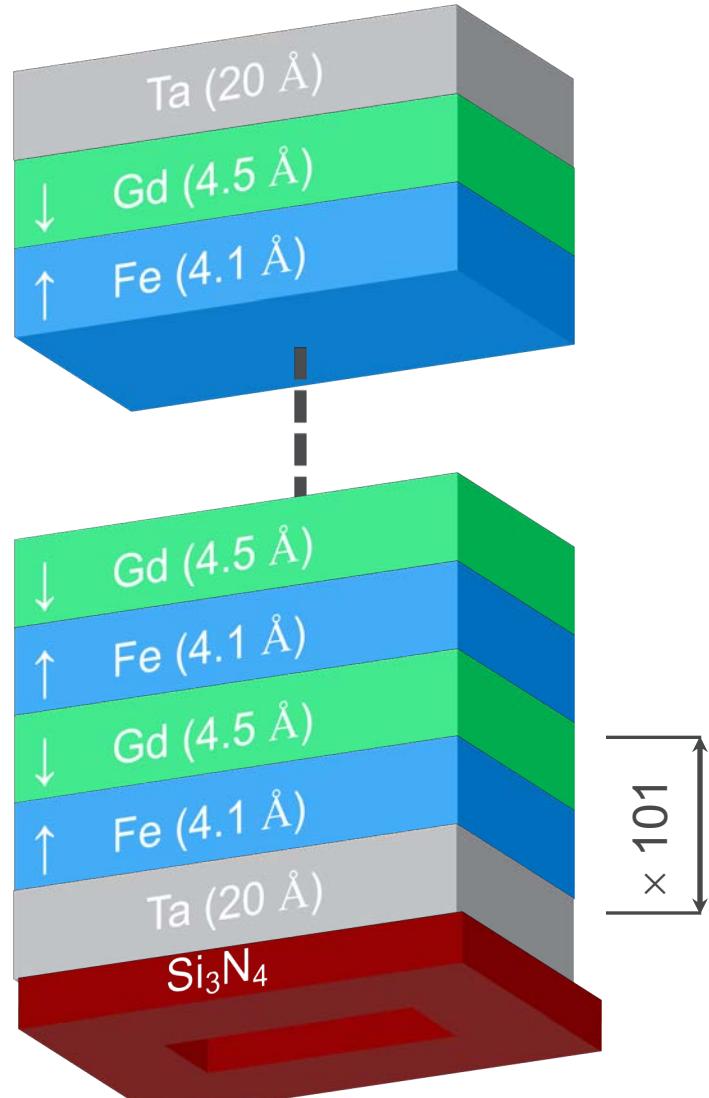
- ❖ Pychographic spectroscopy
  - like STXM XNEAS analysis, but with higher resolution and more information (both absorption and phase) from refractive index



Adapted from D. Shapiro, et al. *Nat. Photon.* **8**, 765 (2014)



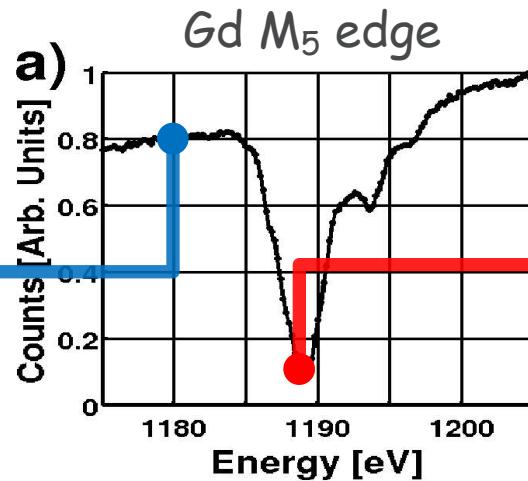
# GDFE LAYERED MAGNETIC FILMS



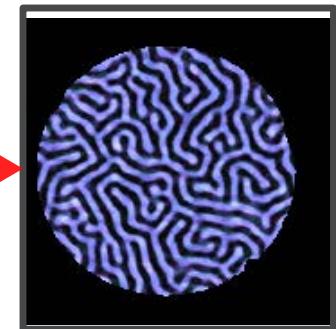
$$E_{tot} = \int [ \underbrace{e_{ex}(\mathbf{m})}_{exchange} + \underbrace{e_{an}(\mathbf{m})}_{anisotropy} - \underbrace{\mu_0 \mathbf{H}_{ex} \cdot \mathbf{M}}_{ext. field} + \underbrace{\frac{1}{2} \mu_0 \mathbf{H}_d^2}_{stray field} ] dV$$

# MAGNETIC CONTRAST MECHANISM

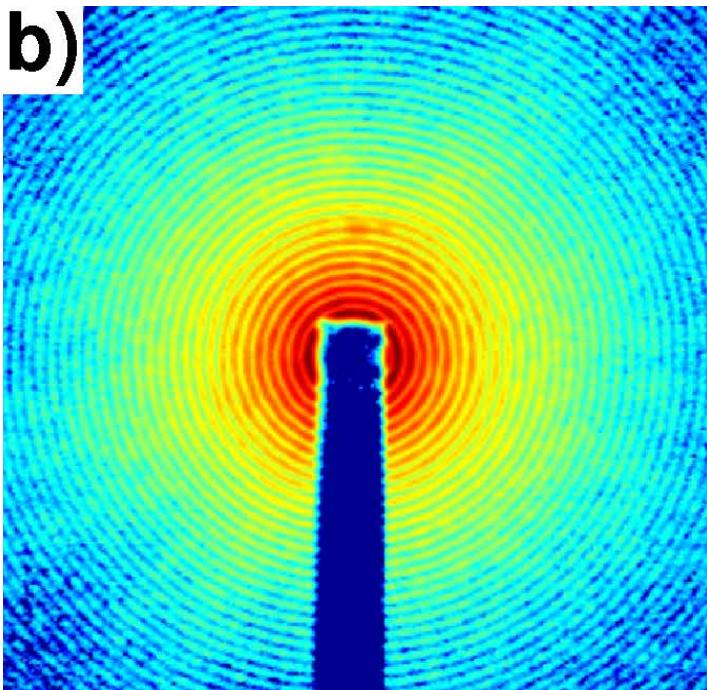
Off-resonance: ●



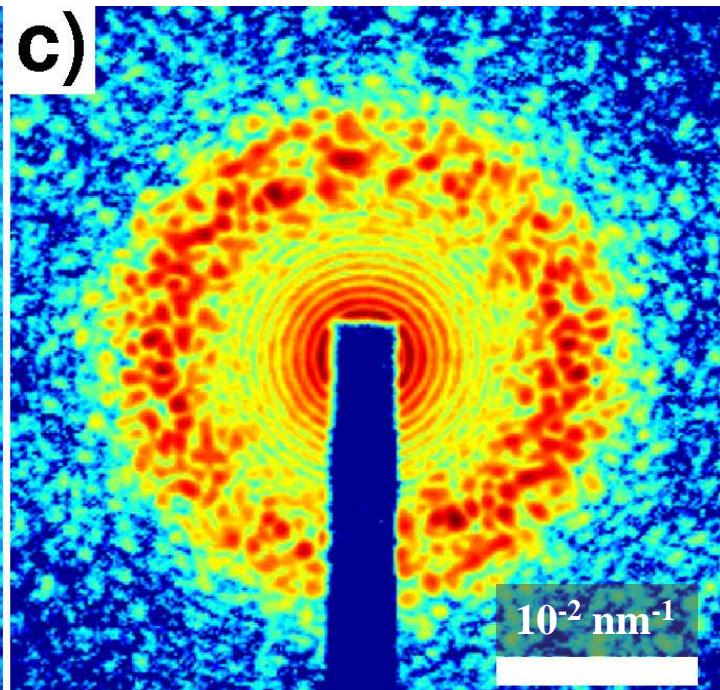
On-resonance: ●



b)

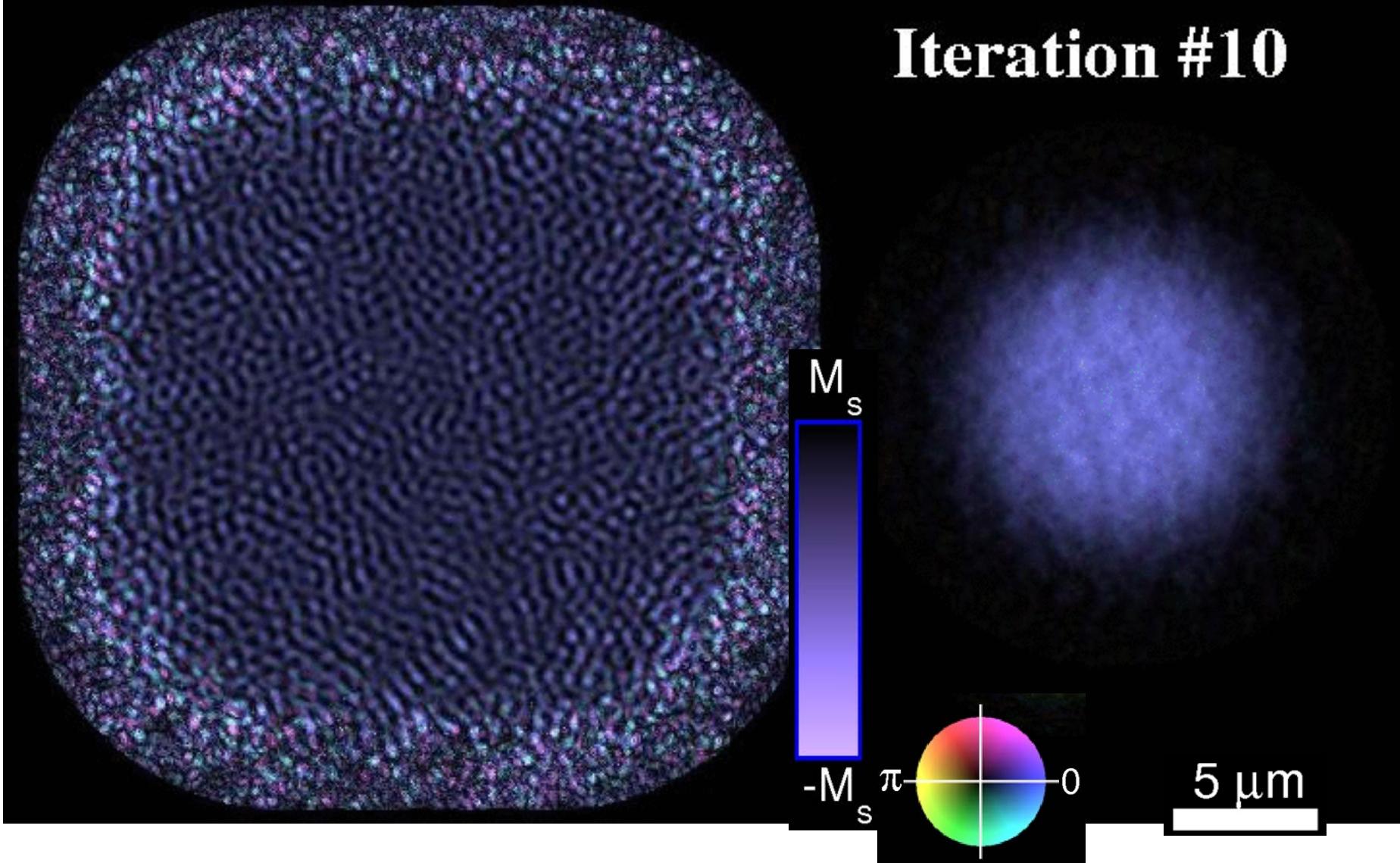


c)



# REAL SPACE RECONSTRUCTION

Iteration #10



Magnetic structure

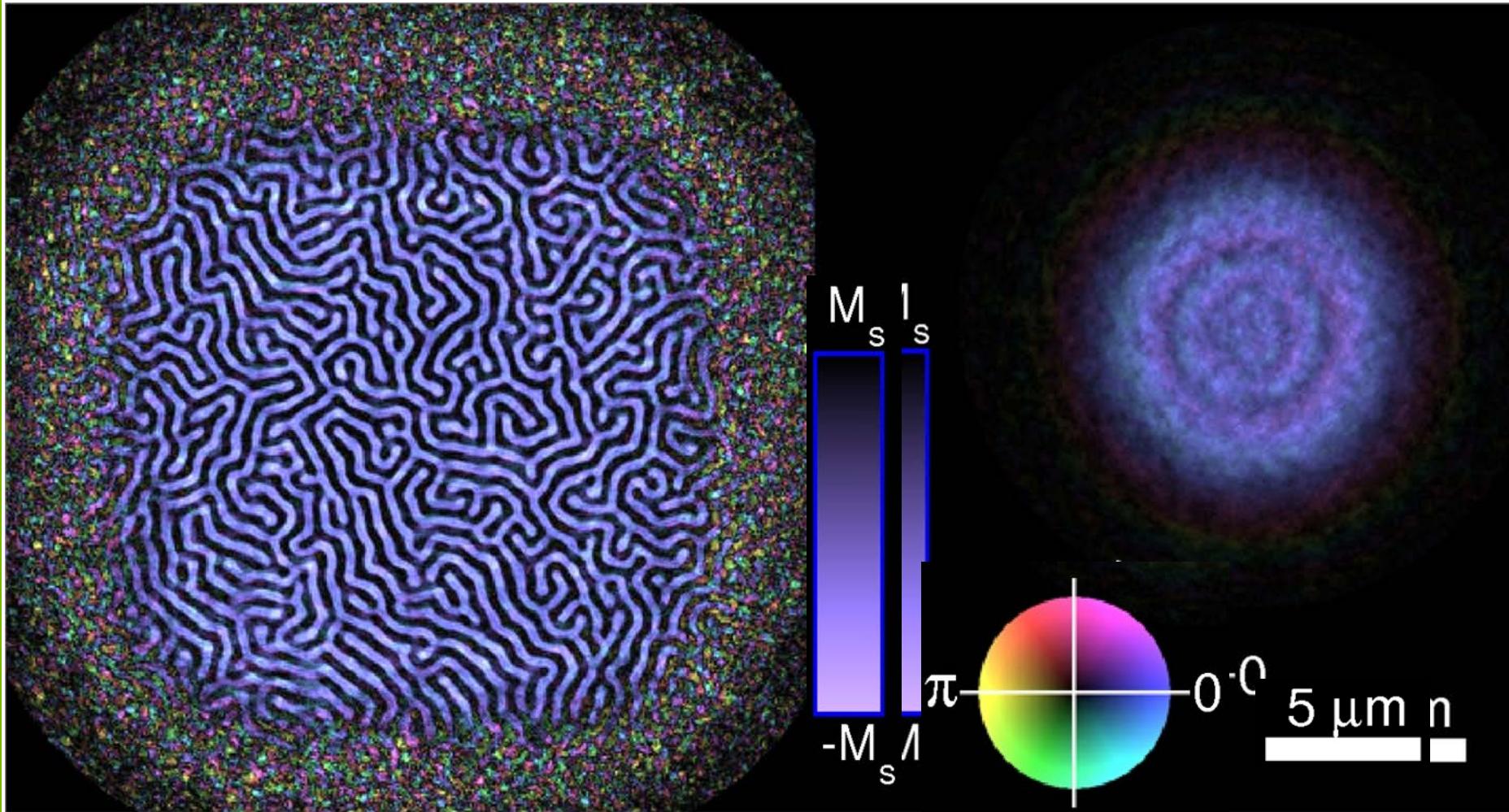
(exit wave)

Illumination Function

A. Tripathi, O.S. et al., Proc Natl Acad Sci USA 108, 13393 (2011)

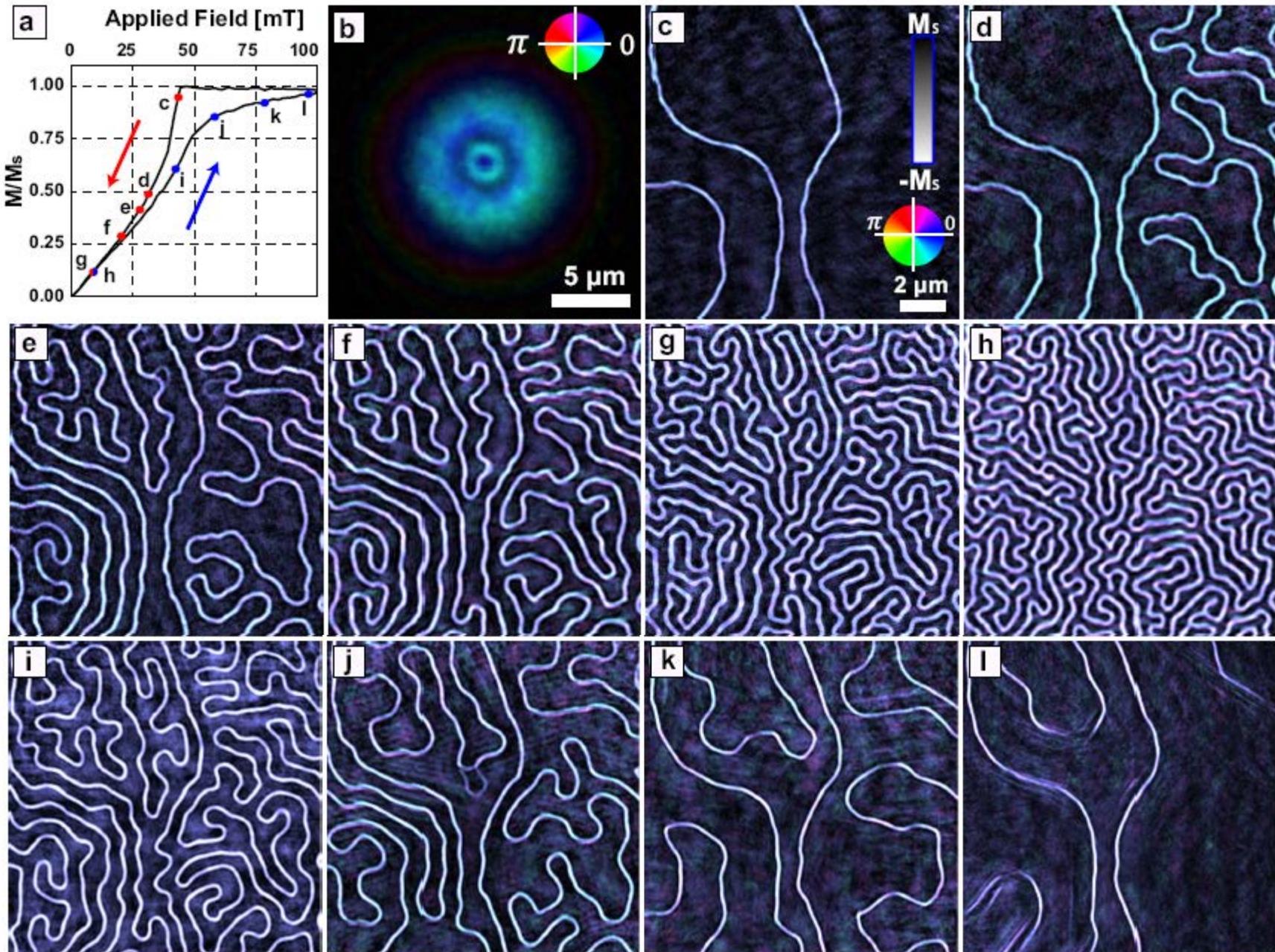
Argonne  
NATIONAL LABORATORY

# REAL SPACE RECONSTRUCTION

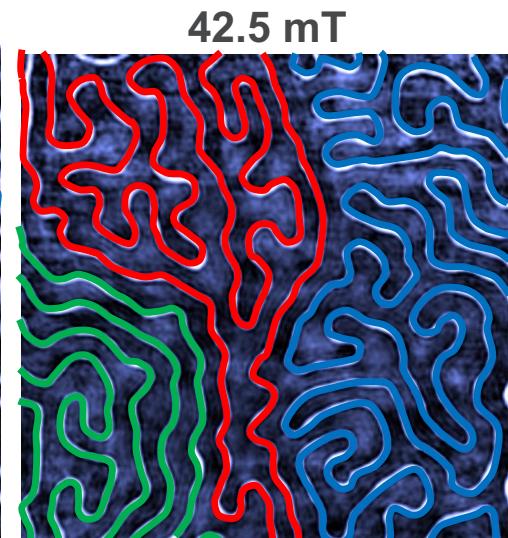
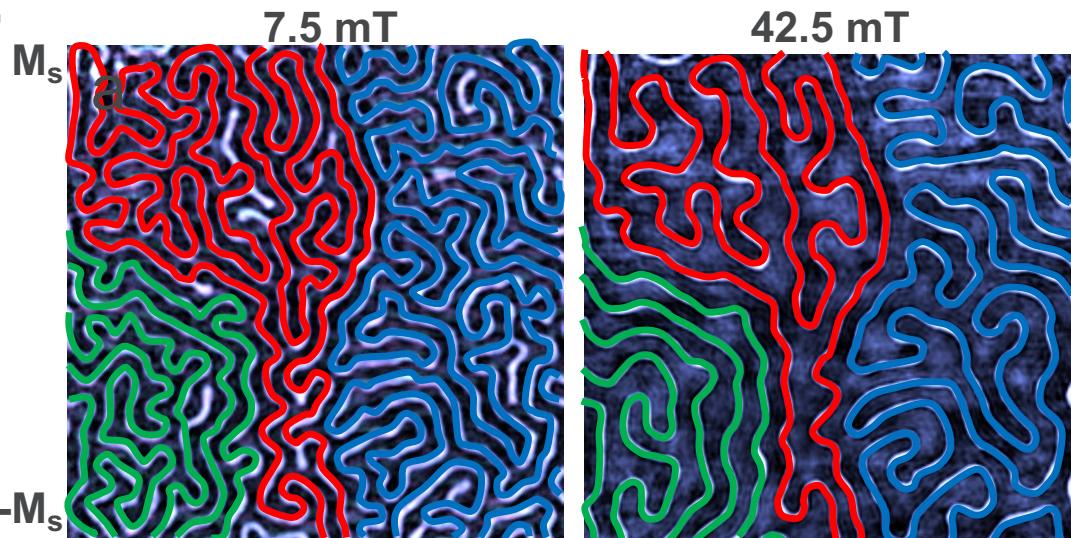
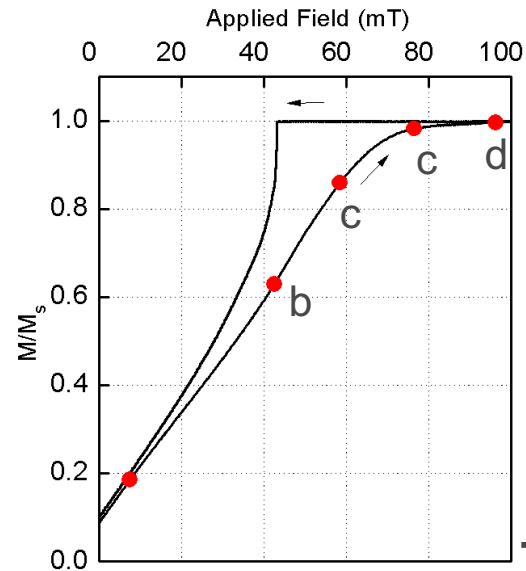


Magnetic structure  
(exit wave)

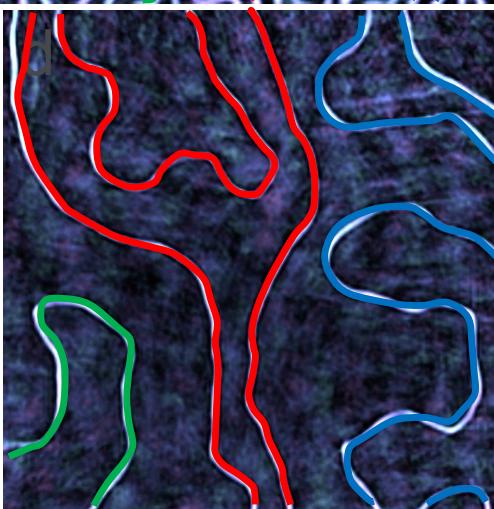
Illumination Function



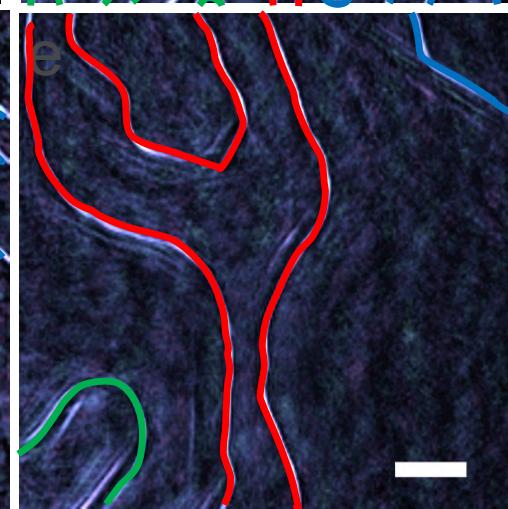
# INCREASING FIELD



58.5 mT

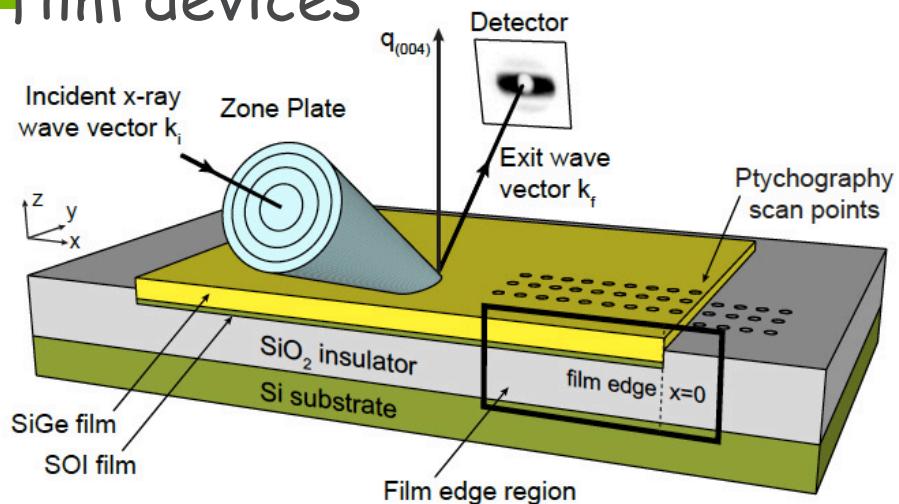


76.5 mT

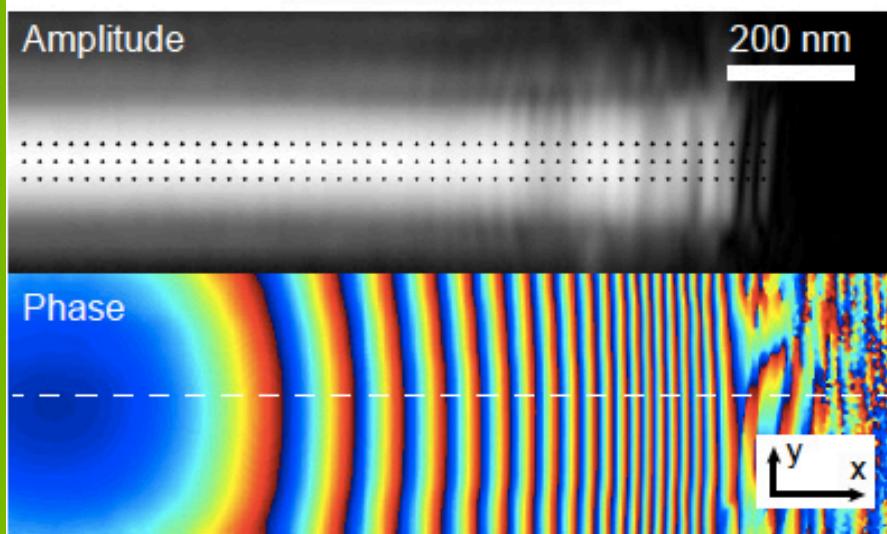


96.5 mT

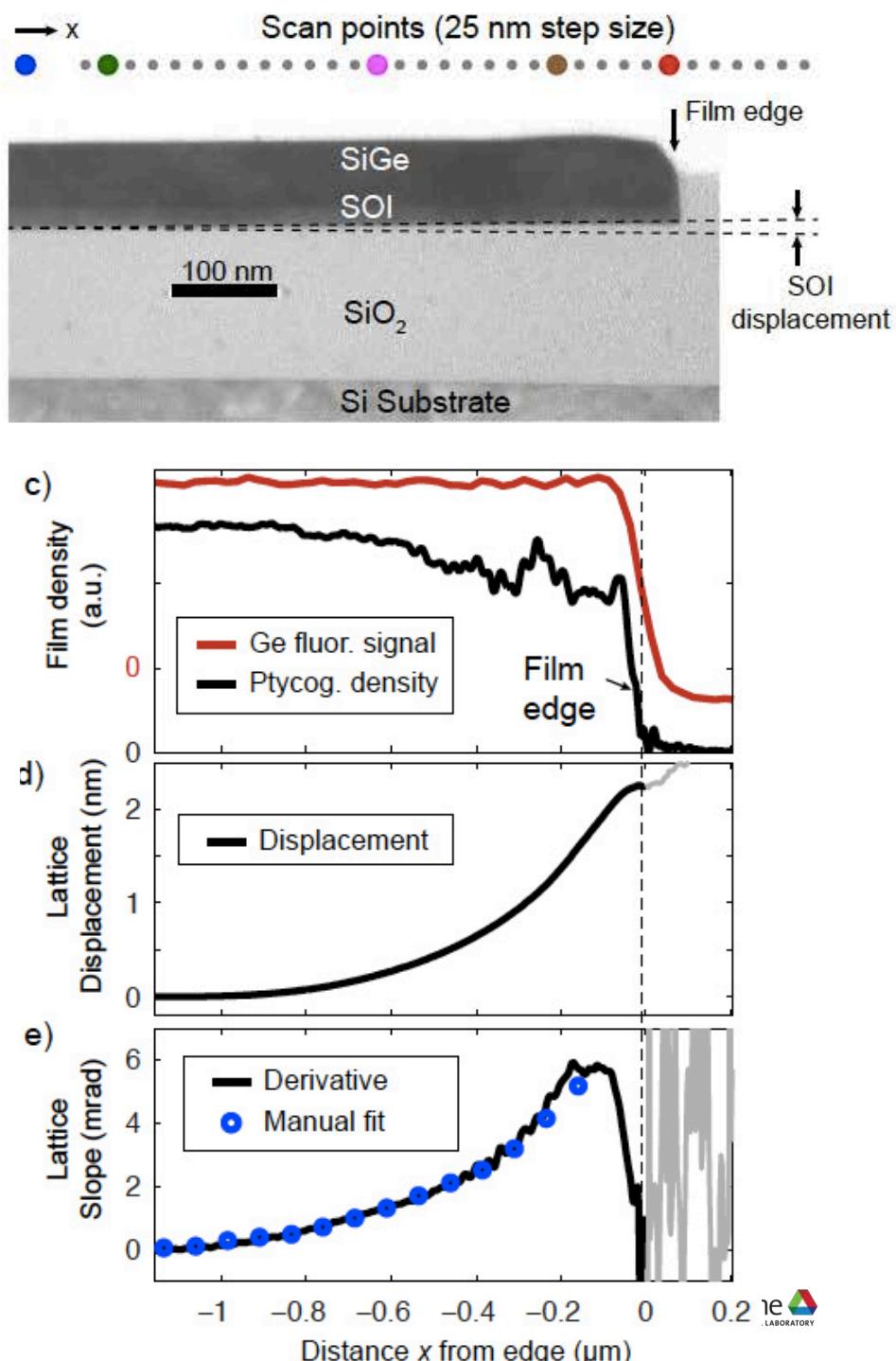
# Nanoscale Strain in SiGe film devices



Film Reconstruction

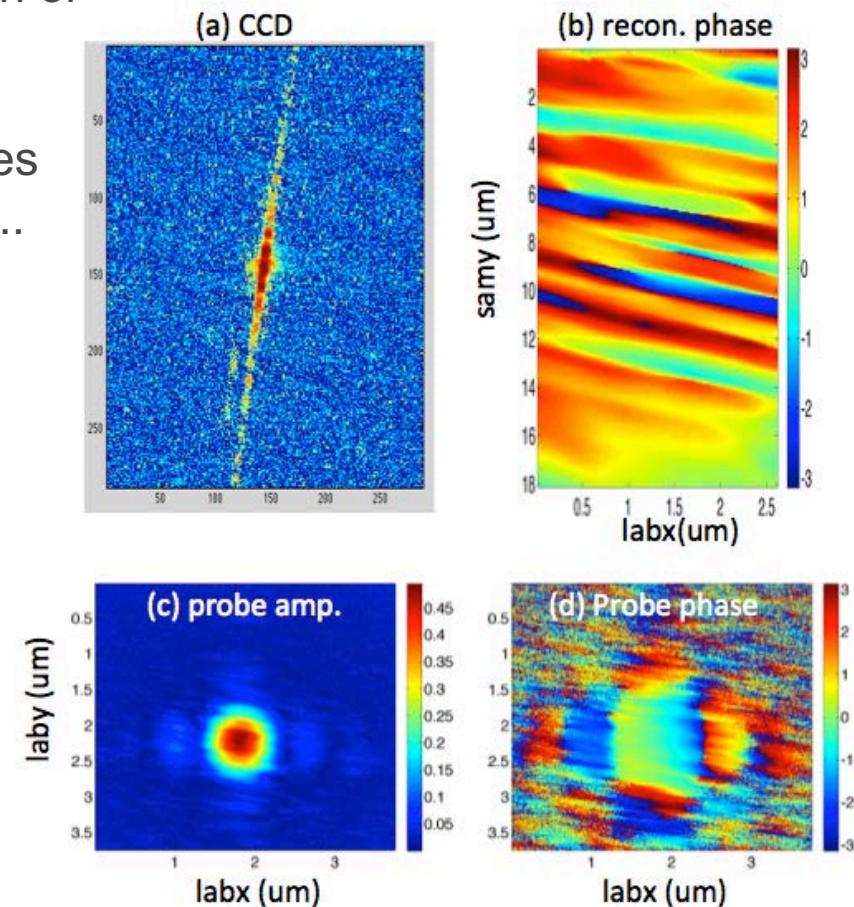
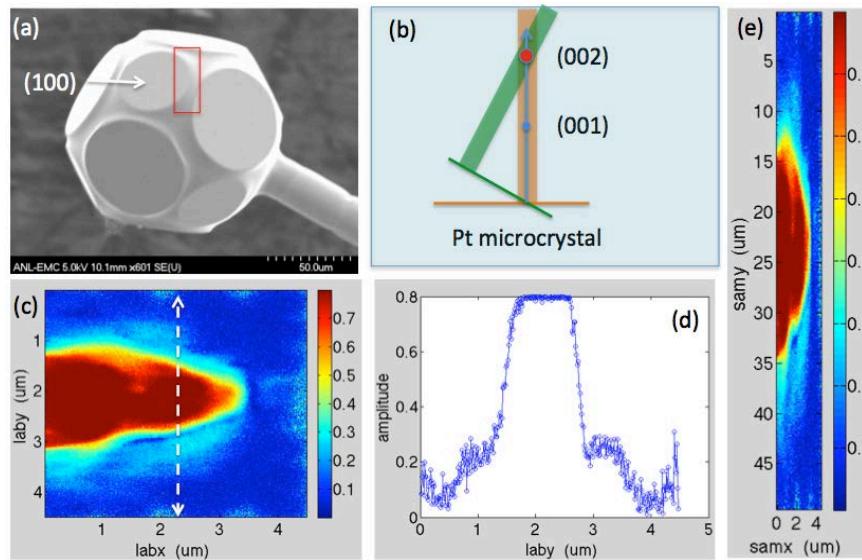


Hruszkewycz, S. O., Holt, M. V., et al.  
(2012). *Nano Letters*, 12(10), 5148–5154.



# SURFACE DIFFRACTION COHERENT IMAGING

- Image local surface structure
- Steps and step dynamics during film growth or interfacial reactivity
- Nanoparticle nucleation
- Defect distributions, particularly at interfaces
- Combined with x-ray micro fluorescence.....

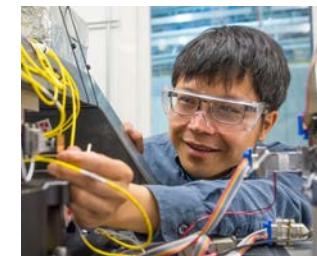
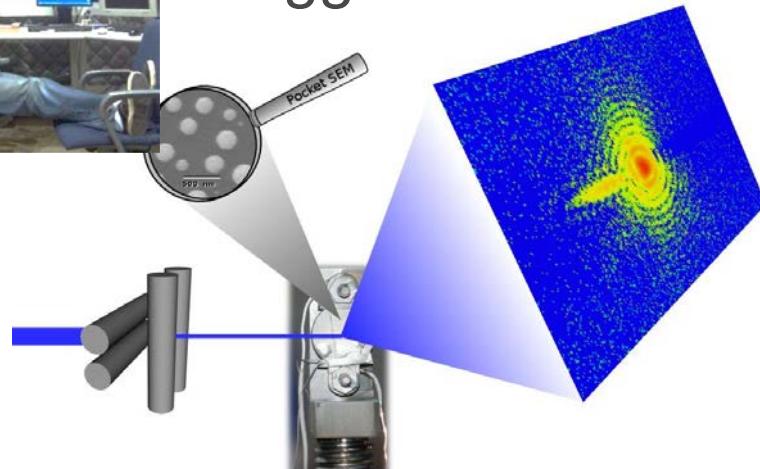


C. Zhu, et al. *Applied Physics Letters*, vol. 106, no. 10, p. 101604, Mar. 2015.

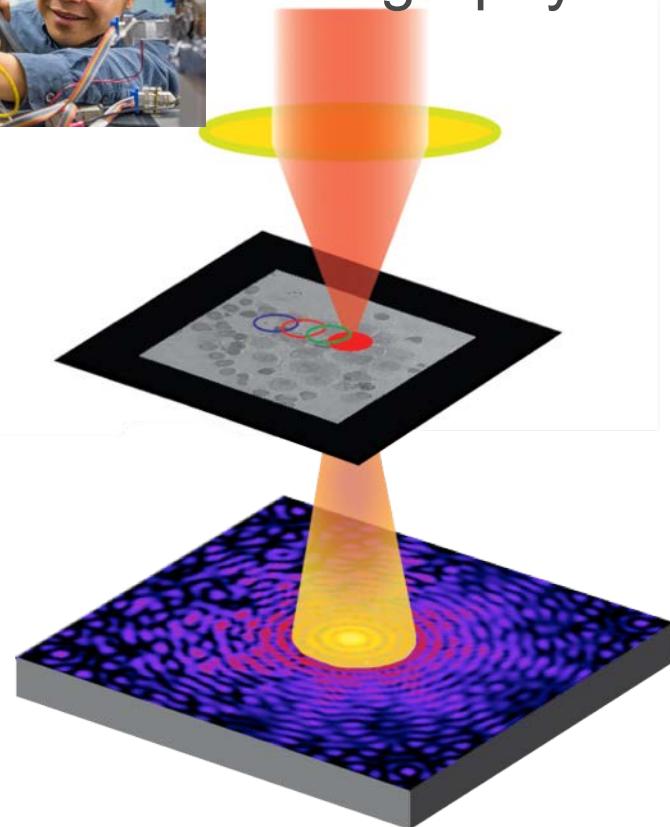
# APPLY FOR COHERENT IMAGING BEAMTIME @ APS!



## Bragg CDI

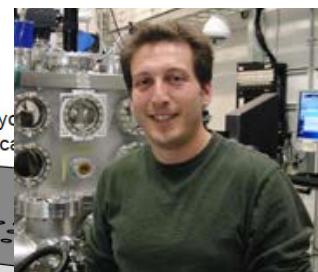
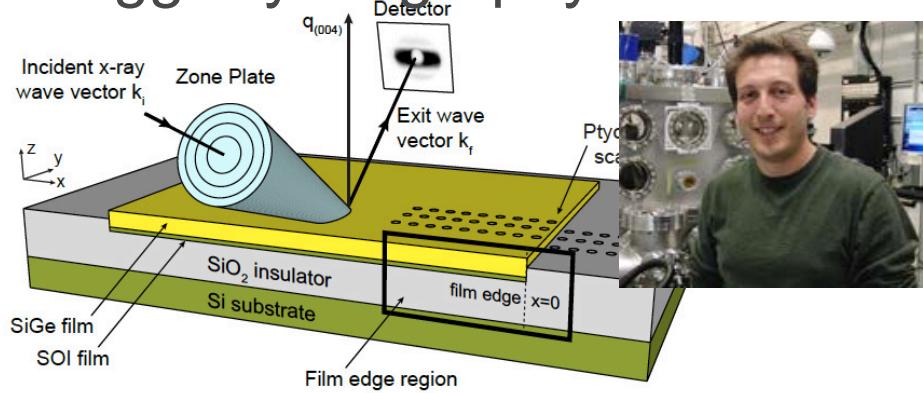


## Ptychography Tomography



Email: Ross Harder [rharder@aps.anl.gov](mailto:rharder@aps.anl.gov)  
<https://wiki-ext.aps.anl.gov/s34idc/index.php/34-ID-C>

## Bragg Ptychography



Email: Martin Holt [mvholt@anl.gov](mailto:mvholt@anl.gov)  
<https://wiki-ext.aps.anl.gov/s26id/index.php/26-ID>

Email: Junjing Deng [junjingdeng@aps.anl.gov](mailto:junjingdeng@aps.anl.gov)

<https://www.aps.anl.gov/Users-Information>